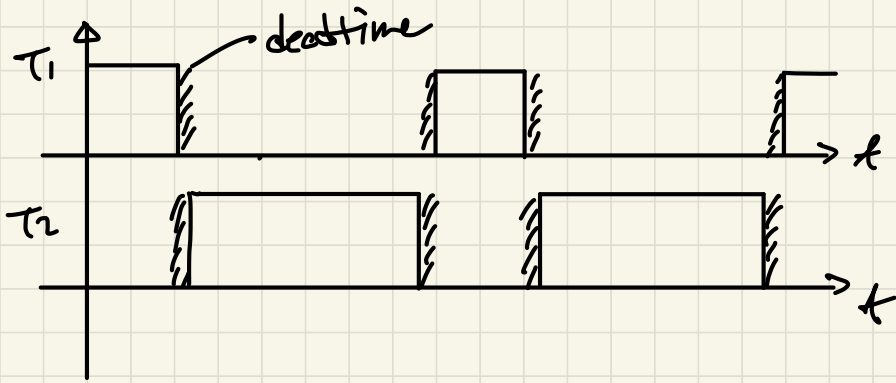
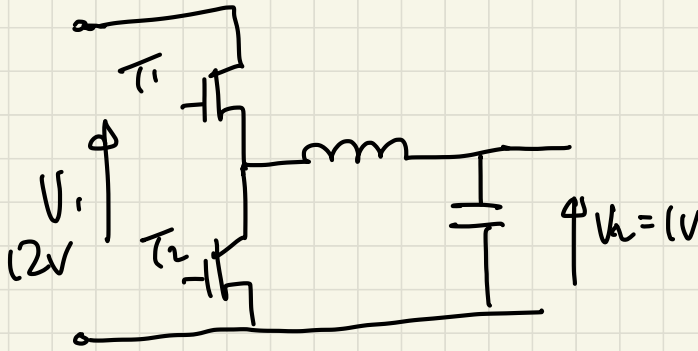
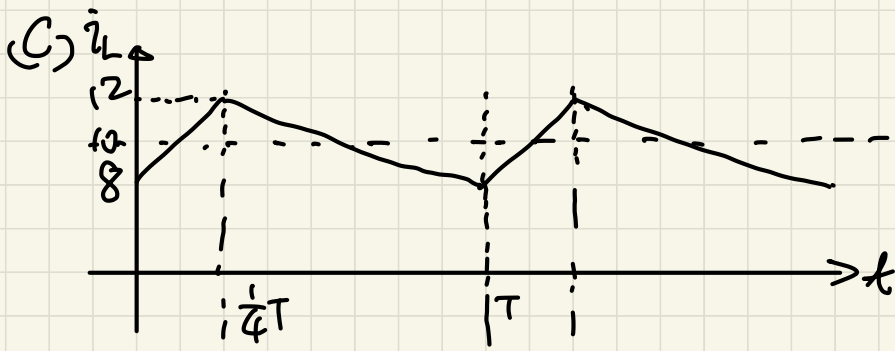


Q1

(a)



(b) T_2 has lower switching loss. The body diode of T_2 conducts current during deadtime. Therefore, when T_2 switches on after the deadtime, it has nearly zero voltage and the switching on loss is nearly zero.

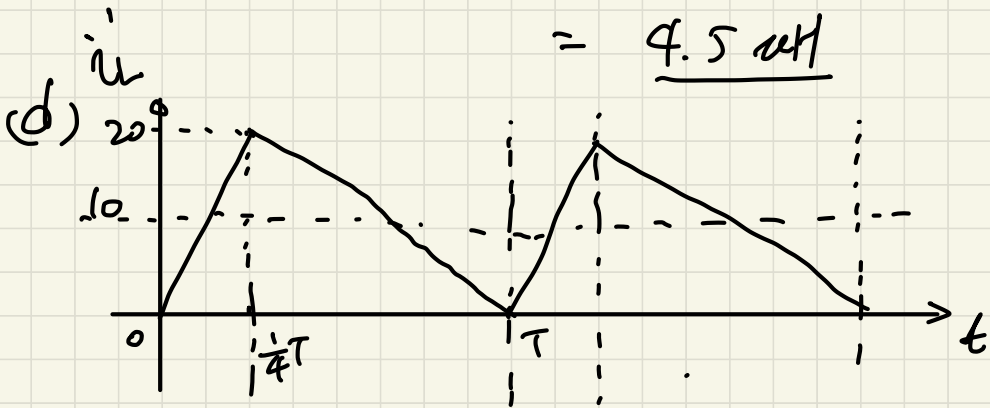


$$L \frac{\Delta i_L}{\Delta t} = V_1 - V_2, \quad L = \frac{(V_1 - V_2) \Delta t}{\Delta i_L}$$

