

ENGINEERING TRIPOS PART IIA

Tuesday 1 May 2007 2.30 to 4

Module 3C3

MACHINE DESIGN – TRIBOLOGY

*Answer not more than **three** questions.*

All questions carry the same number of marks.

*The **approximate** percentage of marks allocated to each part of a question is indicated in the right margin.*

Attachment:

Special Data sheet (10 pages).

STATIONERY REQUIREMENTS

Single-sided script paper

SPECIAL REQUIREMENTS

Engineering Data Book

CUED approved calculator allowed

You may not start to read the questions printed on the subsequent pages of this question paper until instructed that you may do so by the Invigilator

1 (a) The gap between two wide, smooth, flat plates with separation h is supplied with a lubricant of Newtonian viscosity η . The lower plate moves with velocity U and the upper plate is stationary. Briefly outline the argument which leads to the expression

$$q = \frac{Uh}{2} - \frac{h^3}{12\eta} \frac{dp}{dx}$$

in which q is the volumetric flow rate of the fluid per unit width and $\frac{dp}{dx}$ is the pressure gradient within the fluid in the direction of motion. [25%]

(b) Figure 1 shows, not to scale, a section through a proposed fluid film bearing which makes use of two parallel regions in which the film thickness is h : the first of these is of length a and the second of length c and they are separated by a pocket of much greater depth h_p which has length b . The bearing is supplied with fluid at an ambient pressure p_a so that $p = p_a$ when $x = 0$ and $x = a + b + c$.

(i) Explain why the pressure gradient in each of the sections in which the film thickness is h must be the same. [10%]

(ii) Sketch the way in which the absolute pressure p in the fluid varies with co-ordinate x which is measured from the bearing entrance; note that when $x = a$ it is possible that $p < p_a$. [10%]

(iii) If the conditions are such that the fluid just cavitates at the point $x = a$ and the cavitation pressure can be taken as zero, show that the dimension b must satisfy the relation

$$\frac{6\eta U}{p_a} (h_p - h) = \left(1 + \frac{c}{a}\right) \frac{h_p^3}{b} + \frac{h^3}{a}. \quad [30\%]$$

(iv) Assuming that this is the case, confirm that the load carrying capacity per unit width of the bearing is given by the expression

$$\frac{p_a c}{2} \left(\frac{b+c}{a} - \frac{a+b}{c} \right).$$

Comment on the practicality of this arrangement. [25%]

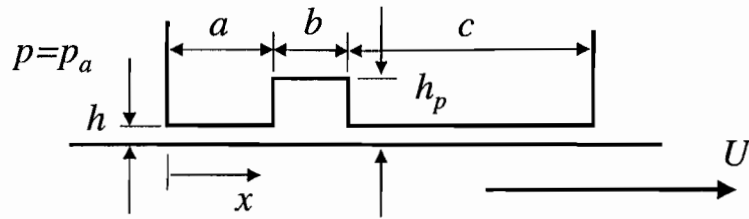


Fig. 1

2 (a) Outline the Kapitza and Ertel-Grubin models used to predict respectively the film thickness in the lubrication of rigid cylinders and conditions of elasto-hydrodynamic lubrication (EHL). Explain why the predicted dependence of film thickness on load for EHL is much less than for the lubrication of rigid contacts. [40%]

(b) It is required to increase by a factor of five the torque through a precision spur gear pair which has demonstrated a satisfactory lifetime. The existing gears have a module of 5 mm and tooth numbers of 17 and 51. Two options are to be considered while retaining a speed ratio of three and using the same materials as in the existing set.

(i) It is proposed to scale all the dimensions of both gears by a factor α while retaining the existing tooth numbers. Assuming that failure is due to contact stress find an appropriate value of α . [30%]

(ii) Alternatively, it is proposed to retain the module and gear face width but increase the number of teeth on both gears. Assuming that the failure is now due to tooth bending propose new tooth numbers. [30%]

3 (a) Explain briefly what is meant by the terms *long* and *short* when applied to hydrodynamically lubricated journal bearings. [10%]

(b) The short bearing approximation results in the following relationship between the steady radial load W on the bearing, its radius R and length L , the radial clearance c , the eccentricity ratio ε , the viscosity of the lubricant η and the speed of rotation ω ,

$$W = \frac{\pi}{4} \frac{\eta \omega \varepsilon R L^3}{c^2 (1 - \varepsilon^2)^2} \left\{ \left(\frac{16}{\pi^2} - 1 \right) \varepsilon^2 + 1 \right\}^{1/2} .$$

Show that when the bearing is heavily loaded the minimum film thickness h_{\min} is given by the approximate expression

$$h_{\min} \approx \frac{1}{2} \sqrt{\frac{\eta \omega R L^3}{W}} .$$

You may find it useful to make the substitution $1 - \varepsilon = \delta$ and allow δ to become small. [40%]

(c) The frictional power loss P_{μ} in such a bearing is given by the expression

$$P_{\mu} = \frac{\pi \eta \omega^2 L R^3 (2 + \varepsilon)}{c (1 + \varepsilon) \sqrt{1 - \varepsilon^2}} .$$

Confirm that when the bearing is lightly loaded this expression reduces to the Petrov solution $P_{\mu} = 2\pi\eta\omega^2LR^3/c$. [10%]

