

Answers

1. (a) $f'(x) = -g'(x) = -(I/2\rho c)\delta(x - x_1)$, $f'(-ct) = f'(ct)$, $f'(ct - L) = f'(ct + L)$
 $\dot{u}(x, t) = (I/2\rho)\{\delta(x - x_1 - ct) + \delta(x - x_1 + ct)\}$
- (b) Average velocity is $I/\rho L$, the same result as a rigid rod.
- (c) $\dot{u}(x, t) = I \sum_n \phi_n(x) \phi_n(x_1) \cos \omega_n t$, $T = (I^2/2) \sum_n \phi_n^2(x_1) \cos^2 \omega_n t$.
- (d) From the above summation T is infinite at $t=0$. The delta function impulse is an unrealistic simplification from this point of view.
2. (a) $k = \omega\sqrt{m/T}$.
- (b) $u(x, t) = -(F/Tk) \cos \omega t \sin kx_1 \sin k(x-L)/\sin kL$ for $x > x_1$.
- (c) $u = A \cos \omega t \sin k(x_2 - L)/\sin k(x_1 - L)$, $\omega_n = n\pi\sqrt{T/m}/(L - x_1)$.
- (d) $C = \sqrt{2/mL}$, $u(x_1, t) = \left(\frac{2F \cos \omega t}{mL}\right) \sum_n \frac{\sin^2(n\pi x_1/L)}{\omega_n^2 - \omega^2}$
- (e) Both results tend to $-(F/5\pi\delta) \sin^2(5\pi x_1/L)/\sqrt{mT}$.