

# PART IIA 2005

## 3C5 Dynamics

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### Answers

1. (b)  $\underline{Q}_p^{(e)} = \dot{\underline{h}}_p$

2. (a) (i) 
$$\begin{bmatrix} 0.89 & -0.48 & 0 \\ -0.48 & 0.61 & 0 \\ 0 & 0 & 1.5 \end{bmatrix} ma^2$$

(ii)  $0.25ma^2, 1.25ma^2, 1.5ma^2$ , directions aligned with particles, perpendicular to line of particles and perpendicular to plate respectively.

(b) AAC =  $13ma^2/6, 13ma^2/6, 2ma^2/3$ , directions of A are anywhere perpendicular to the line of particles, and C is aligned with the line of particles.

3. (a) (i)  $mg/\cos\beta$

(b) steady-state  $\beta$  close to  $\pi/2$

(c)  $2g/a\omega$  for fast spin

4. (a)  $T = m\dot{x}^2 + m\dot{a}\dot{\theta}\cos\theta + \frac{2}{3}ma^2\dot{\theta}^2 \quad V = \frac{1}{2}k\theta^2 + mga(\cos\theta - 1)$

(b)  $M = \begin{bmatrix} 2m & ma \\ ma & \frac{4}{3}ma^2 \end{bmatrix} \quad K = \begin{bmatrix} 0 & 0 \\ 0 & k - mga \end{bmatrix}$

(c)  $\omega = 0$ , rigid body translation,  $\{x, \theta\} = \{1, 0\}$

$$\omega = \frac{6}{5ma^2}(k - mga), \text{ modeshape } \{x, \theta\} = \{a, -2\}$$

(d)  $k > mga$

5. (a)  $Q_x = f \quad Q_\theta = 0$

(b)  $T = m\dot{x}^2 + m\dot{a}\dot{\theta}\cos\alpha + \frac{3}{4}ma^2\dot{\theta}^2 \quad V = -mga\theta\sin\alpha$

(c)  $2m\ddot{x} + ma\ddot{\theta}\cos\alpha = f \quad \ddot{x}\cos\alpha + \frac{3}{2}a\ddot{\theta} = g\sin\alpha$

(d) (i)  $2mg\tan\alpha \quad$  (ii)  $\ddot{x} = \frac{g\sin\alpha\cos\alpha}{\cos^2\alpha - 3}$