(d) When the bearing is again heavily loaded obtain an approximate expression for the frictional power loss as a function of η , ω , L , R , W and c . In a particular case $R = 20$ mm, $L = 20$ mm, $\eta = 0.03$ Pas, $\omega = 60$ s⁻¹, $W = 7.2$ kN and $c/R = 0.001$. By what factor will an estimate of the frictional power loss based on Petrov differ from that evaluated from the derived expression? Comment on the possible reasons for this difference. [40%]

4 (a) Describe briefly the idealisations that are implicit in the Hertz analysis of point contacts. [15%]

(b) A tungsten carbide sphere of radius 5 mm is in contact with two metal plates of different alloys as shown in Fig. 2. The upper plate is steel and has a Young's modulus of 210 GPa and a yield stress in shear of 400 MPa. The lower tungsten alloy plate has Young's modulus of 345 GPa and a yield stress which is known to be at least 40% above that of the steel. The elastic modulus of tungsten carbide is 700 GPa and plastic yield of the carbide sphere need not be taken into account. The Poisson's ratio for all three materials can be taken as 0.3.

(i) A vertical load P is applied to the plates so that they move towards each other through a distance δ equal to 0.001 mm. If it is assumed that all the deformations are elastic, what is the value of the ratio of the contact areas at the two interfaces? Show that the magnitude of the force required is just over 7 N and confirm that elastic behaviour is a reasonable assumption. [30%]

(ii) The two plates are now gradually brought closer together. At which interface will elastic conditions first be exceeded and at what values of δ and P will this occur? Sketch a plot illustrating the way in which the applied load P varies with δ over the regime of elastic contact. [30%]

(iii) The gap between the plates is now reduced still further until δ is just over 0.15 mm. On separation the indentation in the steel plate is observed to be of radius 1.0 mm and that in the tungsten alloy plate 0.75 mm. Estimate the yield stress in shear of the tungsten alloy and the final load that was applied in the test. [25%]

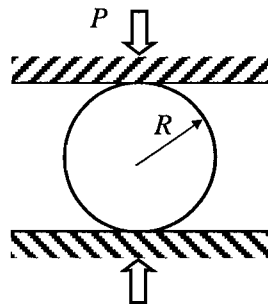


Fig. 2

ENGINEERING TRIPOS Part IIA

Modules 3C3 and 3C4 Data Sheet

HYDRODYNAMIC LUBRICATION

Viscosity: temperature and pressure effects

$$\text{Vogel formula } \eta = \eta_0 \exp\left\{\frac{b}{T + T_c}\right\}$$

$$\text{Barus equation } \eta = \eta_0 \exp\{\alpha p\}$$

$$\text{Roelands equation } \eta = \eta_0 \exp\left\{9.67 + \ln \eta_0 \left[\left(1 + \frac{p}{p_0^*}\right)^\beta - 1 \right]\right\}$$

Viscous pressure flow

Rate of flow q_x per unit width of fluid of viscosity η down a channel of height h due to

$$\text{pressure gradient, } q_x = -\frac{h^3}{12\eta} \frac{dp}{dx}$$

Reynolds' Equation for a steady configuration

$$\text{1-D flow: } \frac{dp}{dx} = 12\eta\bar{U} \left\{ \frac{h - h^*}{h^3} \right\}$$

\bar{U} is the entraining velocity so that $|\bar{U}h^*|$ is flow per unit width through the contact.

$$\text{2-D flow: } \frac{\partial}{\partial x} \left\{ \frac{h^3}{\eta} \frac{\partial p}{\partial x} \right\} + \frac{\partial}{\partial y} \left\{ \frac{h^3}{\eta} \frac{\partial p}{\partial y} \right\} = 12\bar{U} \frac{\partial h}{\partial x}$$

Hydrodynamic lubrication of discs

$\frac{h}{R} = C \frac{\eta\bar{U}}{W'}$ where R is the reduced or effective radius and W' the load per unit length

$C_{\min} = 4.00$ for half Sommerfeld boundary conditions

$C_{\min} = 4.89$ for half Reynolds' boundary conditions

ELASTIC CONTACT STRESS FORMULAE

Suffixes 1, 2 refer to the two bodies in contact.

Effective curvature $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$

where R_1, R_2 are the radii of curvature of the two bodies (convex positive).

Contact modulus $\frac{1}{E^*} = \frac{1-\nu_1^2}{E_1} + \frac{1-\nu_2^2}{E_2}$

where E_1, E_2 and ν_1, ν_2 are Young's moduli and Poisson's ratios.

	<u>Line contact</u>	<u>Circular contact</u>
	(width $2b$; load W' per unit length)	(diameter $2a$; load W)
Semi contact width or contact radius	$b = 2 \left\{ \frac{W'R}{\pi E^*} \right\}^{1/2}$	$a = \left\{ \frac{3WR}{4E^*} \right\}^{1/3}$
Maximum contact pressure ("Hertz stress")	$p_0 = \left\{ \frac{W'E^*}{\pi R} \right\}^{1/2}$	$p_0 = \frac{1}{\pi} \left\{ \frac{6WE^{*2}}{R^2} \right\}^{1/3}$
Approach of centres	$\delta = \frac{2W'}{\pi} \left[\frac{1-\nu_1^2}{E_1} \left\{ \ln \left(\frac{4R_1}{b} \right) - \frac{1}{2} \right\} + \frac{1-\nu_2^2}{E_2} \left\{ \ln \left(\frac{4R_2}{b} \right) - \frac{1}{2} \right\} \right]$	$\delta = \frac{a^2}{R} = \frac{1}{2} \left\{ \frac{9}{2} \frac{W^2}{E^{*2} R} \right\}^{1/3}$
Mean contact pressure	$\bar{p} = \frac{W'}{2b} = \frac{\pi}{4} p_0$	$\bar{p} = \frac{W}{\pi a^2} = \frac{2}{3} p_0$
Maximum shear stress	$\tau_{\max} = 0.300 p_0$ at $(x = 0, z = 0.79b)$	$\tau_{\max} = 0.310 p_0$ at $(r = 0, z = 0.48a)$ for $\nu = 0.3$
Maximum tensile stress	zero	$\frac{1}{3}(1-2\nu)p_0$ at $(r = a, z = 0)$

