

ENGINEERING TRIPOS PART II A

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Friday 7 May 2004 2.30 to 4.00

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Module 3C4

MACHINE DESIGN - TRANSMISSIONS

*Answer not more than three questions.*

*All questions carry the same number of marks.*

*The approximate percentage of marks allocated to each part of a question is indicated in the right margin.*

*Attachments:*

*Special datasheet (10 pages).*

You may not start to read the questions  
printed on the subsequent pages of this  
question paper until instructed that you may  
do so by the Invigilator

(TURN OVER

1 (a) Describe carefully how a belt drive system might be used as part of a continuously variable transmission system for a motorised scooter. Identify relevant design issues in the belt drive system and briefly outline suitable design calculations. [25%]

(b) Figure 1 is a sketch of a two stage planetary drive. The main input shaft, which drives the first sun wheel  $S_1$ , rotates at a speed  $\omega_i$ . An additional input shaft, which rotates at a speed  $\alpha\omega_i$ , is attached to the planet carrier  $C_1$ . Annulus  $A_1$  is rigidly connected to planet carrier  $C_2$  and planet carrier  $C_1$  is rigidly connected to the second sun wheel  $S_2$ . Output is via the second annulus  $A_2$ . The tooth numbers are:  $S_1$  40 teeth,  $A_1$  80 teeth,  $S_2$  30 teeth,  $A_2$  90 teeth.

(i) For the case where  $C_1$  is held fixed ( $\alpha = 0$ ), find the speed and direction of the output shaft in terms of  $\omega_i$ . [25%]

(ii) For the general case where  $C_1$  rotates at a speed  $\alpha\omega_i$ , derive an expression for the speed and direction of the output shaft in terms of  $\omega_i$  and  $\alpha$ . [25%]

(iii) For a value of  $\alpha = 1/8$ , find the proportion of the output power flowing through the sun wheel  $S_2$ . [25%]

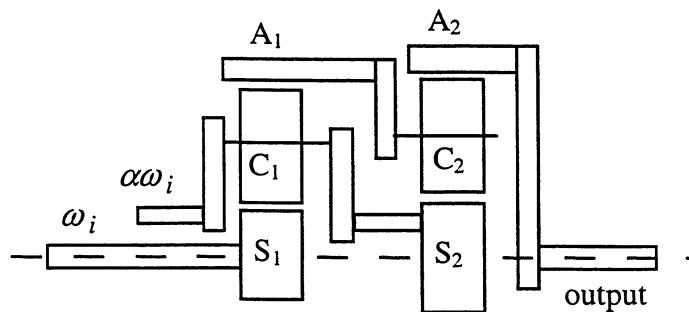


Fig. 1

2 (a) Sketch a typical Hooke's joint coupling, identifying the key components. Explain why it may be undesirable to have a variation in the ratio of input to output speeds as the joint rotates. Describe how a uniform speed ratio is achieved in practice. [25%]

(b) Figure 2 shows a cam which operates a reciprocating roller follower of radius  $r$ . The cam has a base circle radius of  $3r$  and a tip circle radius of  $r$ . The distance between the centres of the tip and base circles equals  $3r$ . The line of action of the follower is offset by a distance  $r$  to the right of the axis of rotation of the cam. The centres of the base circle, tip circle and follower are O, A and B respectively. The cam rotates anticlockwise at a steady angular velocity  $\omega$ .

- (i) Draw an equivalent mechanism for the case of follower contact on the tip circle. Hence show that maximum lift occurs when O, A and B are collinear. [15%]
- (ii) Find the follower accelerations at minimum and maximum lift. [30%]
- (iii) Derive an expression for the follower acceleration when contact is along the straight flank, as a function of the angle of inclination  $\theta$  of the flank relative to the horizontal. [30%]

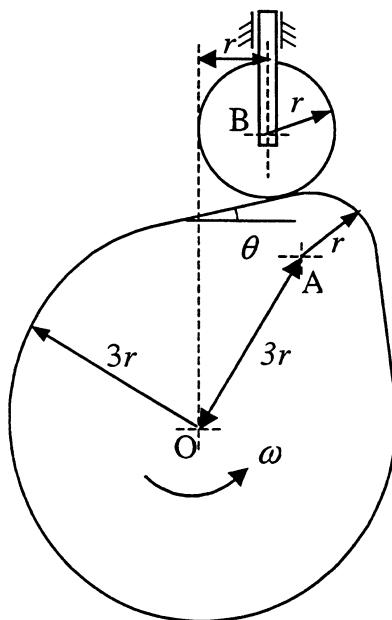


Fig. 2

3 A cyclist's maximum continuous torque output at the pedals is 80 Nm at zero pedal speed and 0 Nm at 20 rad s<sup>-1</sup>, with a linear variation of torque between these two speeds. The force resisting motion of the bicycle up a gradient can be taken as  $mg\alpha$  where  $\alpha$  is the gradient and  $g$  is the acceleration due to gravity. Speed dependent resistance can be neglected.

- (a) Determine the pedalling speeds between which the cyclist is able to generate at least 94 % of the maximum power output. [25%]
- (b) Sketch a graph of maximum output torque against output speed of the cyclist. On the same graph, sketch the form of the load characteristic. [15%]
- (c) The cyclist's bicycle has wheel radius  $r$  equal to 0.36 m, and the combined mass  $m$  of cyclist and bicycle is 90 kg. Determine the minimum number of speed ratios necessary to allow the cyclist to generate at least 94 % of the maximum power output when ascending gradients  $\alpha$  in the range 0.05 to 0.2, and determine suitable numerical values for the speed ratios. [60%]

4 (a) The powertrain of a typical passenger car consists of an internal combustion (IC) engine and a gearbox with manually selectable fixed ratios. Explain why the average fuel consumption of this vehicle under normal operating conditions is likely to be greater than the ideal figure derived from the minimum specific fuel consumption of the IC engine. Support your explanation with a sketch of a typical engine output characteristic.

[15%]

(b) Draw schematic diagrams of a series hybrid drive and a parallel hybrid drive, showing the direction and type of energy flows. Explain any benefits of the systems compared to each other and compared to the conventional arrangement described in (a).

