Engineering Tripos Part IIA, 3C7: Mechanics of Solids, 2019-20

Module Leader
Prof V Deshpande [1]

Lecturers
Prof V Deshpande, Dr C Abadie

Lab Leader
Dr C Abadie [2]

Timing and Structure
Michaelmas Term, 16 lectures

Prerequisites
None

Aims
The aims of the course are to:

- Provide students with an understanding of how the stresses and strains within engineering components are related to both the loads and displacements imposed at their boundaries and to any thermal or inertial loadings to which they are subjected.
- Introduce analytical methods, predominantly for two-dimensional geometries and for both elastic and plastic response.
- Illustrate the methods with a number of engineering case studies.

Objectives
As specific objectives, by the end of the course students should be able to:

- Calculate the stresses in an elastic or plastic axisymmetric system subjected to various loads.
- Use Airy and Prandtl stress functions to find analytical solutions to elastic problems.
- Apply upper- and lower-bound theorems to solid mechanics problems.

Content
Two-Dimensional Elasticity (6L): Prof V Deshpande

- Revision of stress and strain in 2D; Mohr's circle.
- Elastic constitutive relationship.
- Concepts of plane stress and plane strain.
- Equilibrium and compatibility equations in 2D; Cartesian and polar coordinates.
• Analysis of problems with circular symmetry: thick-walled tube, spinning disk, thermo-elastic problems.

**Torsion, Stress Functions and Plasticity (4L): Prof V Deshpande**

• Elastic torsion of prismatic bars: Prandtl stress function.
• Plastic torsion of prismatic bars.
• Airy stress function in Cartesian and polar coordinates.
• Stress distribution in an infinite plate with a circular hole or crack.
• Analysis of contact stresses; half-plane under line and distributed loads.

**Stress analysis in 3D and Plasticity (6L): Dr F Cirak**

• Stress analysis in 3D: principal stresses; stress invariants; hydrostatic and deviatoric stresses; deviatoric stress invariants.
• Yield locus, pi-plane; symmetry; convexity; normality.
• Tresca and von Mises yield criteria; associated flow rules.
• Upper-Bound and Lower-Bound theorems.
• Applications of Upper-Bound and Lower-Bound theorems: thick-walled tubes; rotating disks.
• Revision of rigid block mechanisms: application to forming problems. Elasto-plastic analysis of a thick-walled tube.

**Examples papers**

There will be four Examples Papers, directly related to the lectures.

**Coursework**

**Experimental Stress Analysis**

Use experimental techniques to determine the stress concentration at the edge of a circular hole in finite plates.

**Learning objectives:**

• To develop an appreciation of errors that occur in experimental measurements of stresses using strain-gauges.
• To note that the stress concentrations are sensitive to the location of the hole in the plate.
• To compare measured concentration factors with simple analytical predictions.

**Practical information:**

• Sessions will take place in South Wing Mechanics Lab.
• To sign-up go to [http://to.eng.cam.ac.uk/teaching/apps/cuedle/index.php?context=3C7](http://to.eng.cam.ac.uk/teaching/apps/cuedle/index.php?context=3C7) [3].
• Reports should be posted into the Post Box outside room BE3-39 (Ms Hilde Hambro-Fernandez)

**Full Technical Report:**

Students won't have the option to submit a Full Technical Report.

**Booklists**

Please see the [Booklist for Part IIA Courses](http://teaching.eng.cam.ac.uk) [4] for references for this module.

**Examination Guidelines**

Please refer to [Form & conduct of the examinations](http://teaching.eng.cam.ac.uk) [5].