Mildly elliptical contacts

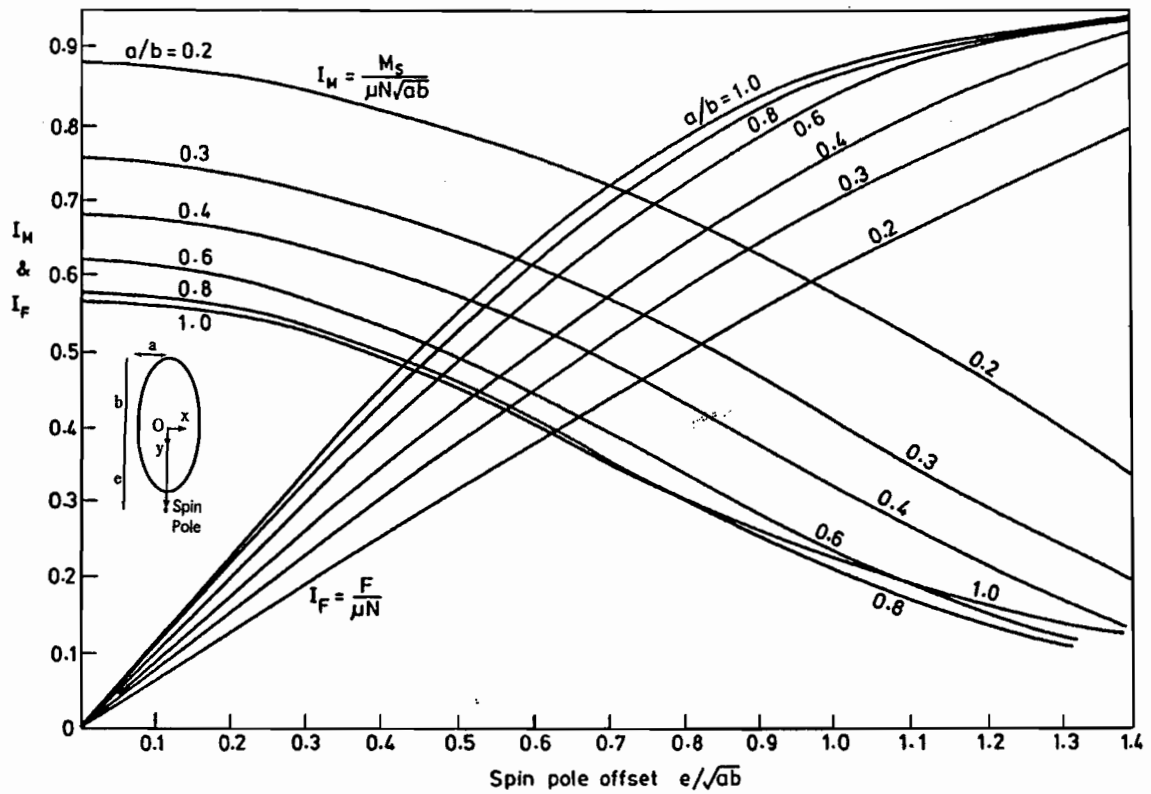
If the gap at zero load is $h = \frac{1}{2}Ax^2 + \frac{1}{2}By^2$, and $0.2 < A/B < 5$

Ratio of semi-axes $b/a \cong (A/B)^{2/3}$

To calculate the contact **area** or Hertz **stress** use the circular contact equations with $R = (AB)^{-1/2}$ or better $R_e = [AB(A+B)/2]^{-1/3}$.

For **approach** use circular contact equation with $R = (AB)^{-1/2}$ (not R_e)

Hertzian contact frictional losses



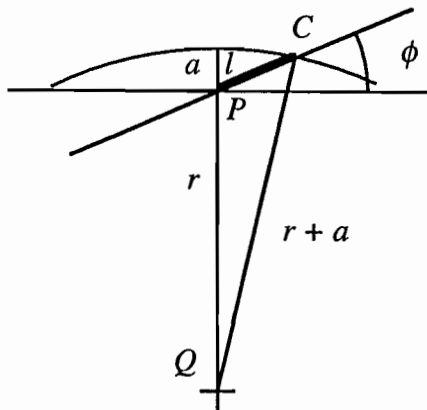
INVOLUTE GEARING

Spur gears

pitch cylinder radii	r	} with suffix 1 or 2
base cylinder radii	r_b	
addendum cylinder radii	r_a	
number of teeth	N	
addendum	$a = r_a - r$	
pressure angle	ϕ	

circumferential pitch	$p = 2\pi r/N$
base pitch	$p_b = p \cos \phi$
module	$m = p/\pi = 2r/N$
ratio of contact	r_c
radius of curvature at pitch point	$\rho = r \sin \phi$

Path of contact



$$l = \left\{ r^2 \sin^2 \phi + a(2r + a) \right\}^{1/2} - r \sin \phi$$

For a standard 20° spur wheel with N teeth of module m this becomes

$$\frac{l}{m} = \left(0.02924N^2 + N + 1 \right)^{1/2} - 0.1710N$$

Standard tooth forms

Addendum $a = m$, Dedendum $= \frac{7}{6}m$, pressure angle $= 20^\circ$.