[30%]

(c) The force  $f$  required to move the vehicle is given by

$$f = m \frac{du}{dt} + cu$$

where  $u$  is the speed of the vehicle,  $m$  is the mass and  $c$  is a viscous loss coefficient. The vehicle is designed for an operating cycle of period  $T$  consisting of constant acceleration throughout the first half of the cycle, from zero speed to speed  $V$ . Throughout the second half of the cycle there is constant deceleration back to zero speed. Energy is recovered during the deceleration phase.

(i) Neglecting energy conversion losses, show that the ratio of peak power consumption to mean power consumption is given by

$$\frac{6m}{cT} + 3 \quad [45\%]$$

(ii) Discuss the implications of the result given in (i). [10%]

**END OF PAPER**



## ENGINEERING TRIPPOS Part IIA

### Modules 3C3 and 3C4 Data Sheet

#### HYDRODYNAMIC LUBRICATION

##### Viscosity: temperature and pressure effects

Vogel formula  $\eta = \eta_0 \exp\left\{\frac{b}{T + T_c}\right\}$

Barus equation  $\eta = \eta_0 \exp\{\alpha p\}$

Roelands equation  $\eta = \eta_0 \exp\left\{[9.67 + \ln \eta_0] \left[ \left(1 + \frac{p}{p_0^*}\right)^\beta - 1 \right]\right\}$

##### Viscous pressure flow

Rate of flow  $q_x$  per unit width of fluid of viscosity  $\eta$  down a channel of height  $h$  due to

pressure gradient,  $q_x = -\frac{h^3}{12\eta} \frac{dp}{dx}$

##### Reynolds' Equation for a steady configuration

1-D flow:  $\frac{dp}{dx} = 12\eta \bar{U} \left\{ \frac{h - h^*}{h^3} \right\}$

$\bar{U}$  is the entraining velocity so that  $|\bar{U}h^*|$  is flow per unit width through the contact.

2-D flow:  $\frac{\partial}{\partial x} \left\{ \frac{h^3}{\eta} \frac{\partial p}{\partial x} \right\} + \frac{\partial}{\partial y} \left\{ \frac{h^3}{\eta} \frac{\partial p}{\partial y} \right\} = 12\bar{U} \frac{\partial h}{\partial x}$

##### Hydrodynamic lubrication of discs

$$\frac{h}{R} = C \frac{\eta \bar{U}}{W'} \quad \text{where } R \text{ is the reduced or effective radius and } W' \text{ the load per unit length}$$

$C_{\min} = 4.00$  for half Sommerfeld boundary conditions

$C_{\min} = 4.89$  for half Reynolds' boundary conditions

## ELASTIC CONTACT STRESS FORMULAE

Suffixes 1, 2 refer to the two bodies in contact.

$$\text{Effective curvature } \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

where  $R_1, R_2$  are the radii of curvature of the two bodies (convex positive).

$$\text{Contact modulus } \frac{1}{E^*} = \frac{1-v_1^2}{E_1} + \frac{1-v_2^2}{E_2}$$

where  $E_1, E_2$  and  $v_1, v_2$  are Young's moduli and Poisson's ratios.

### Line contact

(width  $2b$ ; load  $W'$  per unit length) (diameter  $2a$ ; load  $W$ )

Semi contact width or contact radius

$$b = 2 \left\{ \frac{W'R}{\pi E^*} \right\}^{1/2}$$

$$a = \left\{ \frac{3WR}{4E^*} \right\}^{1/3}$$

Maximum contact pressure ("Hertz stress")

$$p_0 = \left\{ \frac{W'E^*}{\pi R} \right\}^{1/2}$$

$$p_0 = \frac{1}{\pi} \left\{ \frac{6WE^{*2}}{R^2} \right\}^{1/3}$$

Approach of centres

$$\delta = \frac{2W'}{\pi} \left[ \frac{1-v_1^2}{E_1} \left\{ \ln \left( \frac{4R_1}{b} \right) - \frac{1}{2} \right\} + \frac{1-v_2^2}{E_2} \left\{ \ln \left( \frac{4R_2}{b} \right) - \frac{1}{2} \right\} \right]$$

