Y 2021-22 4010 In= 47540 cm<sup>4</sup>. Iyy = 2007 cm<sup>4</sup> Zy = 2059 cm<sup>3</sup> (n-anis). I= 51.5 cm<sup>4</sup>; A = 105 cm<sup>2</sup> Qui 529.3 -D > K-96 1=51. man = 82.2 kg/m. = 13 mm. 5355 grade; 208.8 (4) P=OKN 208.8-9.6-2×13]/2]/13.2 in companyis) ty; grade > 6.56 12 235 355 = 0.814 class (1) 528.3 - 2x13.2 -Midemen 2×13 ]/9.6] vadis tor web. 4 = (in bending) 49.57 722 = 58.68 () a > 49.57. , 50 clam 150 contrical moment = I JEIGJ 1+ EZ ET in internal torquiral 12 GT = Iyy d<sup>2</sup> 1y = (2007 × 104) × (528.3 - B.2)<sup>2</sup> 1y = 1.3297 × 10<sup>12</sup> mm6 with L= 6m. give for data dreet : Cunequal =) 0.6 Mur 10.6 Mar = Mir/Cunequal =

ELyy 65 = 210×109 × (2007)×108 × 81×109 (51.5)×108 E(Ta) Imp(m4) 6(Ta J(m4))  $= 1.758 \times 10^{11} (Nm^2)^2$ .  $E \overline{7}_{65} = 210 \cdot \frac{1.33 \times 10^{12}}{51.5 \times 10^{4}} = 6.70 \times 10^{6} \text{ mm}^{2}$  $M_{LT} = \underline{\underline{H}} \left[ \underline{E} \underline{\Gamma}_{qq} \underline{G} \underline{J}^{\mu} \left[ 1 + \underline{\overline{n}}^{2} \underline{E} \underline{\Gamma} \right]^{\mu} \right]$  $= \frac{\pi}{6} \left[ \frac{1.758 \times 10^{11}}{1.758 \times 10^{11}} \right]^{1/2} \left[ \frac{1}{62} + \frac{\pi^2}{62} \left( \frac{6.70 \times 10^6}{62} \right) + 10^{-6} \right]^{1/2}$ 1.68 = 369.79KNm  $M_{cr} = M_{r} | C_{nnegnd} = \frac{370}{6.6} = \frac{616.3 \text{ kN}_{m}}{-1000}$   $M_{pl} = \frac{730.9 \text{ kN}_{m}}{-1000}$  $\lambda = \int M_{\rm M} = \frac{731}{616} = \frac{1.09}{-9.000}$ hlb>Z =) use onne bad o (ingrenfedr for = 0.34 (if proson calc) heading up => X=0.54 for h=1.09 curves. =) Mmax = XMM = 0.54 + 730.9 = 395 kNm

clan move X= Ey, all Cr- $\frac{(1-1)^{2}}{(1-1)^{2}} \times \frac{(1-1)^{2}}{(1-1)^{2}} \times \frac{(1-1)^{2}}{(1-$ 0 Ŀ. b fran 528.3 355 = 1.16  $(1 - 0 - 22) = 0.698 \pm 0.7$ .sect: p= Foreff 156-6 mm. removed 155.6+9.6 Aven = 105 cm2 155.6. (9006×10-(210×104) × (47590 × 10 6842.51 mid-legh. -disedu, sebbi IN y  $= \frac{12}{6^2} \left( \frac{2059 \times 10^{-8}}{6^2} \right) = \frac{1185}{6^2}$ = II ZELMY Pur ()P.V.O

1 = 3KH = 1.64. } b-cuive for ( =) 2) is more contrical (lower X.) ~ 0.3 from reading DSI => Atbrah limital = 0.3×3197 = 959 kN. linear inberrich inve. MUNM 34 M\*=271 for P(kn) ... (1×1× (300,300) Ve canvie = 271.

(rivden won-sech. (5355 Qui Longth (axial) = 27m 350230 Aven = 2x350x30 + 1200x14 7800 mm2 andu 350,30 17010130 1200×14/12+ 2× 350×30 /2+ = 7.94×10 mm 4 018+10 mm of- quider = 27m => 2714 = 6.75m: actual q of- quiden = 3.5 < 6.75=> effective stab lag spring of g width = 5.5 name weight <u>63.5m</u> [\_\_\_\_\_\_\_\_\_\_\_ (37800+10-6 x 9.-81 A m[52. Inguider tor the state: 2400 x (3.5×0.2) × 9.81 = 17.16 KN/m lond Inclus 1)erd load fordow = 1.5. when volling point moment Md accus middle of  $M_{d} = 300 \times \frac{27}{4} + \frac{27.07 \times 27}{8} = \frac{4491.8 \text{ Wm}}{8}$ ()distributed loading