Modules:	0.3 – 1.0 mm in 0.1 mm steps
1.0 – 4.0 mm in 0.25 mm steps	4.0 – 7.0 mm in 0.5 mm steps
7.0 – 16.0 mm in 1.0 mm steps	16.0 – 24.0 mm in 2.0 mm steps
24.0 – 45.0 mm in 3.0 mm steps	45.0 – 75.0 mm in 5.0 mm steps

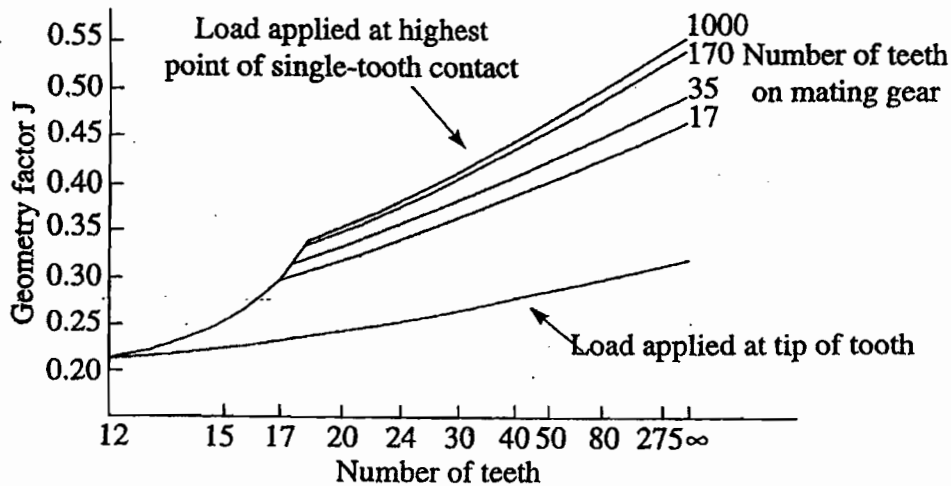
Friction in spur gears

$$\frac{\text{average friction loss}}{\text{power transmitted}} \approx \mu\pi \left\{ \frac{1}{N_1} + \frac{1}{N_2} \right\}$$

Tooth failure

Allowable bending stress σ_b according to AGMA guidelines given by $\sigma_b = \frac{P_T'}{Jm}$

where P_T' is force per unit face-width acting tangentially to pitch circle and J given in the figure below for 20° spur gears. Typical values of σ_b shown in table.



Typical allowable tooth stresses (AGMA)

Material	Condition	Bending fatigue strength σ_b (MPa)	Surface fatigue strength σ_s (MPa)
Steel	Through hardened and tempered	170-390	590-1200
	Carburised and case hardened	380-480	1250-1550
Cast iron	As cast	69-90	450-590
Nodular iron	Quenched, annealed and tempered	150-300	500-800
Malleable iron	Pearlitic	70-145	500-650

EPICYCLIC SPEED RULE

$$\omega_s = (1 + R)\omega_c - R\omega_a \quad \text{where } R = \frac{A}{S}$$

ROLLING ELEMENT BEARINGS

Fatigue life

$$L = a_1 a_2 a_3 (C/P)^p \quad p = 3 \text{ for ball and } 10/3 \text{ for roller bearings}$$

Fatigue probability %	10	5	4	3	2	1
Life adjust factor a_1	1	0.62	0.53	0.44	0.33	0.21

Minimum radial load F_{rm}

$$\text{For a ball bearing } F_{rm} = k_r \left(\frac{vn}{1000} \right)^{2/3} \left(\frac{d_m}{100} \right)^2$$