$$= \frac{(48 - 12) \times \frac{1}{4} \times \frac{1}{500 \times 10^3}}{4}$$

$$= 4.5 \times 10^{-6} \text{ H}$$

$$= \underline{4.5 \mu\text{H}}$$



$$L' = \frac{(V_1 - V_2) \Delta t}{\Delta i_L'} = \frac{(48 - 12) \times \frac{1}{4} \times \frac{1}{500 \times 10^3}}{20}$$

$$= \underline{0.9 \mu\text{H}} \quad 8$$

(c) $0 < t < \frac{T}{4}$, T_1 conducting.

$$P_{T_1} = \frac{\int_0^{\frac{T}{4}} i_{T_1}^2 R dt}{T} = \frac{R}{T} \int_0^{\frac{T}{4}} \left(\frac{80}{T} t\right)^2 dt = \frac{(80)^2 R}{T^3} \frac{t^3}{3} \Big|_0^{\frac{T}{4}}$$
$$= \frac{100}{3} R = \underline{0.067W}$$

$\frac{T}{4} < t < T$, T_2 conducting.

$$P_{T_2} = \frac{\int_{\frac{T}{4}}^T i_{T_2}^2 R dt}{T} = \frac{R \int_{\frac{T}{4}}^T \left(\frac{80}{3T} t\right)^2 dt}{T} = 100R = \underline{0.2W}$$

// Alternative: using RMS current to find the total

loss. $P = \left(\frac{20}{3}\right)^2 \cdot R = 0.267W$. $P_{T_1} = \frac{1}{4} P = 0.067W$

$P_{T_2} = \frac{3}{4} P = 0.2W$
//

(f) CCM:

$$I = I_{DC} + I_{ripple}, \quad I_{ripple} \text{ has peak value } 2A$$

$$I_{RMS} = \sqrt{I_{DC}^2 + I_{ripple\ RMS}^2} = \sqrt{10^2 + \left(\frac{2}{\sqrt{3}}\right)^2}$$

$$P_{loss\ CCM} = I_{RMS}^2 R = \left(100 + \frac{4}{3}\right) R$$

Critical CCM

$$I = I_{DC} + I_{ripple}, \quad I_{ripple} \text{ has peak value } 10A$$

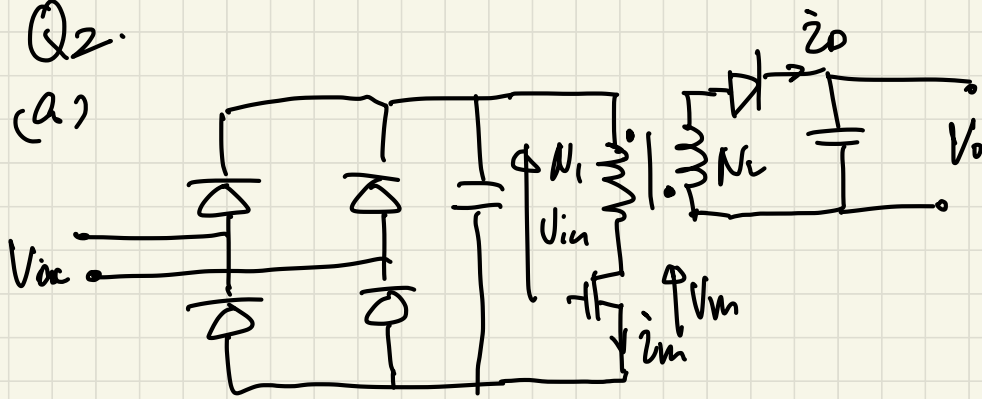
$$I_{RMS} = \sqrt{I_{DC}^2 + I_{ripple}^2} = \sqrt{10^2 + \left(\frac{10}{\sqrt{3}}\right)^2}$$

$$P_{loss\ critical\ CCM} = \left(100 + \frac{100}{3}\right) R$$

$$\frac{P_{critical\ CCM}}{P_{CCM}} = \frac{\frac{400}{3}}{\frac{304}{3}} = \underline{1.315}$$

Q2.