trume NA in the steel; force in concrete = 0.6 falt/hppxy = 0.6 × (30×10°) + 3.5×0.2 = 12600kN QuZ O.bfed (epp x h) Axial eqlm: (2.p. 0.35). f-y heff + Ny. 0.35 Fy (160-x) 0.6fcd = (As-(Asty-0.6falhbeff-2×0.35× =  $\chi_{\mu} =$ 355×10 =) np = 3.3 my [np +0.35xfy = 409 kN]. Moment for force Machs: 1 = 409 × ×p12 + 12600 < [100 + ×p] + (13419-409) × 1256.7 = 9477.5 kNm [c.f. 9311 kNm if m = 0] 1256.7 M = - 409 [c.f. 9311 kNm Keynwel moment = 4491.8 hom " sufficie Assume a shear connector barght ZZmm how duta sheet: Prd = (0.8 fry. trd2/4 Yv 1.35. - fu= 450M/ => 1ed = 0.8 (450+106) + 17 + 0.022 / 1.25 = 109.56N  $\frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} \frac{1}{\sqrt{1-1}} \frac{1}{\sqrt{1-1}} = \frac{1}{\sqrt{1-1}} \frac{$ 

Select lower PRJ=109.5h.N: # connector= Wed. Quz  $= \frac{12600}{109.5} = 115$ Need to bransform Section to all steel, ming modulant value = 210/33 = 6.36 => JJ 1 1 100 35/6.36 3.5/1.7L = 550 mm d is locale of new prevall N.A. 2 Ky = dx2A: (550x200k 00+ 350x30x [200+15+ 200+1200+30+15 10pfluge blan fluge + (1200+14) ~ [200+30+60] = d. [550+200+2+350+30+ => d = 286.8mm. the new Ixx for the section is needed In = 550 ×2003/12 + (550×200) + 1872 + Ienguden II Ion black + A \* 5432. 1 200130+100-287 = 543 7-944109 + 37-8007+5432 23.30×109 mm4 Need to calculate storen a blow from, located 543+600+30 = 1173 =)  $T = \frac{M_y}{I} = \frac{19102 \times 1073}{(23.3 \times 10^9) \times (10^{-12})} = \frac{51.7 M_y}{I}$ M# = moment when the cave is '14 of the way across the bridge = 150 kN × 2714 = 1013 kNm readmatssypport-However, need to include factored load => 51.771.35 = 69.710

Qu2] The # cycles to forhave is Nor (10 1 = K, m=3. Kin Min come in (2x10) x (71)3: At in Mila.  $2 \times 10^{6} + 71^{3} = N_{1} \times (69.71)^{3}$ 27 =)  $N_{\rm P} = 2.205 \times 10^6$  cycles.

Studend diedes une local brickling for fluges [ web, in comprenie, beding and in streat. Elements need to the "stockier" because of higher Quis (ai) higher yield To deal with local buckling "k" must be allocated numerically for each adrian: (aii) k = 4 (internal), 0.43 (esternal) : comptension<math>k = 23.9 : bending k = 5.34 = shear. For For outstand in compression: (-13)  $\pi^2 = (-1)^2$  $12(1-\nu^2)$   $(-1)^2$  $\frac{-2) 0 \cdot 43 \times \overline{u^{2}} \cdot (210 \times 10^{9}) (\frac{1}{2})^{2} \cdot 960 \times 10^{6} = \frac{1}{2} \cdot \frac{1}{2} \cdot 85 = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{9}{2} \cdot \frac{2}{2} \cdot \frac{9}{2} \cdot \frac{2}{2} \cdot \frac{9}{2} \cdot \frac{2}{2} \cdot \frac{2}{2}$ Web in beding: 73.9 = 2 (210×10] (6/2) > 960×10<sup>6</sup> => < 68.74 12(1-52) In shew: 5.34 m² (210×10°) (t) 2> 160×10°=7 <= 5 24:67 12(1-52) (t) 3 == 5 24:67  $\frac{4\pi e_{m}}{12} = \frac{2 \times 200 \times 5 \times 2 \times 190 \times 5}{190 \times 190^{3}} = \frac{3900 \text{ mm}^{2}}{12}$ 200- $V_{cv} = \bar{n}^{2} ET = \bar{n}^{2} (210 + 10^{4}) + (24 + 73 + 10^{6}) + 10^{-12} 227.8 \text{ km}$ 0