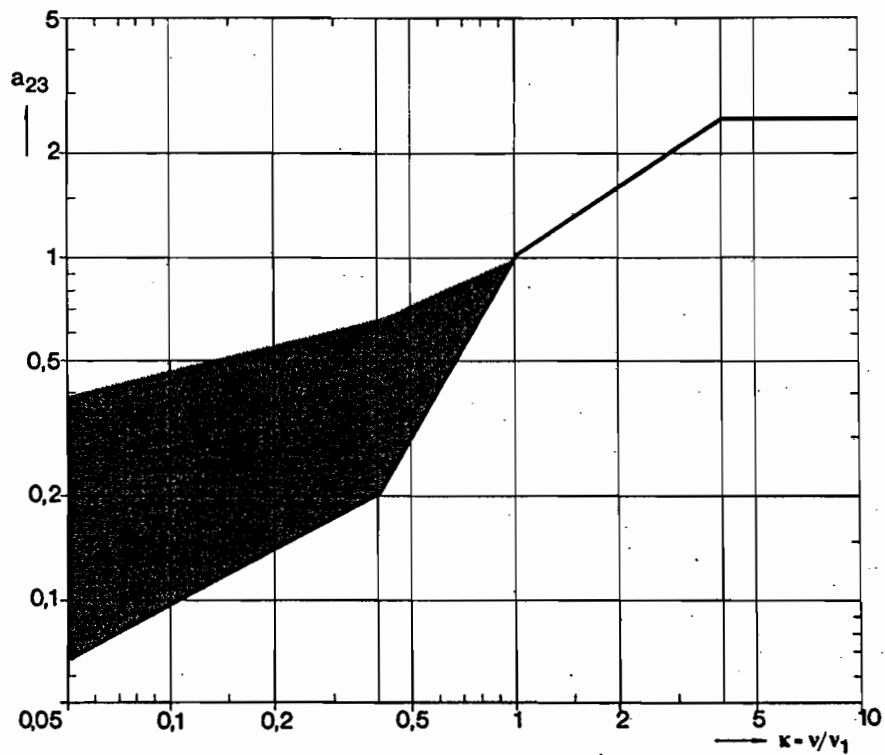
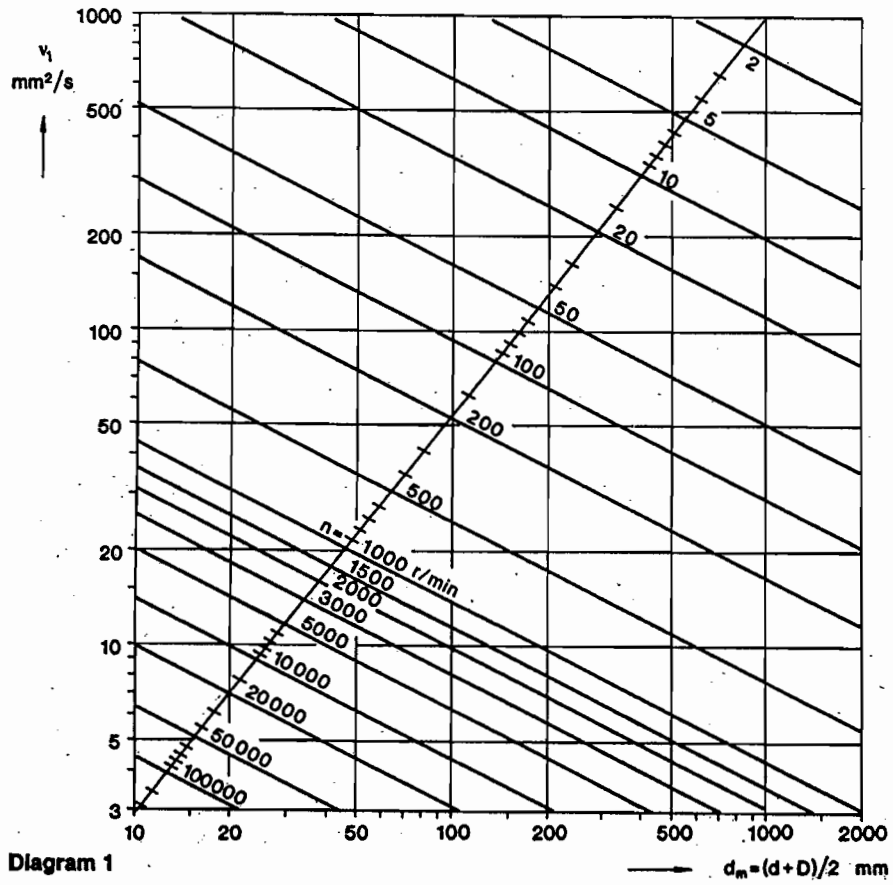
$$\text{For a roller bearing } F_{rm} = k_r \left(6 + \frac{4n}{n_r} \right) \left(\frac{d_m}{100} \right)^2$$

F_{rm} is the minimum radial load in N, d_m is the mean bearing diameter in mm, v is the kinematic viscosity in mm^2s^{-1} , n the speed in rpm and n_r the limiting speed for oil lubrication. k_r is typically 25 for ball bearings and 150 for roller bearings.

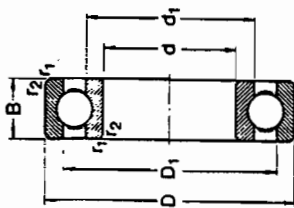
Bearing choice

The information on the following pages concerning minimum loads, viscosities and standard bearing sizes and ratings is extracted from the SKF General Bearing Catalogue and is copied with permission. It is SKF copyright and is not to be further reproduced.

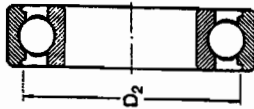
Required viscosities and the effect of viscosity ratio on a_{23}