(a)



(b) The capacitor is very large thus the DC voltage is clamped at the peak voltage of input.

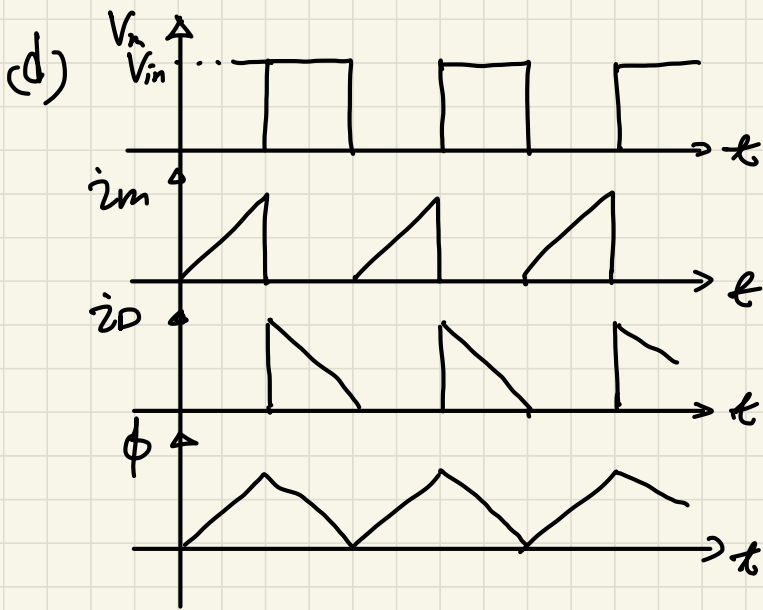
$$V_{DC} = \sqrt{2} \cdot V_{ac rms} = \sqrt{2} \times 230 = \underline{325V}$$

The input current is very distorted so the power factor is poor.

(c) Flux is continuous, $\frac{V_o}{V_{in}} = \frac{N_2}{N_1} \frac{D}{1-D}$

It's a step down Flyback, thus $\frac{N_2}{N_1} = \frac{1}{20}$

$$\frac{D}{1-D} \cdot \frac{1}{20} = \frac{15}{325}, \quad D = \underline{0.48}$$



e) Max B_m is set by saturation point

$$B_m = 0.75 \times 0.36 = 0.27 \text{ T.}$$

$$\phi_m = B_m \cdot A = 0.27 \times 0.25 \times 10^{-4} = 0.0675 \times 10^{-4} \text{ Wb}$$

$$N_1 \frac{d\phi}{dt} = V_{in}$$

$$N_1 = \frac{\Delta t V_{in}}{\Delta \phi} = \frac{DT V_{in}}{\Delta \phi} = \frac{0.48 \times \frac{1}{500 \times 10^3} \times 325}{\phantom{0.48 \times \frac{1}{500 \times 10^3} \times 325}}$$

$$= 46.2 \approx 46$$

$$N_2 = \frac{46}{20} = \underline{\underline{2.3 \approx 2}}$$

Using the modified turns ratio $\frac{46}{2} = 23$,

modified duty ratio $\frac{D'}{1-D'} = 23 \times \frac{15}{325}$

$$D' = 0.515$$

(f)

Assum: ① B is evenly distributed in the core

② Leakage inductance is neglected.