Mean contact pressure

$$\bar{p} = \frac{W'}{2b} = \frac{\pi}{4} p_0$$

$$\bar{p} = \frac{W}{\pi a^2} = \frac{2}{3} p_0$$

Maximum shear stress

$$\tau_{\max} = 0.300 p_0$$

$$\tau_{\max} = 0.310 p_0$$

at  $(x = 0, z = 0.79b)$

at  $(r = 0, z = 0.48a)$  for  $\nu = 0.3$

Maximum tensile stress

zero

$$\frac{1}{3}(1-2\nu)p_0 \text{ at } (r = a, z = 0)$$

### Mildly elliptical contacts

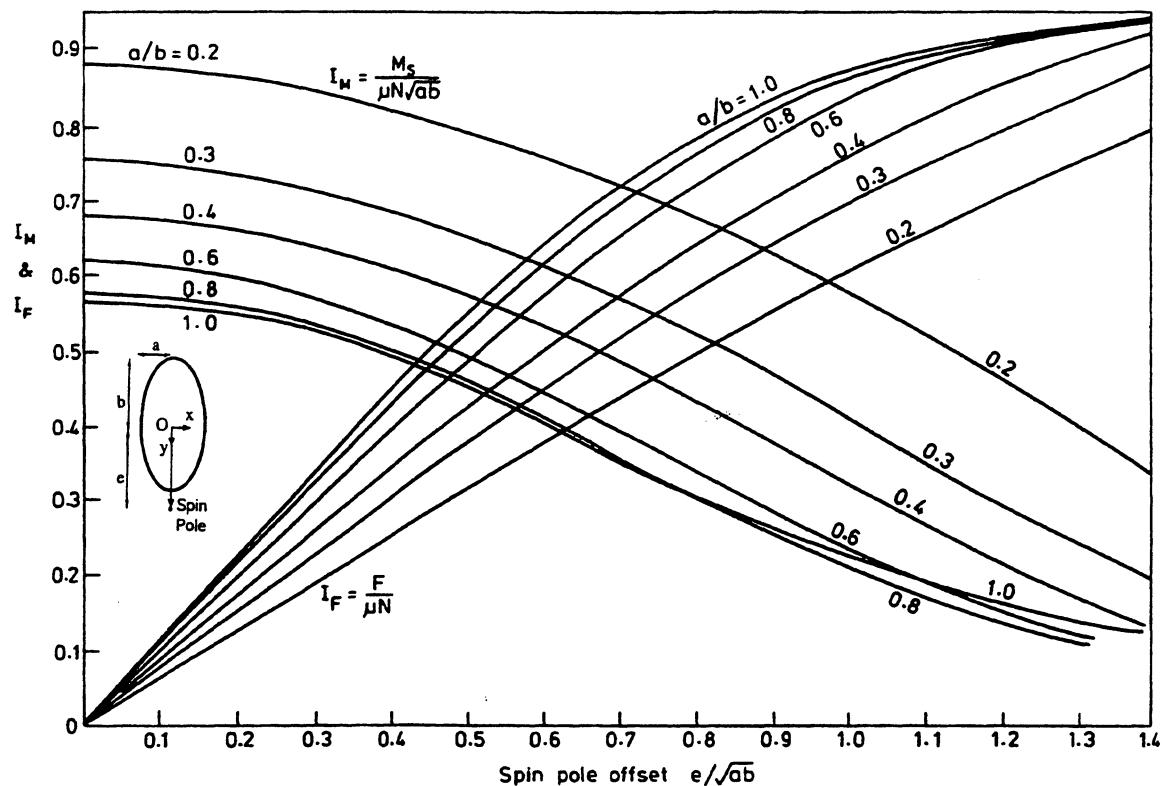
If the gap at zero load is  $h = \frac{1}{2}Ax^2 + \frac{1}{2}By^2$ , and  $0.2 < A/B < 5$

Ratio of semi-axes  $b/a \approx (A/B)^{2/3}$

To calculate the contact **area** or Hertz **stress** use the circular contact equations with  $R = (AB)^{-1/2}$  or better  $R_e = [AB(A+B)/2]^{-1/3}$ .

For **approach** use circular contact equation with  $R = (AB)^{-1/2}$  (**not**  $R_e$ )

### Hertzian contact frictional losses



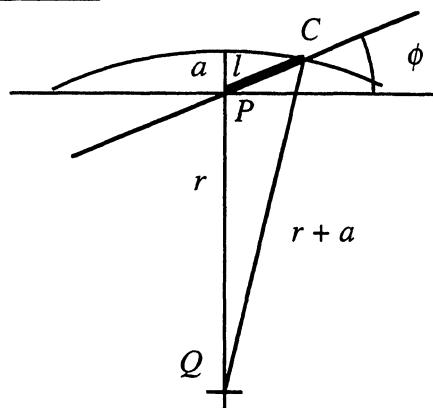
### INVOLUTE GEARING

#### Spur gears

pitch cylinder radii	$r$	with suffix 1 or 2
base cylinder radii	$r_b$	
addendum cylinder radii	$r_a$	
number of teeth	$N$	
addendum	$a = r_a - r$	
pressure angle	$\phi$	

circumferential pitch	$p = 2\pi r/N$
base pitch	$p_b = p \cos \phi$
module	$m = p/\pi = 2r/N$
ratio of contact	$r_c$
radius of curvature at pitch point	$\rho = r \sin \phi$

#### Path of contact



$$l = \left\{ r^2 \sin^2 \phi + a(2r + a) \right\}^{1/2} - r \sin \phi$$

For a standard  $20^\circ$  spur wheel with  $N$  teeth of module  $m$  this becomes

$$\frac{l}{m} = \left( 0.02924N^2 + N + 1 \right)^{1/2} - 0.1710N$$

Standard tooth forms

Addendum  $a = m$ , Dedendum =  $\frac{7}{6}m$ , pressure angle =  $20^\circ$ .

Modules:

1.0 – 4.0 mm in 0.25 mm steps  
7.0 – 16.0 mm in 1.0 mm steps  
24.0 – 45.0 mm in 3.0 mm steps

0.3 – 1.0 mm in 0.1 mm steps

4.0 – 7.0 mm in 0.5 mm steps  
16.0 – 24.0 mm in 2.0 mm steps  
45.0 – 75.0 mm in 5.0 mm steps

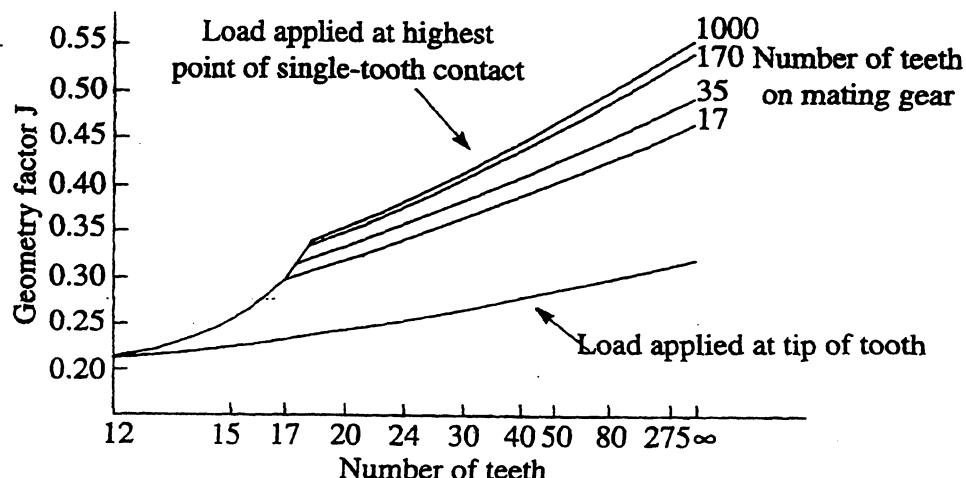
Friction in spur gears

$$\frac{\text{average friction loss}}{\text{power transmitted}} \approx \mu\pi \left\{ \frac{1}{N_1} + \frac{1}{N_2} \right\}$$

Tooth failure

Allowable bending stress  $\sigma_b$  according to AGMA guidelines given by  $\sigma_b = \frac{P'_T}{Jm}$

where  $P'_T$  is force per unit face-width acting tangentially to pitch circle and  $J$  given in the figure below for  $20^\circ$  spur gears. Typical values of  $\sigma_b$  shown in table.