Deep groove ball bearings
single row
d 35-55 mm



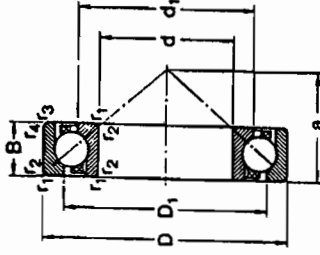
With full outer ring shoulders



With recessed outer ring shoulders

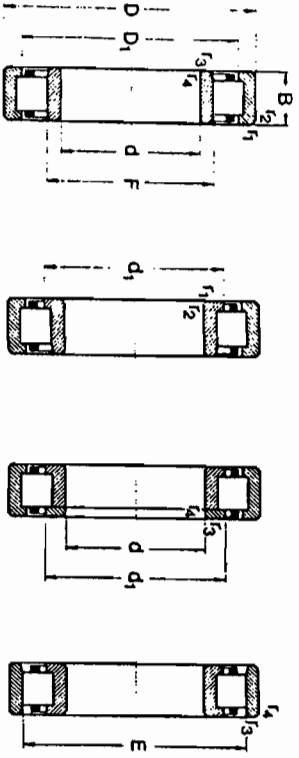
Principal dimensions	Basic load ratings			Fatigue load limit P_u	Speed ratings Lubrication grease oil	Mass	Designation		
	d	D	B					C	C_0
35	47	7	4 750	3 200	166	13 000	16 000	0,030	61807
	55	10	9 560	6 200	280	11 000	14 000	0,060	61907
	62	9	12 400	8 150	375	10 000	13 000	0,11	61607
	62	14	15 900	10 200	440	10 000	13 000	0,16	6007
	72	17	25 500	15 300	655	9 000	11 000	0,29	6207
	80	21	33 200	19 000	815	8 500	10 000	0,46	6307
	100	25	55 300	31 000	1 290	7 000	8 500	0,95	6407
40	52	7	4 940	3 450	186	11 000	14 000	0,034	61808
	62	12	13 800	9 300	425	10 000	13 000	0,12	61908
	68	9	13 300	9 150	440	9 500	12 000	0,13	61008
	68	15	16 800	11 600	490	9 500	12 000	0,19	6008
	80	18	30 700	19 000	800	8 500	10 000	0,37	6208
	90	23	41 000	24 000	1 020	7 500	9 000	0,63	6308
	110	27	63 700	36 500	1 530	6 700	8 000	1,25	6408
45	58	7	6 050	4 300	228	9 500	12 000	0,040	61809
	68	12	10 100	6 700	285	9 000	11 000	0,14	61909
	75	10	15 600	10 800	520	9 000	11 000	0,17	61609
	75	16	20 800	14 600	640	9 000	11 000	0,25	6009
	85	19	33 200	21 600	915	7 500	9 000	0,41	6209
	100	25	52 700	31 500	1 340	6 700	8 000	0,83	6309
	120	29	76 100	45 000	1 900	6 000	7 000	1,55	6409
50	65	7	6 240	4 750	250	9 000	11 000	0,052	61810
	72	12	14 600	10 400	500	8 500	10 000	0,14	61910
	80	10	16 300	11 400	560	8 500	10 000	0,18	61610
	80	16	21 600	16 000	710	8 500	10 000	0,26	6010
	90	20	35 100	23 200	980	7 000	8 500	0,46	6210
	110	27	61 800	38 000	1 600	6 300	7 500	1,05	6310
	130	31	87 100	52 000	2 200	5 300	6 300	1,90	6410
55	72	9	8 320	6 200	325	8 500	10 000	0,063	61811
	80	13	15 900	11 400	560	8 500	9 500	0,19	61911
	90	11	19 500	14 000	695	7 500	9 000	0,26	6011
	90	18	28 100	21 200	900	7 500	9 000	0,39	6111
	100	21	43 600	29 000	1 250	6 300	7 500	0,61	6211
	120	29	71 500	45 000	1 900	5 600	6 700	1,35	6311
	140	33	99 500	62 000	2 600	5 000	6 000	2,30	6411

Angular contact ball bearings
single row
d 10-65 mm



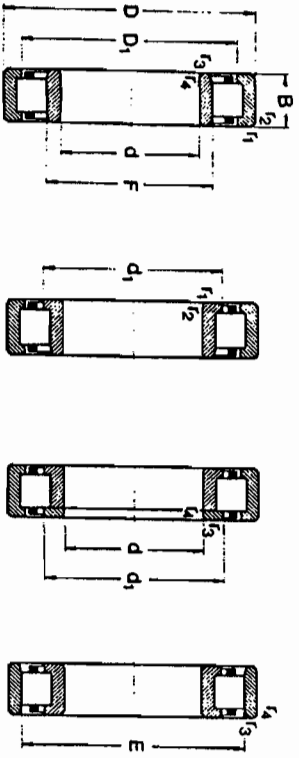
Principal dimensions	Basic load ratings			Fatigue load limit P_u	Speed ratings Lubrication grease oil	Mass	Designation		
	d	D	B					C	C_0
10	30	9	7 020	3 350	140	19 000	28 000	0,030	7200 BE
12	32	10	7 610	3 800	160	18 000	26 000	0,036	7201 BE
	37	12	10 600	5 000	208	17 000	24 000	0,060	7301 BE
15	35	11	8 940	4 800	204	17 000	24 000	0,045	7202 BE
	42	13	13 000	6 700	280	15 000	20 000	0,080	7302 BE
17	40	12	11 100	6 100	260	15 000	20 000	0,065	7203 BE
	47	14	15 900	8 300	355	13 000	18 000	0,11	7303 BE
20	47	14	14 000	8 300	355	12 000	17 000	0,11	7204 BE
	52	15	19 000	10 400	440	11 000	16 000	0,14	7304 BE
25	52	15	15 600	10 200	430	10 000	15 000	0,13	7205 BE
	62	17	26 000	15 600	655	9 000	13 000	0,23	7305 BE
30	62	16	23 800	15 600	655	8 500	12 000	0,20	7206 BE
	72	19	34 500	21 200	900	8 000	11 000	0,34	7306 BE
35	72	17	30 700	20 800	880	8 000	11 000	0,28	7207 BE
	80	21	39 000	24 500	1 040	7 500	10 000	0,45	7307 BE
40	80	18	36 400	26 000	1 100	7 000	9 500	0,37	7208 BE
	80	23	49 400	33 500	1 400	6 700	9 000	0,63	7308 BE
45	85	19	37 700	28 000	1 200	6 700	9 000	0,42	7208 BE
	100	25	60 500	41 500	1 730	6 000	8 000	0,85	7309 BE
60	90	20	39 000	30 500	1 280	6 000	8 000	0,47	7210 BE
	110	27	74 100	51 000	2 200	5 300	7 000	1,10	7310 BE
65	100	21	48 800	38 000	1 630	5 600	7 500	0,62	7211 BE
	120	29	85 200	60 000	2 550	4 800	6 300	1,40	7311 BE
60	110	22	57 200	45 500	1 930	5 000	6 700	0,80	7212 BE
	130	31	95 600	69 500	3 000	4 500	6 000	1,75	7312 BE
65	120	23	66 300	54 000	2 280	4 500	6 000	1,00	7213 BE
	140	33	108 000	80 000	3 350	4 300	5 600	2,15	7313 BE