$$\frac{I_{2\max} \cdot (1-D)T}{2} = I_2 \cdot T$$

$$I_{2\max} = \frac{2I_2}{1-D} = \frac{2 \times 2}{1-0.515} = 8.25 \text{ A}$$

Magnetic inductance referred to 2nd side,

$$V_o = L_m \frac{\Delta \hat{i}_2}{\Delta t}, \quad L_m = \frac{V_o \Delta t}{\Delta i_2} = \frac{V_o (1-D)T}{I_{2\max}}$$
$$= \frac{15 \times 0.485 \times \frac{1}{100 \times 10^3}}{8.25}$$
$$= 1.76 \times 10^{-6} \text{ H}$$

$$L_m = \frac{N^2 \mu_0 \mu_r A}{l},$$

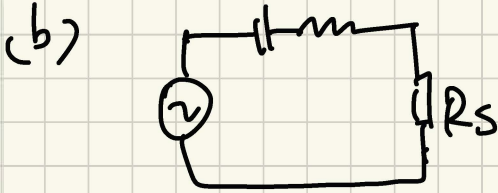
$$\mu_r = \frac{L_m \cdot l}{N^2 A \mu_0}$$

$$= \frac{1.76 \times 10^{-6} \times 10^{-2}}{2^2 \times 0.27 \times 10^{-4} \times 1.26 \times 10^{-6}}$$

$$= \underline{139.6}$$

Q3

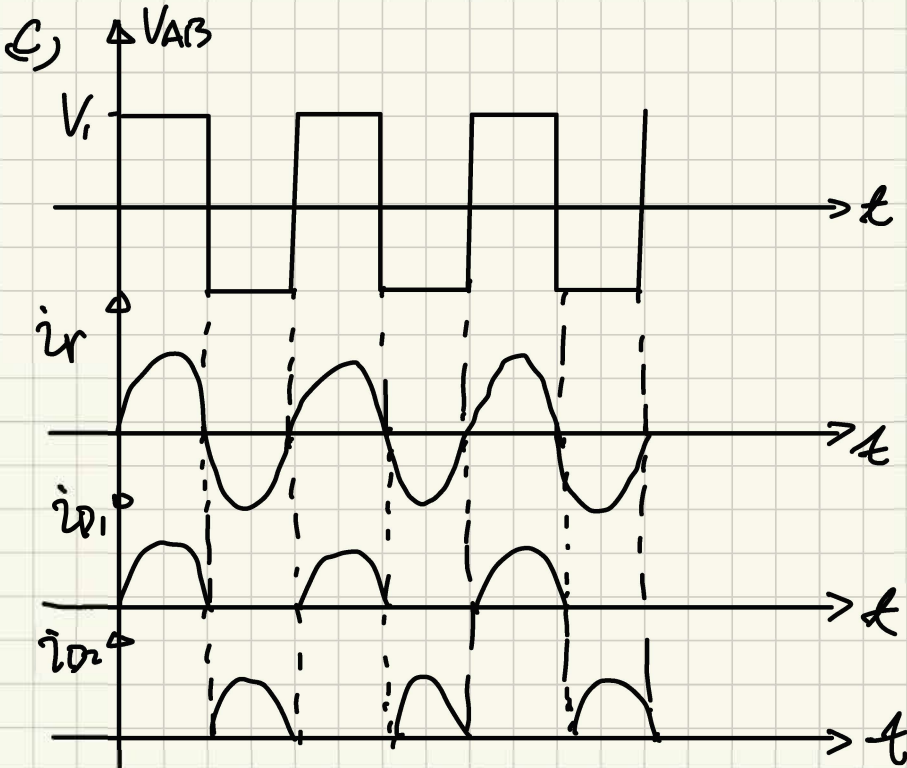
$$a) f_r = \frac{1}{2\pi\sqrt{LC}}$$



Voltage square, current sin.

$$R_s = \frac{N^2 \cdot \frac{2\sqrt{2}V_0}{\pi}}{\frac{\pi I_0}{2\sqrt{2}}} = N^2 \frac{8R}{\pi^2}$$

$$R_s = \frac{8N^2 R}{\pi^2}$$



(d) The magnetizing inductance of transformer is very large, At f_s , the tank impedance is zero.

Therefore,
$$V_o = \frac{\hat{V}_{AB1}}{N} = \frac{4 V_i}{a N}$$

(e) In this LLC, $Q = \frac{L_m}{L_r} \rightarrow \infty$.

When Q is small, the gain changes insignificantly when f_s deviates from f_r .