Typical allowable tooth stresses (AGMA)

Material	Condition	Bending fatigue strength $\sigma_b$ (MPa)	Surface fatigue strength $\sigma_s$ (MPa)
Steel	Through hardened and tempered	170-390	590-1200
	Carburised and case hardened	380-480	1250-1550
Cast iron	As cast	69-90	450-590
Nodular iron	Quenched, annealed and tempered	150-300	500-800
Malleable iron	Pearlitic	70-145	500-650

## EPICYCLIC SPEED RULE

$$\omega_s = (1 + R)\omega_c - R\omega_a \quad \text{where } R = \frac{A}{S}$$

## ROLLING ELEMENT BEARINGS

### Fatigue life

$$L = a_1 a_{23} (C/P)^p \quad p = 3 \text{ for ball and } 10/3 \text{ for roller bearings}$$

Fatigue probability %	10	5	4	3	2	1
Life adjust factor $a_1$	1	0.62	0.53	0.44	0.33	0.21

### Minimum radial load $F_{rm}$

$$\text{For a ball bearing } F_{rm} = k_r \left( \frac{\nu n}{1000} \right)^{2/3} \left( \frac{d_m}{100} \right)^2$$

$$\text{For a roller bearing } F_{rm} = k_r \left( 6 + \frac{4n}{n_r} \right) \left( \frac{d_m}{100} \right)^2$$

$F_{rm}$  is the minimum radial load in N,  $d_m$  is the mean bearing diameter in mm,  $\nu$  is the kinematic viscosity in  $\text{mm}^2\text{s}^{-1}$ ,  $n$  the speed in rpm and  $n_r$  the limiting speed for oil lubrication.  $k_r$  is typically 25 for ball bearings and 150 for roller bearings.

### Bearing choice

The information on the following pages concerning minimum loads, viscosities and standard bearing sizes and ratings is extracted from the SKF General Bearing Catalogue and is copied with permission. It is SKF copyright and is not to be further reproduced.

Required viscosities and the effect of viscosity ratio on  $a_{23}$

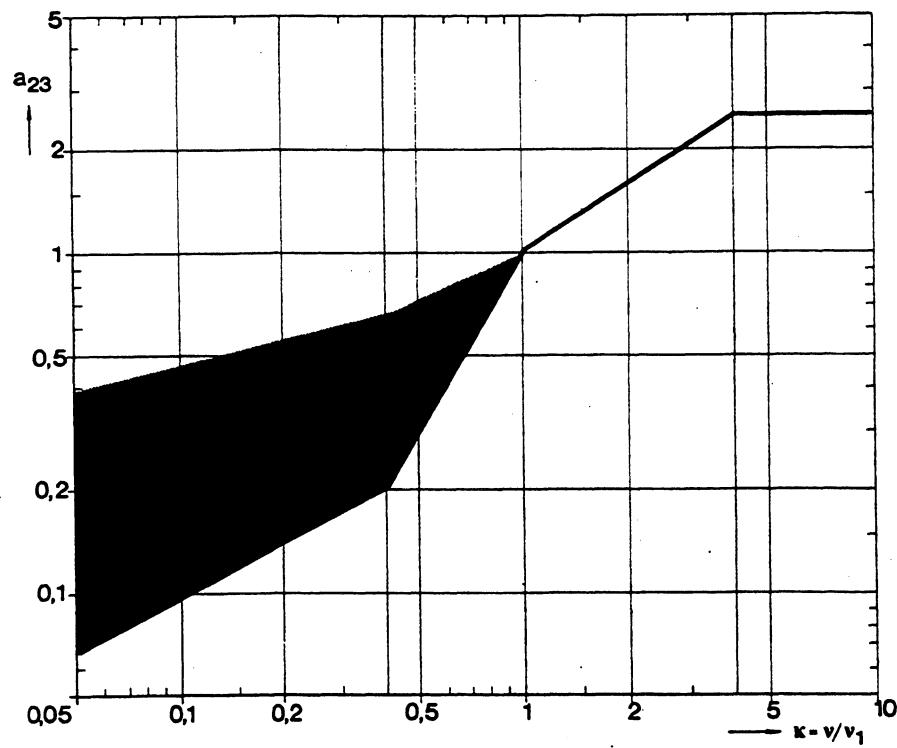
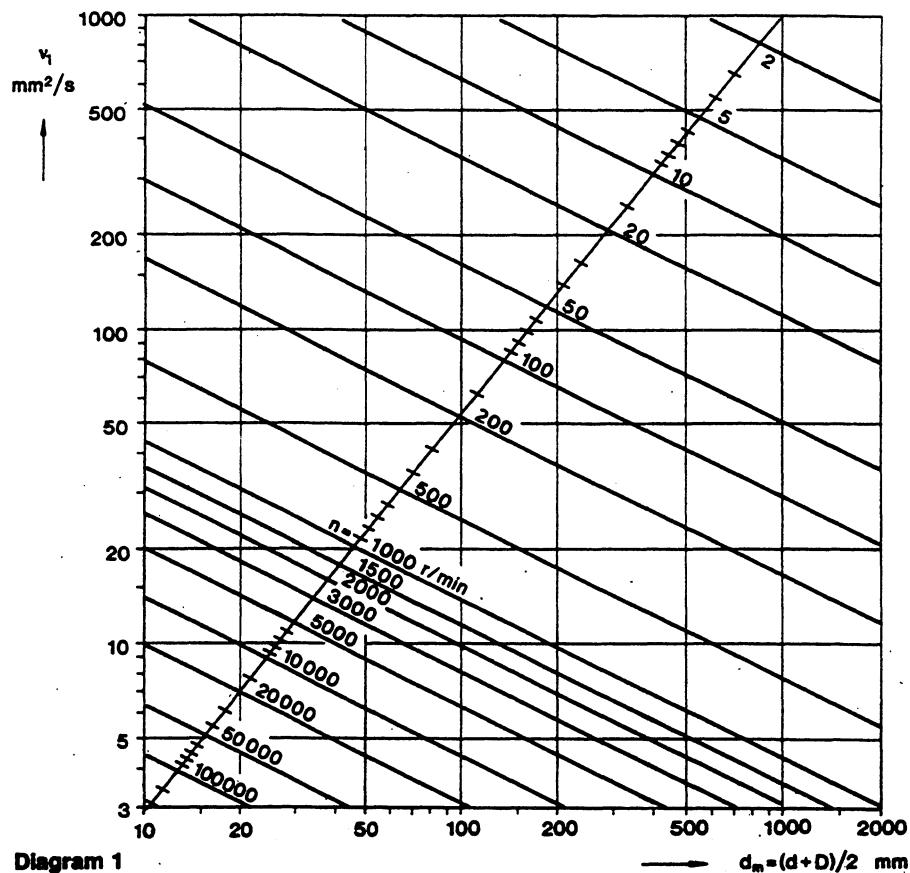
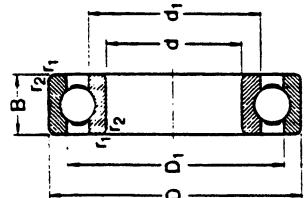