Cylindrical roller bearings
single row
d 40–45 mm



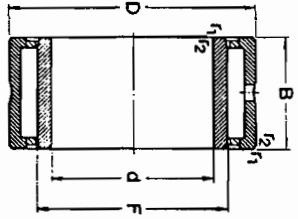
Principal dimensions	D	D	B	C	N	Basic load ratings dynamic	C ₀	Fatigue load limit P _u	Speed ratings Lubrication grease oil	Mass kg	Designation
40 (cont.)	90	90	23	80 900	78 000	10 200	6 700	8 000	0.65	NU 308 EC	
	90	90	23	80 900	78 000	10 200	6 700	8 000	0.67	NJ 308 EC	
	90	90	23	80 900	78 000	10 200	6 700	8 000	0.68	NJP 308 EC	
	90	90	23	80 900	78 000	10 200	6 700	8 000	0.64	N 308 EC	
	90	90	33	112 000	120 000	15 300	6 300	7 500	0.94	NU 2308 EC	
	90	90	33	112 000	120 000	15 300	6 300	7 500	0.96	NJ 2308 EC	
	90	90	33	112 000	120 000	15 300	6 300	7 500	0.98	NJP 2308 EC	
	110	110	27	96 800	90 000	11 600	6 000	7 000	1.30	NU 408	
	110	110	27	96 800	90 000	11 600	6 000	7 000	1.30	NJ 408	
	110	110	27	96 800	90 000	11 600	6 000	7 000	1.35	NJP 408	
45	75	75	16	44 600	52 000	6 300	9 000	11 000	0.26	NU 1009 EC	
	85	85	19	60 500	64 000	8 150	6 700	8 000	0.43	NU 209 EC	
	85	85	19	60 500	64 000	8 150	6 700	8 000	0.44	NJ 209 EC	
	85	85	19	60 500	64 000	8 150	6 700	8 000	0.45	NJP 209 EC	
	85	85	19	60 500	64 000	8 150	6 700	8 000	0.43	N 209 EC	
	85	85	23	73 700	81 500	10 600	6 700	8 000	0.52	NU 2209 EC	
	85	85	23	73 700	81 500	10 600	6 700	8 000	0.54	NJ 2209 EC	
	85	85	23	73 700	81 500	10 600	6 700	8 000	0.55	NJP 2209 EC	
	85	85	23	73 700	81 500	10 600	6 700	8 000	0.52	N 2209 EC	
	100	100	25	99 000	100 000	12 900	6 300	7 500	0.90	NU 309 EC	
100	100	25	99 000	100 000	12 900	6 300	7 500	0.92	NJ 309 EC		
100	100	25	99 000	100 000	12 900	6 300	7 500	0.95	NJP 309 EC		
100	100	25	99 000	100 000	12 900	6 300	7 500	0.98	N 309 EC		
100	100	36	138 000	153 000	20 000	5 600	6 700	1.30	NU 2309 EC		
100	100	36	138 000	153 000	20 000	5 600	6 700	1.30	NJ 2309 EC		
100	100	36	138 000	153 000	20 000	5 600	6 700	1.35	NJP 2309 EC		
120	120	29	106 000	102 000	13 400	5 600	6 700	1.65	NU 409		
120	120	29	106 000	102 000	13 400	5 600	6 700	1.65	NJ 409		
120	120	29	106 000	102 000	13 400	5 600	6 700	1.70	NJP 409		