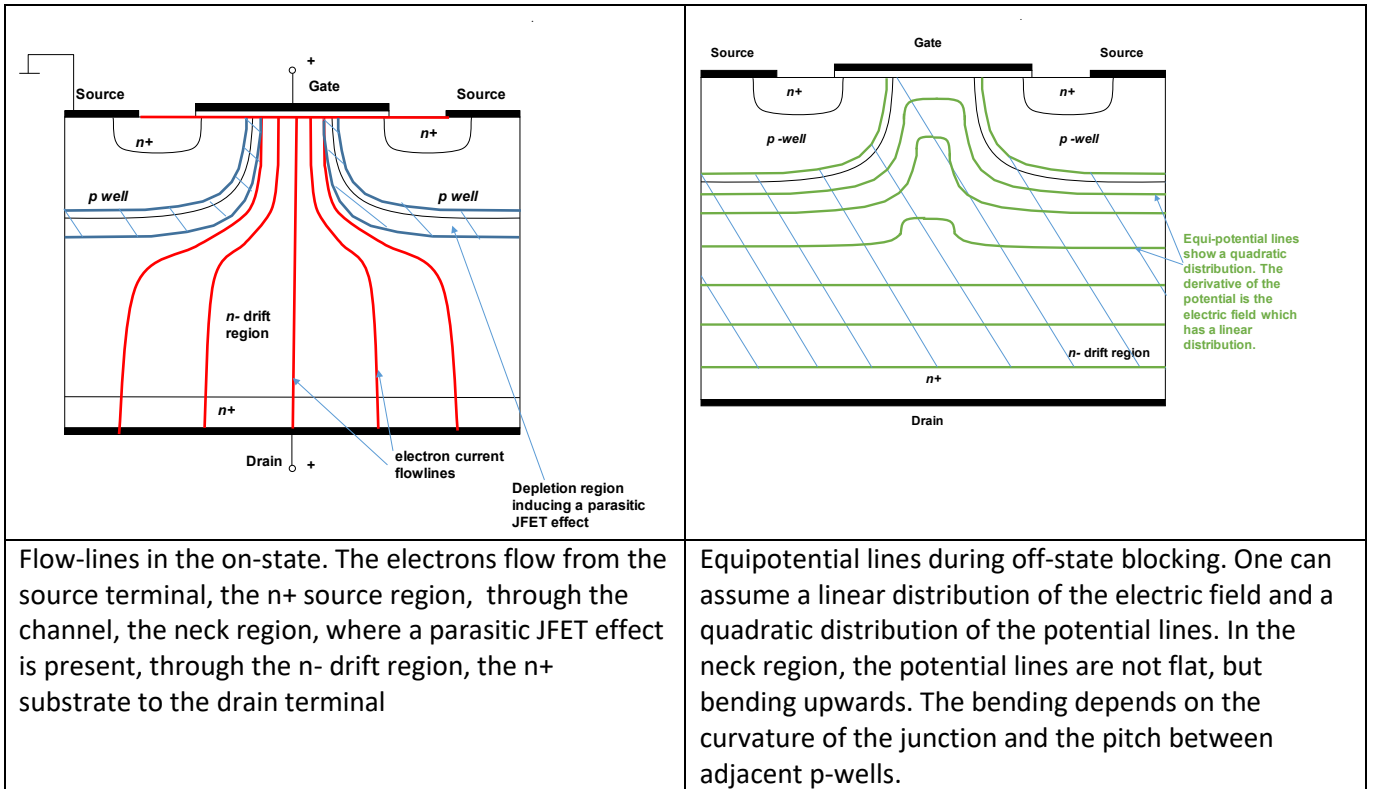
For a given rated current, the Q can be set to be small. Then, when the load is reduced Q can only be even smaller. The load does the gain is becoming even smoother. Thus the gain

has even smaller changes when f_s is not f_r .

Therefore, no matter the load changes, the gain remains nearly unchanged.