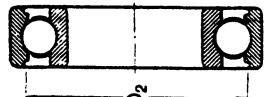
Diagram 3

**Deep groove ball bearings**  
single row  
d 35–55 mm

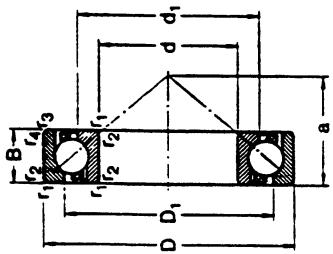
**Angular contact ball bearings**  
single row  
d 10–65 mm



With full outer  
ring shoulders

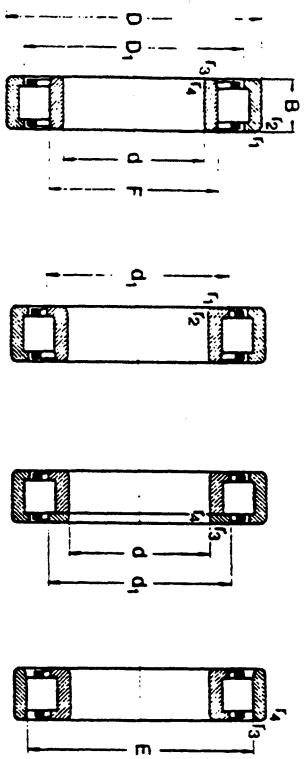


With recessed outer  
ring shoulders



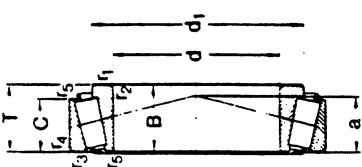
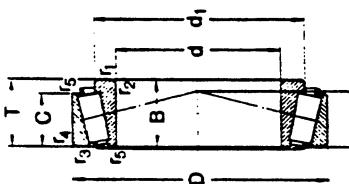
Principal dimensions						Basic load ratings			Fatigue load limit $P_u$			Speed ratings Lubrication oil			Mass			Designation		
d	D	B	C	$C_0$		d	D	B	C	$C_0$		N	r/min	N	r/min	N	r/min	N	r/min	
35	47	7	4750	3200	168	13 000	16 000	0 030	61607	10	30	9	7 020	3 350	140	19 000	28 000	0 030	7200 BE	
55	55	10	9 5560	6 200	280	11 000	14 000	0 080	61608	12	32	10	7 610	3 800	160	18 000	26 000	0 036	7201 BE	
62	62	9	12 400	8 150	375	10 000	13 000	0 11	61607	12	37	12	10 600	5 000	208	17 000	24 000	0 080	7301 BE	
62	62	14	15 900	10 200	440	10 000	13 000	0 16	6007	15	35	11	8 640	4 800	204	17 000	24 000	0 045	7202 BE	
72	72	17	25 500	15 300	655	9 000	11 000	0 29	6207	15	42	13	13 000	6 700	260	15 000	20 000	0 080	7302 BE	
80	80	21	33 200	19 000	815	8 500	10 000	0 46	6307	17	40	12	11 100	6 100	260	15 000	20 000	0 065	7203 BE	
100	100	25	56 300	31 000	1 290	7 000	8 500	0 95	6407	17	47	14	15 900	8 300	355	13 000	18 000	0 11	7303 BE	
40	52	7	4 940	3 450	186	11 000	14 000	0 034	61608	20	47	14	14 000	8 300	355	12 000	17 000	0 11	7204 BE	
62	62	12	13 800	9 300	425	10 000	13 000	0 12	61608	60	52	15	12 000	10 400	440	11 000	16 000	0 14	7304 BE	
68	68	9	13 900	9 150	440	9 500	12 000	0 13	61608	25	52	15	15 600	10 200	430	10 000	15 000	0 13	7205 BE	
68	68	15	16 800	11 600	490	9 500	12 000	0 19	6008	65	62	17	26 000	15 600	655	9 000	13 000	0 23	7305 BE	
80	80	18	30 700	19 000	800	8 500	10 000	0 37	6208	40	62	16	23 800	15 600	655	6 500	12 000	0 20	7206 BE	
90	90	23	41 000	24 000	1 020	7 500	8 000	0 63	6308	35	72	17	21 200	34 500	900	6 000	11 000	0 34	7306 BE	
110	110	27	63 700	36 500	1 530	6 000	7 500	1 25	6408	80	80	21	39 000	24 500	1 040	7 500	10 000	0 45	7307 BE	
45	59	7	6 050	4 300	228	9 500	12 000	0 040	61608	45	60	18	36 400	26 000	1 100	7 000	9 500	0 37	7208 BE	
68	68	12	10 100	6 700	285	9 000	11 000	0 14	61608	60	62	16	23 800	14 000	33 500	1 400	6 700	9 000	0 63	7308 BE
75	75	16	15 600	10 800	520	9 000	11 000	0 17	61609	75	72	19	34 500	21 200	900	6 000	11 000	0 34	7309 BE	
75	75	18	20 800	14 800	640	9 000	11 000	0 25	6009	80	72	17	30 700	20 800	850	6 000	11 000	0 42	7209 BE	
85	85	19	33 200	21 600	915	7 500	9 000	0 41	6209	90	80	21	39 000	24 500	1 040	7 500	10 000	0 45	7307 BE	
100	100	25	52 700	31 500	1 340	7 000	8 000	0 83	6309	100	80	20	39 000	30 500	1 280	6 000	9 000	0 47	7210 BE	
120	120	29	76 100	45 000	1 800	6 000	7 000	1 55	6409	110	90	27	74 100	51 000	2 200	6 300	7 000	1 10	7310 BE	
50	65	7	6 240	4 750	250	9 000	11 000	0 052	61610	55	65	19	37 700	28 000	1 200	6 700	9 000	0 42	7209 BE	
72	72	12	14 600	10 400	500	8 500	10 000	0 14	61610	65	100	25	60 500	41 500	1 750	6 000	9 000	0 85	7309 BE	
80	80	16	16 300	11 400	560	8 500	10 000	0 18	61610	70	90	20	39 000	30 500	1 280	6 000	9 000	0 47	7210 BE	
80	80	16	21 600	16 000	710	8 500	10 000	0 26	6210	80	90	20	39 000	30 500	1 280	6 000	9 000	0 47	7210 BE	
90	90	20	35 100	23 200	980	7 000	8 500	0 46	6210	90	90	27	74 100	51 000	2 200	6 300	7 000	1 10	7310 BE	
110	110	27	61 800	38 000	1 600	6 300	7 500	1 05	6310	100	100	21	48 800	38 000	1 650	6 000	9 000	1 10	7311 BE	
130	130	31	67 100	52 000	2 200	6 300	7 500	1 80	6410	120	120	29	65 200	60 000	2 550	4 800	6 300	1 40	7311 BE	
55	72	9	8 320	6 200	325	8 500	10 000	0 053	61611	60	110	22	57 200	45 500	1 850	5 000	6 700	0 80	7212 BE	
80	80	13	15 900	11 400	560	8 000	9 500	0 19	61611	65	130	31	95 800	69 600	3 000	4 500	6 000	1 75	7312 BE	
80	80	11	19 500	14 000	695	7 500	9 000	0 26	60011	90	110	23	68 300	64 000	2 200	4 500	6 000	1 00	7213 BE	
80	80	18	25 100	21 200	900	7 500	9 000	0 39	62111	100	130	31	95 800	69 600	3 000	4 500	6 000	2 30	7313 BE	
100	100	21	43 600	29 000	1 250	8 300	1 250	0 61	63111	120	120	29	67 200	60 000	2 300	4 300	6 000	2 15	7313 BE	
120	120	29	71 500	45 000	1 900	5 600	6 700	1 35	63111	140	140	33	99 500	98 000	10 000	6 000	6 000	2 00	7313 BE	

