

3A1 2003 Answers to exam questions

1. (a) see crib
(b) see crib
(c) see crib
(d) $U_T/U_C = 1/(1 + C_f P_T S_C / C_D A_C)^{1/2}$
(e) See crib
(f) $\Delta T = (1/2 C_D A_C L (U_C - U_T)^2 U_C) / (A_T C_p U_T S_C)$
(g) $\Delta T = \Delta T(\eta_c = 1) * (2 - \eta_c)$
2. (a) $L = \rho U^2 \pi c \sin \alpha$
(b) $L = 2 \rho U^2 \pi c \sin \alpha (1 + 4(\tilde{h}/c)^2) / (4 + 8(\tilde{h}/c)^2)$
(c) see crib
3. (a) $F(z) = Uz + (i\Gamma/2\pi)(\ln(z+ia) - \ln(z-ia))$
(b) $\zeta = a^{3/2} e^{i3\pi/4}$ (and origin maps to corner)
(c) $\Gamma = -\pi a U$
(d) $u - iv = 1/2 U a^{-1/2} e^{-i\pi/4}$
4. (a) $V_p 4s^2 \Gamma / \pi h / (9s^4 + 10s^2 h^2 + h^4)$
(b) $h = 0.86s$
(c) see crib
5. (a) $d\Gamma = (d\Gamma/dz) dz$
(b) $\Gamma_{op} = (3\pi/8) \Gamma_{oc}$
(c) $w_p/w_c = 3/2$
(d) see crib

6. (a) $u/U_e = \sin(\pi\eta/2)$
- (b) (i) $\delta^* = (1 - 2/\pi)\delta$
- (ii) $\tau = \delta(2/\pi - 1/2)$
- (iii) $T_w = \pi\rho\nu U_e/\delta$
- (c) see crib
- (d) $\delta = x (2\pi/(4/\pi - 1))^{1/2} R_x^{-1/2}$
- $C_f = ((4 - \pi)/2)^{1/2} R_x^{-1/2}$
7. (a) see crib
- (b) $L = (\rho\nu/\sigma B^2)^{1/2}$
- (c) $U = \cosh(z/L) - \cosh(h/2L)$
- (d) see crib
8. (a) $\Psi = U \sin\theta(r - a^2/r)$
- (b) 12% error
- (c) $F_y = -(4/3)\rho a U^2$ (down-force)
- (d) see crib