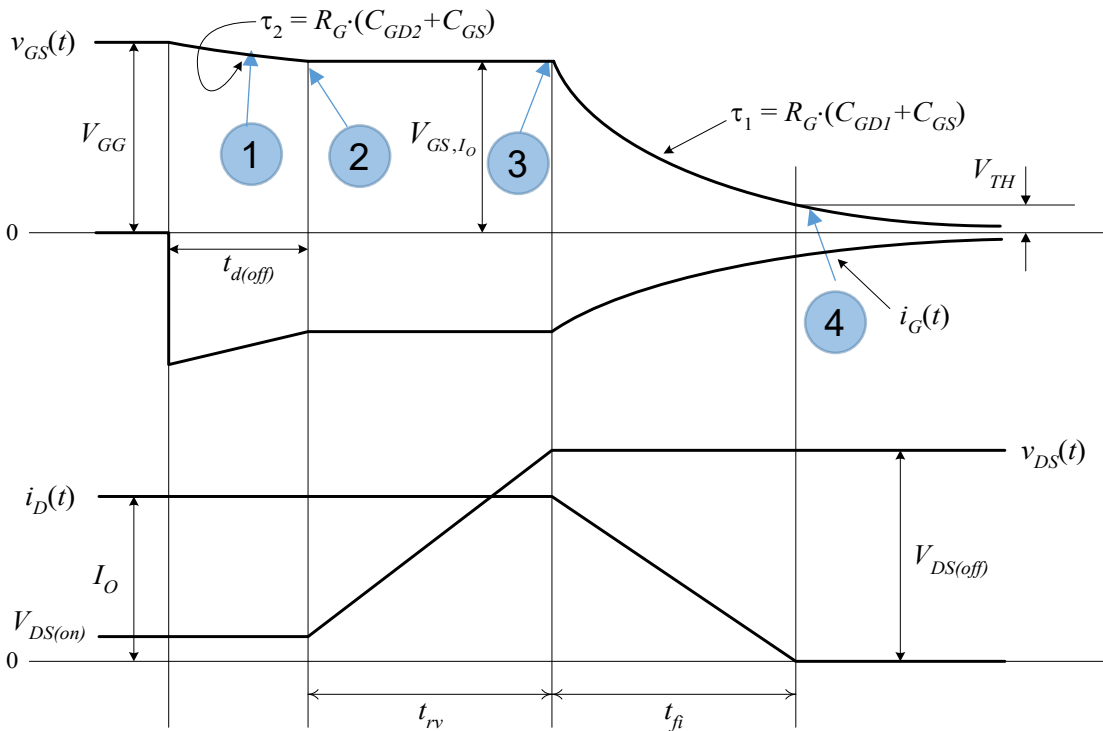
Q4

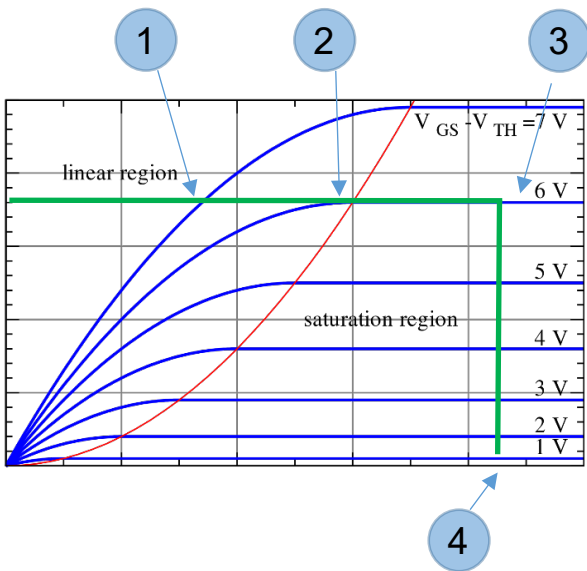
a)



[20%]

(a)