ZJer = Per/A = 227.8×103/[3900-10-6] = 58.42Mla Ju 3) For 5235:  $\lambda = \int F_{4} = 735 = 7.00 \quad 4 = 190 \quad 38 = 7$   $\overline{0.7} = \sqrt{58.4} = \frac{7.00}{12} \quad 4 = 5 = 100 \quad 38 = 7$ Use budding curve c, as suggested. => X = 0.2 (for vending mp) => actual limita land 0.2 ~ A ~ fy = 0.2 ~ (3900~10<sup>-6</sup>) ~ (235~10<sup>6</sup>) = 183 kN  $F_{47} \leq 960$ ;  $\Sigma = 235 = 235 = 0.495$ ; 425 = 20.8 $c.f. C_{1} = 38 > 472 = 7 (lam 4) structure : used$  $X = 4 (internal : compression) = 4 · <math>\pi^{2} E = (E_{1})^{2} = G_{2}r.$   $E = 4 (internal : compression) = 4 · \pi^{2} E = (E_{1})^{2} = G_{2}r.$   $I_{2}(1-v^{2}) = 525Mla$ => Ocr = 523MPa  $\lambda = \int \frac{460}{525} = 1.35 \quad = \frac{1}{2} \left[ 1 - 0.22 \right] = 0.62$ => App = pA = 0.62×3900 (=) p televis b = 7418 mm<sup>2</sup> left-befind after remark Ter = ler/Aeff = 227.8+103 = 94.2 M/2 N= Ity = J960 = 3:19 which is beyond the graphical rage : for course c, d(imp. Backer) = 0.49  $\phi = 1 + \alpha (\lambda - 0.2) + \lambda^2 = 6.32 =) \chi = \frac{1}{\phi + \sqrt{\phi^2 - \lambda^2}} 1.5.1$ 

 $\chi = \frac{1}{6\cdot 32 + 16\cdot 32^2 - 3\cdot 14^2} = 0.085.$ Qu3. =) actual limit of Per = X Aeff Fy = 0.025x(2418+106) × 960 × 106 = 197.12 kN - limit of 183kN par 5235: a diff of 14kN! Kemon: Aender column, buckling at high & (low X > close to claritic Einter prediction in both cases: The effectiveness or combribation, from having a high yield Soven, is not realized.

Verign monunt = 3500 kNm : theory force = 1500 kN. Need the usual three in the top flage centrood, ad at the punction of web-to-flage: therefore, delermine I for the unspliced sector. I 2 1200 × 14 + 2×(30×350) × 615<sup>2</sup> 12 = 9.959×10<sup>9</sup> mm<sup>4</sup> 1350×10 Qu4)  $\frac{\log \beta \log \varphi}{\log \varphi} = \frac{My}{I} = \frac{(3500 \times 10^3) \times 0.615}{(9.959 \times 10^9) \times 10^{-12}} = \frac{216.14 M/a}{I}$   $\frac{\log \varphi}{I} = \frac{My}{I} = \frac{9.959 \times 10^9}{10^9} \times 10^{-12} = \frac{216.14 M/a}{I}$ bolt check in sheart: each M22 grade 8.3 bolt ca Suntin a max sheart force of. 22mmp 2 × 0.6 × Aven × Fub 2 200 HPa at-yield. : aven = Ti × (0.00)<sup>2</sup> double sheart Yuz 21.1 => force = 331.8 km Each rde of punct: has & holts => capacity= 7654kN The axial force in top flange = Ter x A [216+106] + 0.35 +0.03 +216+10a = 7268kN : enough bolls for shear. Intrud area Splice plate melding => [0.35+2+0.15]+0.016 + (355+106) 350+16 32,55 150+16 4 12268,0K) 150+16 4 126 150+16 4

ly bearing: use USS. ooking at top plate in plu view: A = ei ar l'i 1 do-holt 3do 3do 4 diameter 1055 =)  $dA = \frac{50}{2} = 0.757$  at  $dA = \frac{100}{3} = \frac{1}{2} = 1.265$ . drugse 21 = 0.757 k, = 2.8ez/1 - 27 w 1.4tz/2 - 1.7 w 2.5 (whichever is smalled  $k_1 = \frac{2.8 \times 75}{22} - 1.7 = 7.85; k_1 = 1.4.200 - 1.7 = 11.03.$ ". choose k, = 2.5 Kho form 1155: Fo, Rd (bott capacity) = kabitu Ot  $X_b$  is smallest  $J - A_d$ ,  $f_{1b} = a + 1$ ;  $A_b = x_4 = 0.757$ 2 bearing zones >1=(300/490) => Fb, Rd = 2 × 1.5 × 0.69 × (490×106) × (0.022) × 0.016 R1 db Fr. 9 Ed-ple = 519kNAquin, 8 holls per side in bearing = 8+514=4154 kN (7266 ()

