Engineering Tripos Part IIB, 4F7: Statistical Signal Analysis, 2020-21

Module Leader
Dr S.S. Singh

Lecturer
Dr S.S. Singh

Timing and Structure
Michaelmas term. 16 lectures (including examples classes). Assessment: 100% exam

Prerequisites
3F3; Useful 3F1 and 3F8

Aims
The aims of the course are to:

- Continue the study of statistical signal processing techniques from the basics studied in 3F3.
- Introduce time-series models, in particular State-space models and hidden Markov models; understand their role in applications of signal processing.
- Develop techniques for fitting statistical models to data and estimating hidden signals from noisy observations.

Objectives
As specific objectives, by the end of the course students should be able to:

- Understand state-space models and hidden Markov models including their mathematical characterisation, strengths and limitations.
- Understand how to execute all the necessary computational tasks involved in fitting the models to data, to estimate unobserved quantities and make future predictions.
- Understand the computational methodology employed, their mathematical derivation, their strengths and weaknesses, how to execute them, and their use more generally in Statistical and data-centric engineering problems.

Content
This course is about fitting statistical models to data that arrives sequentially over time. Once an appropriate model has been fit, tasks like predicting future trends or estimating quantities not directly observed can be performed. The statistical modelling and computational methodology covered by this course is widely used in many applied areas. For example, data that arrives sequentially over time is a common occurrence in Signal Processing (Engineering), Finance, Machine Learning, Environmental statistics etc.
The model that most appropriately describes data that arrives sequentially over time is a time-series model, an example of which is the ARMA model (studied in 3F3.) However, this course will look at more versatile models that incorporate hidden or latent state variables as these are able to account for richer behaviour. Also, models that aim to describe how many really physical processes evolve over time often necessarily have to incorporate unobserved hidden states that form a Markov process.

- Introduction to state-space models and optimal linear filtering; the Kalman filter; exemplar problems in signal processing.
- Introduction to hidden Markov models: definition; inference/estimation aims; exact computation of the conditional probability distributions.
- Importance sampling: introduction; weight degeneracy; statistical properties.
- Sequential importance sampling and resampling (also known as the particle filter): application to hidden Markov models; filtering; smoothing.
- Calibrating hidden Markov models: maximum likelihood estimation and its implementation.
- Exemplar problems in Signal Processing.

Booklists

Please refer to the Booklist for Part IIB Courses for references to this module, this can be found on the associated Moodle course.

Examination Guidelines

Please refer to Form & conduct of the examinations [2].

UK-SPEC

The UK Standard for Professional Engineering Competence (UK-SPEC) [3] describes the requirements that have to be met in order to become a Chartered Engineer, and gives examples of ways of doing this.

UK-SPEC is published by the Engineering Council on behalf of the UK engineering profession. The standard has been developed, and is regularly updated, by panels representing professional engineering institutions, employers and engineering educators. Of particular relevance here is the 'Accreditation of Higher Education Programmes' (AHEP) document [4] which sets out the standard for degree accreditation.

The Output Standards Matrices [5] indicate where each of the Output Criteria as specified in the AHEP 3rd edition document is addressed within the Engineering and Manufacturing Engineering Triposes.

Last modified: 01/09/2020 10:38