Cylindrical roller bearings
single row
d 50–55 mm

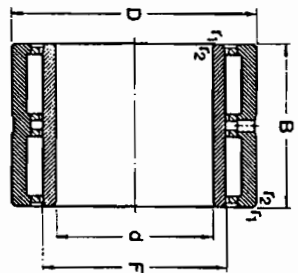


Principal dimensions	D	D	B	C	N	Basic load ratings dynamic	C ₀	Fatigue load limit P _u	Speed ratings Lubrication grease oil	Mass kg	Designation
50	80	80	16	30 800	34 500	4 000	8 500	10 000	0.31	NU 1010	
	90	90	20	64 400	69 500	8 800	6 300	7 500	0.48	NU 210 EC	
	90	90	20	64 400	69 500	8 800	6 300	7 500	0.49	NJ 210 EC	
	90	90	20	64 400	69 500	8 800	6 300	7 500	0.51	NJP 210 EC	
	90	90	20	64 400	69 500	8 800	6 300	7 500	0.48	N 210 EC	
	90	90	23	78 100	88 000	11 400	6 300	7 500	0.56	NU 2210 EC	
	90	90	23	78 100	88 000	11 400	6 300	7 500	0.58	NJ 2210 EC	
	90	90	23	78 100	88 000	11 400	6 300	7 500	0.59	NJP 2210 EC	
	110	110	27	110 000	112 000	15 000	5 000	6 000	1.15	NU 310 EC	
	110	110	27	110 000	112 000	15 000	5 000	6 000	1.15	NJ 310 EC	
55	90	90	18	57 200	69 500	8 300	7 000	8 500	0.40	NU 1011 EC	
	100	100	21	84 200	95 000	12 200	6 000	7 000	0.66	NU 211 EC	
	100	100	21	84 200	95 000	12 200	6 000	7 000	0.67	NJ 211 EC	
	100	100	21	84 200	95 000	12 200	6 000	7 000	0.69	NJP 211 EC	
	100	100	21	84 200	95 000	12 200	6 000	7 000	0.66	N 211 EC	
	100	100	25	99 000	118 000	15 300	6 000	7 000	0.79	NU 2211 EC	
	100	100	25	99 000	118 000	15 300	6 000	7 000	0.81	NJ 2211 EC	
	100	100	25	99 000	118 000	15 300	6 000	7 000	0.82	NJP 2211 EC	
	100	100	25	99 000	118 000	15 300	6 000	7 000	0.79	N 2211 EC	
	120	120	29	138 000	143 000	18 600	4 800	5 600	1.45	NU 311 EC	
120	120	29	138 000	143 000	18 600	4 800	5 600	1.50	NJ 311 EC		
120	120	29	138 000	143 000	18 600	4 800	5 600	1.55	NJP 311 EC		
120	120	29	138 000	143 000	18 600	4 800	5 600	1.45	N 311 EC		

Needle roller bearings with flanges
with inner ring
d 40-65 mm



Series Nk(S), NA 49



Series NA 69

Principal dimensions	d	D	B	Basic load ratings		Fatigue load limit P_u	Speed ratings		Mass	Designation
				dynamic	static C_0		Lubrication: grease oil	t/min		
				N		N				
	mm									
40	55	20	27	500	57 000	7 200	6 300	9 000	0,14	Nk1 40/20
	55	30	40	200	93 000	12 000	6 300	9 000	0,22	Nk1 40/30
	62	22	42	900	71 000	9 150	5 600	8 000	0,23	NA 4908
	62	40	67	100	125 000	16 000	5 600	8 000	0,43	NA 6908
	65	22	42	900	72 000	9 150	5 600	8 000	0,28	Nk(S) 40
42	57	20	29	200	61 000	7 650	6 000	8 500	0,15	Nk1 42/20
	57	30	41	800	98 000	12 900	6 000	8 500	0,22	Nk1 42/30
45	62	25	38	000	78 000	10 000	5 600	8 000	0,23	Nk1 45/25
	62	35	48	500	110 000	14 300	5 600	8 000	0,32	Nk1 45/35
	68	22	45	700	79 000	10 000	5 300	7 500	0,27	NA 4909
	68	40	70	400	137 000	17 300	5 300	7 500	0,50	NA 6909
	88	22	44	600	78 000	10 000	5 000	7 000	0,34	Nk(S) 45
50	68	25	40	200	88 000	11 200	5 300	7 500	0,27	Nk1 50/25
	68	35	52	300	122 000	16 000	5 300	7 500	0,38	Nk1 50/35
	72	22	47	300	85 000	11 000	5 000	7 000	0,27	NA 4910
	72	40	73	700	150 000	19 000	4 500	6 300	0,52	NA 6910
	80	28	62	700	104 000	13 700	4 500	6 300	0,52	Nk(S) 50
55	72	25	41	800	96 500	12 200	4 800	6 700	0,27	Nk1 55/25
	72	35	55	000	134 000	17 600	4 800	6 700	0,38	Nk1 55/35
	80	25	57	200	106 000	13 700	4 500	6 300	0,40	NA 4911
	80	45	89	700	190 000	24 000	4 500	6 300	0,78	NA 6911
	85	28	66	000	114 000	15 000	4 300	6 000	0,56	Nk(S) 55
60	82	25	44	000	95 000	12 000	4 300	6 000	0,40	Nk1 60/25
	82	35	60	500	146 000	19 000	4 300	6 000	0,55	Nk1 60/35
	85	25	60	500	114 000	14 600	4 300	6 000	0,43	NA 4912
	85	45	93	500	204 000	26 000	4 300	6 000	0,81	NA 6912
	90	28	68	200	120 000	15 600	4 000	5 600	0,56	Nk(S) 60
65	90	25	61	600	120 000	15 300	4 000	5 600	0,46	NA 4913
	90	35	82	800	169 000	21 800	4 000	5 600	0,47	Nk1 65/25
	90	45	73	700	163 000	21 800	4 000	5 600	0,86	Nk1 65/35
	95	28	70	400	132 000	17 000	3 800	5 300	0,83	NA 6913
									0,64	Nk(S) 65