Local budding of outstand E = 16mm, c = 75mm: use k = 0.43.  $G_{47} = 0.43 \overline{u}^2 E$   $(E_1)^2 = 0.43 \overline{u}^2 (210 \times 10^{2}) (16)^2 = 37.141$   $12(1-v^2) (E_1)^2 = 12(1-0.3^2) (75)^2 = 37.141$ Qn 4  $\frac{0 \times 10^{a}}{3^{2}} \left( \frac{16}{75} \right)^{2} = \frac{3714}{714} \frac{14}{14}$ Ter >> Fu (490 MPa) .. ok. Wy web connection need to find applied nt from M= o I web o = top junder stron = y 20.9 MPa frakefor  $M = (210.9 \times 10^{6}) \times (0.014 \times 1.2^{3} / 12) / 0.6 = 7056 \text{ km}$ Tweld force in each bolt M. M. Zr<sup>2</sup>. 100,00,100 in calculation of Eriz × 4 for whole 150. 150. 150. 150. 150. 150  $\sum_{v=1}^{2} = \left[ 4 \times 50^{2} + 75^{2} + 725^{2} + 15375^{2} + 525^{2} \right]$ 100 + 4x 1502+ 752 7 2252 7 375 7 5252] et cluster 1045-10 mm 2. = . 421, = 4180+10<sup>3</sup> mm<sup>2</sup>, Finas = Imas. M Erz Finax = 150 -> 5254  $F_{max} = \left[ \underbrace{OF15^{2}10.525^{2}}_{T_{max}} \right]^{1/2} \times \left( \frac{705.6 \times 10^{3}}{(4180 \times 10^{3}) \times 10^{-6}} \right]^{1/2} = \frac{92.12 \text{ kN}}{(4180 \times 10^{3}) \times 10^{-6}}$ =7 ()

furthert bolt 92.26N (-appled 16 = 93.75k N sherr force. 944 for moment) = J92.22+93.752 - 131.5kN =) Total shear for Previous capacity determined to be 331.8kN, MmOK! the duck bearing med local broking of web and splice place. the

## Q1 Beam-column capacity

Part (a) was generally well answered. The most common mistakes were: (i) using the fully plastic moment in the calculations, without checking whether the beam was indeed Class 1 or 2; (ii) using the full length L=12 m in the check for lateral-torsional buckling, thus ignoring the out-of-plane restraint at mid-span; and (iii) using the wrong y-value in calculating  $C_{unequal}$ . Out of the two 6 m long segments to be checked for lateral-torsional buckling, the segment subject to the larger moments was critical, and thus: y = 0.5 and  $C_{unequal} = 0.8$ .

In Part (b), a small minority of students did not check the class of the cross-section in compression (despite the guidance in the question) and thus failed to realize it was Class 4. In the calculation of the column slenderness, the numerator should contain  $A_{eff} f_y$ , while the Euler load in the denominator is based on the *gross* section properties. It is also not immediately clear whether minor axis buckling ( $L_{cr} = 6$  m, smaller I) or major axis buckling ( $L_{cr} = 12$  m, but larger I) would be critical and both needed to be checked.

## Q2 Composite floor-decking design

Part (a) was generally well answered. A common (relatively minor) mistake was to use the characteristic concrete strength,  $f_{ck}$ , in the calculations, rather than the design strength,  $f_{cd} = f_{ck}/1.5$ . In the calculation of the applied moment, the self-weight of the composite beam was quite often ignored or calculated wrongly.

The most common mistake in Part (b) was the failure to realize that  $N_c/P_{Rd}$  results in the number of connectors over *half* the span.

In Part (c), very few students were able to correctly calculate the fatigue limit state moment as the moment at quarter-span, caused only by the (unfactored) point load, placed at quarter-span. The remainder of the question seemed much less problematic.

## Q3 Buckling and compactness design

Most students realized that local buckling would become a more prominent issue in high-strength steel beams but did not always draw the conclusion that the cross-sections would have to be more 'stocky' (containing less slender flanges and webs) to keep them inside Class 3. In Part (b) the most common oversight was not checking the class of the cross-section, resulting in a failure to realize that the S960 column was Class 4.

## Q4 Bolted splice joint design

A small minority of students attempted this question. While the connection looked perhaps intimidating due to the sheer number of bolts, the design checks were relatively straightforward. Almost all students correctly identified the various failure modes. Identifying a realistic tear-out mechanism in the flange plates appeared to be the most common problem.