Cylindrical roller bearings  
single row  
 $d = 40\text{--}45 \text{ mm}$



Type NU				Type NJ				Type NUP				Type N			
Principal dimensions				Basic load ratings dynamic static				Fatigue load limit				Speed ratings lubrication oil			
d	D	B	C	$C_0$	$P_u$										
40	90	23	80 900	78 000	10 200	6 700	8 000	0,65	NU 308 EC						
(cont.)	90	23	80 900	78 000	10 200	6 700	8 000	0,67	NJ 308 EC						
	90	23	80 900	78 000	10 200	6 700	8 000	0,68	NUP 308 EC						
	90	23	80 900	78 000	10 200	6 700	8 000	0,64	N 308 EC						
90	33	112 000	120 000	120 000	15 300	6 300	7 500	0,94	NU 2308 EC						
	90	33	112 000	120 000	120 000	15 300	6 300	7 500	0,96	NJ 2308 EC					
	90	33	112 000	120 000	120 000	15 300	6 300	7 500	0,98	NUP 2308 EC					
110	27	96 800	90 000	11 600	6 000	7 000	1,30	NU 408							
	110	27	96 800	90 000	11 600	6 000	7 000	1,30	NJ 408						
	110	27	96 800	90 000	11 600	6 000	7 000	1,35	NUP 408						
45	75	16	44 600	52 000	6 300	9 000	11 000	0,26	NU 1009 EC						
	85	19	60 500	64 000	8 150	6 700	8 000	0,43	NU 209 EC						
	85	19	60 500	64 000	8 150	6 700	8 000	0,44	NJ 209 EC						
	85	19	60 500	64 000	8 150	6 700	8 000	0,45	NUP 209 EC						
	85	19	60 500	64 000	8 150	6 700	8 000	0,43	N 209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,54	NJ 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,55	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NU 2209 EC							
85	23	73 700	81 500	10 600	6 700	8 000	0,52	NJ 2209 EC							
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	NUP 2209 EC						
	85	23	73 700	81 500	10 600	6 700	8 000	0,52	N 2209 EC						
85	23	73 700	81 500	10 600	6 700	8 000	0,52</td								

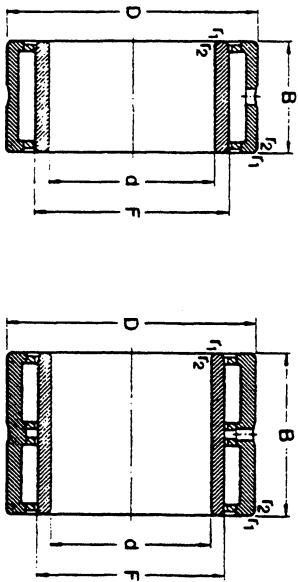
Taper roller bearings  
single row  
d 50–65 mm