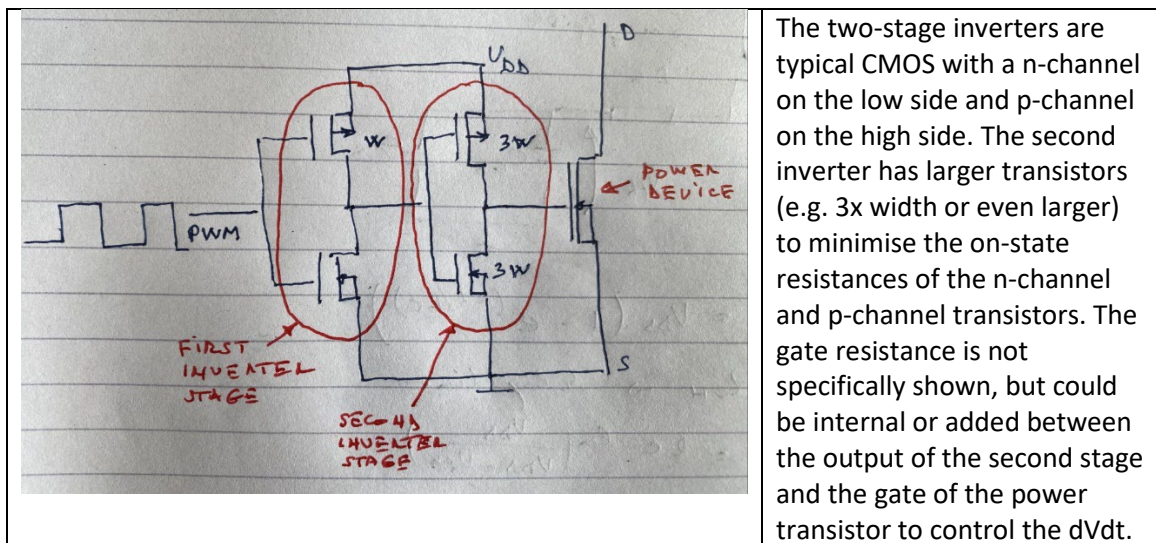




- C_{GD1} - Miller capacitance (saturation region – this capacitance is small)
- C_{GD2} - Miller capacitance (linear region – this capacitance is large)
- C_{GS} - Gate-Source capacitance
- t_{doff} - Initial delay time
- t_{rv} - Rise time in which v_{DS} reaches its off-state value $V_{DS(off)}$ from $V_{DS(on)}$
- t_{fi} - Time taken for i_D to fall from its full load value I_D to 0; the end of this

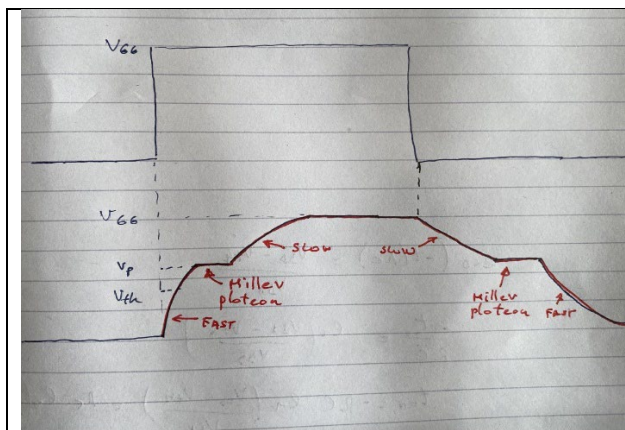
[40%]

(b)

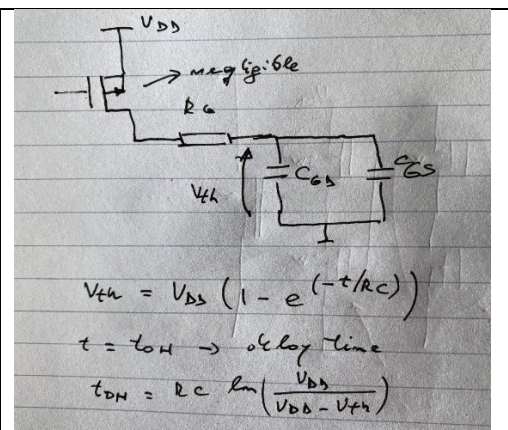


The two-stage inverters are typical CMOS with a n-channel on the low side and p-channel on the high side. The second inverter has larger transistors (e.g. 3x width or even larger) to minimise the on-state resistances of the n-channel and p-channel transistors. The gate resistance is not specifically shown, but could be internal or added between the output of the second stage and the gate of the power transistor to control the dVdt.

[15%]



The shape of the gate signal is dictated by the switching conditions (here it is shown to be inductive) [15%]



The turn-on delay time is until the channel becomes open – V_{th} . The input capacitance is the parallel combination of C_{GD} and C_{GS} . $R = R_G$. $C = C_{GS} + C_{GD}$ [10%]