Taper roller bearings  
single row  
d 35–50 mm

Principal dimensions d D T C Co	Basic load ratings dynamic static				Fatigue load limit $P_u$				Speed ratings Lubrication grease oil				Fatigue load limit $P_u$				Speed ratings Lubrication grease oil				Designation				Dimension Series to ISO 355				
	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	
35 (cont.)	80	22.75	72.100	73.500	8.500	5.000	6.700	0.52	30307	30307	X	-	-	50	110 (cont.)	28.25	125.000	140.000	17.000	3.600	4.800	1.25	30310	2FB	2FB	2FD	5FD	-	
	80	22.75	61.600	67.000	7.800	4.500	6.000	0.52	31307	32307	B	2FB	7FB	90	110	29.25	105.000	120.000	14.300	3.200	4.300	1.20	31310	2CE	3CE	3DB	5DC	-	
	80	32.75	95.200	106.000	12.200	4.600	6.300	0.73	32307	32307	B	2FE	5FE	110	110	42.25	172.000	216.000	24.500	3.200	4.300	1.80	32310 B	2FD	3DC	3DC	5ED	-	
	60	32.75	93.500	114.000	13.200	4.500	6.000	0.80	32307	32307	B	55	90	90	23	78.100	112.000	12.500	4.000	5.300	0.56	K-JLM 506849/K-JLM 506810	3CC	3CC	3CE	3CE	-		
40	68	19	52.800	71.000	7.800	5.300	7.000	0.27	32008	32008	X	90	90	23	80.900	116.000	13.200	4.000	5.300	0.55	32011 X	-	-	-	-	-			
	75	26	79.200	104.000	5.000	6.700	0.51	33108	33108	B	90	90	27	69.700	137.000	16.300	4.000	5.300	0.67	33011	2CE	3CE	3DB	5DC	-				
	80	19.75	61.600	68.000	7.650	4.800	6.300	0.42	30208	30208	B	95	30	110.000	156.000	18.000	3.800	6.000	0.86	33111	2CE	3CE	3DB	5DC	-				
	80	24.75	74.800	86.500	9.800	4.800	6.300	0.53	32208	32208	B	100	100	22.75	89.700	106.000	12.200	3.800	6.000	0.70	30211	2ED	3ED	3ED	5ED	-			
	80	32	105.000	132.000	15.300	4.300	5.600	0.77	33208	33208	B	100	100	26.75	106.000	128.000	16.000	3.800	6.000	0.83	32211	2ED	3ED	3ED	5ED	-			
	85	33	121.000	150.000	17.300	4.500	6.000	0.90	32208	32208	B	100	100	35	138.000	180.000	22.000	3.800	6.000	1.20	32211 B	3DE	3DE	3DE	3DE	-			
	90	25.25	85.800	95.000	11.000	4.500	6.000	0.72	30308	30308	B	110	39	179.000	232.000	3.400	3.400	4.500	1.70	T2ED 055	2ED	2ED	2ED	2ED	-				
	90	35.25	73.700	81.500	9.650	4.000	5.300	0.72	31308	31308	B	115	34	125.000	163.000	19.600	3.000	4.000	1.60	TFFC 055	2FB	2FB	2FB	2FB	-				
	90	35.25	117.000	140.000	16.300	4.000	5.300	1.00	32308	32308	B	120	31.5	121.000	137.000	17.000	3.200	4.300	1.55	31311	2FB	2FB	2FB	2FB	-				
	90	35.25	108.000	140.000	16.300	4.000	5.300	1.10	32308	32308	B	120	45.5	198.000	250.000	28.000	3.000	4.000	2.30	32311	2FD	2FD	2FD	2FD	-				
	45	75	58.300	80.000	4.800	6.300	0.34	32009	32009	X	30308	30308	30308	30308	120	45.5	190.000	250.000	30.000	2.800	3.800	2.50	32311 B	-	-	-	-	-	
	80	26	84.200	114.000	12.900	4.500	6.000	0.56	33109	33109	X	30308	30308	30308	30308	95	23	82.500	122.000	13.700	3.800	5.000	0.59	32012 X	4CC	4CC	4CC	4CC	-
	65	20.75	66.000	76.500	8.650	4.500	6.000	0.48	30209	30209	B	3DB	95	24	84.200	132.000	15.000	3.800	6.000	0.62	K-JLM 506848/K-JLM 506810	-	-	-	-	-			
	65	24.75	80.900	98.000	11.200	4.500	6.000	0.58	32209	32209	B	95	27	91.300	143.000	16.000	3.800	6.000	0.71	33012	3CE	3CE	3DB	5DC	-				
	65	24.75	79.200	93.000	11.300	4.500	6.000	0.60	32209	32209	B	95	100	27.75	99.000	117.000	19.600	3.800	6.000	0.82	33112	3ED	3ED	3ED	3ED	-			
	85	32	108.000	143.000	16.300	4.000	5.300	0.82	33209	33209	B	7FC	110	29.75	99.000	125.000	160.000	19.000	3.400	4.500	1.15	33212	3ED	3ED	3ED	3ED	-		
	95	29	89.700	112.000	12.900	3.600	4.800	0.92	31309	31309	B	2ED	110	30	125.000	160.000	19.000	3.400	4.500	1.15	33212	3ED	3ED	3ED	3ED	-			
	95	36	147.000	168.000	21.200	4.000	5.300	1.20	32209	32209	B	2FB	110	38	168.000	236.000	27.000	3.000	4.000	1.60	33212	3ED	3ED	3ED	3ED	-			
	100	27.25	108.000	120.000	14.600	4.000	5.300	0.97	30309	30309	B	115	39	168.000	250.000	27.500	3.000	4.000	1.85	T2ED 060	2ED	2ED	2ED	2ED	-				
	100	36.25	91.300	102.000	12.500	3.400	4.500	0.95	31309	31309	B	115	40	194.000	250.000	30.000	3.200	4.300	2.05	TFFC 060	2FB	2FB	2FB	2FB	-				
	100	36.25	140.000	170.000	20.400	3.600	4.800	1.35	32309	32309	B	120	37	154.000	204.000	24.500	2.800	3.800	2.05	TFFC 060	2FB	2FB	2FB	2FB	-				
	50	60	20	60.500	88.000	9.650	6.000	0.37	32010	32010	X	30308	30308	30308	30308	130	33.5	145.000	188.000	23.600	3.000	4.000	1.95	30312	4CC	4CC	4CC	4CC	-
	80	24	69.300	102.000	11.400	4.500	6.000	0.45	33010	33010	B	2CE	130	49.5	122.000	180.000	22.000	3.000	4.000	2.80	32312 B	2FD	2FD	2FD	2FD	-			
	82	21.5	72.100	100.000	11.000	4.500	6.000	0.43	K-JLM 104948/K-JLM 104910	K-JLM 104948/K-JLM 104910	-	3CE	130	49.5	120.000	180.000	22.000	3.000	4.000	2.80	32312 B	2FD	2FD	2FD	2FD	-			
	85	26	65.800	122.000	13.000	4.300	5.600	0.59	33110	33110	B	3DC	100	27	86.800	156.000	17.600	3.400	4.500	0.63	32013 X	4CC	4CC	4CC	4CC	-			
	90	21.75	62.500	100.000	11.600	4.300	5.600	0.61	32210	32210	B	5DC	100	27	86.800	156.000	17.600	3.400	4.500	0.78	K-JM 511048/K-JM 511010	2CE	2CE	2CE	2CE	-			
	90	24.75	62.500	104.000	10.500	4.800	5.200	0.95	32210	32210	B	5DC	110	28	123.000	183.000	21.200	3.000	4.000	1.05	K-JM 511048/K-JM 511010	3DE	3DE	3DE	3DE	-			
	90	28	106.000	140.000	16.300	4.000	5.300	0.75	K-JM 205149/K-JM 205110	K-JM 205149/K-JM 205110	-	30308	110	34	142.000	208.000	24.500	3.000	4.000	1.30	32113	3ED	3ED	3ED	3ED	-			
	90	32	114.000	160.000	18.300	4.000	5.300	0.90	32310	32310	B	120	32.75	151.000	193.000	23.200	3.000	4.000	1.15	32213	3ED	3ED	3ED	3ED	-				
	100	36	154.000	200.000	22.800	3.800	5.000	1.30	32310	32310	B	120	32	161.000	240.000	27.500	3.000	4.000	1.95	T2ED 050	2ED	2ED	2ED	2ED	-				
	105	32	108.000	137.000	16.000	3.200	4.300	1.20	32310	32310	B	120	32	161.000	240.000	27.500	3.000	4.000	1.95	TFFC 050	2ED	2ED	2ED	2ED	-				

**Needle roller bearings with flanges  
with inner ring  
d 40–65 mm**



Series NKI(S), NA 49

Series NA 69

Principal dimensions d	D	B	C	C <sub>0</sub>	P <sub>u</sub>	Basic load ratings		Speed ratings lubrication grease oil	Mass	Designation	
						dynamic	static				
40	55	20	27 500	57 000	7 200	6 300	9 000	0,14	NKI 40/20	NKI 40/20	
	55	30	40 200	93 000	12 000	6 300	9 000	0,22	NA 4908	NA 4908	
	62	22	42 800	71 000	9 150	5 600	8 000	0,23	NA 6908	NA 6908	
	62	42	67 100	125 000	16 000	5 600	8 000	0,43	NKIS 40	NKIS 40	
	65	22	42 800	72 000	6 150	5 600	8 000	0,28	NKI 42/20	NKI 42/20	
42	57	20	29 200	61 000	7 650	6 000	8 500	0,15	NA 4910	NA 4910	
	57	30	41 800	98 000	12 800	6 000	8 500	0,22	NKIS 42/30	NKIS 42/30	
46	62	25	38 000	78 000	10 000	5 600	8 000	0,23	NKI 45/25	NKI 45/25	
	62	35	49 500	110 000	14 300	5 600	8 000	0,32	NA 4909	NA 4909	
	68	22	45 700	78 000	10 000	5 600	7 500	0,27	NA 6909	NA 6909	
	68	40	70 400	137 000	17 300	5 300	7 500	0,50	NKIS 45	NKIS 45	
	72	22	44 600	78 000	10 000	5 000	7 000	0,34			
50	68	25	40 200	88 000	11 200	5 300	7 500	0,27	NKI 50/25	NKI 50/25	
	68	35	52 300	122 000	16 000	5 300	7 500	0,38	NKI 50/35	NKI 50/35	
	72	22	47 300	85 000	11 000	5 000	7 000	0,27	NA 4910	NA 4910	
	72	40	73 700	150 000	19 000	5 000	7 000	0,52	NA 6910	NA 6910	
	80	28	62 700	154 000	13 700	4 500	6 300	0,52	NKIS 50	NKIS 50	
	82	72	35	41 800	96 500	12 200	4 600	6 700	0,27	NKI 55/25	NKI 55/25
	82	72	35	55 000	134 000	17 600	4 600	6 700	0,38	NKI 55/35	NKI 55/35
	80	25	57 200	106 000	13 700	4 500	6 700	0,40	NA 4911	NA 4911	
	80	45	89 700	190 000	24 000	4 500	6 700	0,78	NA 6911	NA 6911	
	85	28	66 000	114 000	15 000	4 300	6 000	0,56	NKIS 55	NKIS 55	
65	90	25	44 000	95 000	12 000	4 300	6 000	0,40	NKI 60/25	NKI 60/25	
	82	82	60 500	146 000	18 000	4 300	6 000	0,55	NA 6912	NA 6912	
	85	25	60 500	204 000	14 600	4 300	6 000	0,43	NA 6912	NA 6912	
	85	45	93 500	28 000	14 600	4 300	6 000	0,81	NKIS 60	NKIS 60	
	80	28	68 200	120 000	15 600	4 000	5 600	0,56			
80	90	25	61 600	120 000	15 300	4 000	5 600	0,46	NA 4913	NA 4913	
	90	52	80 000	163 000	13 700	4 000	5 600	0,47	NKI 65/25	NKI 65/25	
	90	80	73 700	21 600	4 000	5 600	0,88	NKI 65/35	NKI 65/35		
	95	45	95 200	212 000	27 000	4 000	5 600	0,83	NA 6913	NA 6913	
	95	80	132 000	17 000	3 800	5 300	0,64	NKIS 65	NKIS 65		