ENGINEERING TRIPOS PART IIA

Friday 27 April 2007 2.30 to 4

Module 3D5

ENVIRONMENTAL ENGINEERING I

Answer not more than three questions.

All questions carry the same number of marks.

The approximate percentage of marks allocated to each part of a question is indicated in the right margin.

Attachment: Environmental Engineering I Data Sheet (6 pages)

STATIONERY REQUIREMENTS

SPECIAL REQUIREMENTS

Single-sided script paper

Engineering Data Book

Graph paper

CUED approved calculator allowed

You may not start to read the questions printed on the subsequent pages of this question paper until instructed that you may do so by the Invigilator

1 (a) Rain falls uniformly and at constant intensity for 3 hours over a small urban catchment of area 20 km². The distribution percentages for the outflow hydrograph over six successive 3 hour periods starting at the beginning of the rainfall are 5, 17, 28, 23, 16, 11. Assuming that the catchment is impervious, estimate the distribution percentages over successive one hour intervals from uniform rainfall of one hour duration and of 15 mm hr⁻¹ intensity. Plot the shape of this hydrograph and estimate the peak outflow in m³s⁻¹.

[40%]

(b) Explain why a steady flow in an open channel cannot undergo a smooth transition from upstream supercritical flow to downstream subcritical flow.

[40%]

(c) Explain why the fall velocity of sand particles (of diameter D) in water (as given on the Data Sheet) is proportional to $D^{1/2}$ for large particles, but proportional to D^2 for small particles.

[20%]

A wide flat smooth channel of rectangular cross-section and of length 500 m is carrying a steady flow with depth 1.8 m and mean velocity 0.6 m s⁻¹ towards a power station at its downstream end. At time t = 0 the power station releases a large quantity of water into the channel causing the depth in the channel adjacent to the power station to rise at a rate of 1 metre per minute for 2 minutes. The depth adjacent to the power station remains constant thereafter. At what time t does the depth at the upstream end of the channel reach a maximum?

[100%]

A straight wide open channel of uniform cross-section has a bed-slope of 0.00015. The flow is steady and has a depth of 1.2 m. The suspended sediment can be considered to be the sediment carried above the bed layer, which is 0.015 m thick. The concentration of suspended sediment at the top of the bed layer is 8.6 kg m⁻³.

Assume that the Karman constant is 0.4, the bed roughness height is 0.015 m, the specific gravity of the sediment grains is 2.65, all grain diameters are 0.09 mm, the kinematic viscosity of water v is 10^{-6} m² s⁻¹ and the water temperature is 20° C.

(a) Estimate the flow velocity at the top surface of the channel. [30%]

- (b) Estimate the sediment transport rate in suspension per metre width above the bed layer. [50%]
 - (c) What, according to various theories, would be the bed regime? [20%]

4 (a) A centrifugal pump when run at 750 rpm gave the following relationship between head, discharge and efficiency:

Discharge (litres per second)	Head (metres)	Efficiency (%)		
0	32.3	-		
5	32.0	59		
9.5	31.4	74		
14	29.3	81		
18.5	23.8	79		
23	n	_		

The pump is connected to a pipe system which discharges to atmosphere at 20 m above sump level, and the total energy losses (in metres) can be found from the equation:

$$h_f = 0.02 Q^2$$
 (where Q is in litres/second)

Calculate the discharge and the pump input power.

Note:
$$Q_1/Q_2 = N_1/N_2$$
 and $H_1/H_2 = N_1^2/N_2^2$ where N is pump speed. [50%]

(b) It is expected that future encrustation in the pipe will reduce the pipe diameter and increase the friction factor so that the total energy losses in the system will become:

$$h_f = 0.03 Q^2$$
 (where Q is in litres/second)

Calculate the new pump speed required in order to maintain the same flow. If the cost of electricity is 6p/kW hour calculate the extra cost each day of running the pump. [50%]

END OF PAPER



Module 3D5: Environmental Engineering I

Data Sheet

(SI units throughout)

f-capacity equation

$$f = f_c + (f_0 - f_c) e^{-K_f t}$$

Spatially-varied flow (backwater curves)

$$\delta d = \ell \left(\frac{S - \overline{U}^2 C_f / 2gR}{1 - \overline{U}^2 / gd} \right)$$

Open-channel characteristics

$$\overline{U} + 2c - g(S - S_f)t = const$$

$$\frac{dx}{dt} = \overline{U} + c$$

$$\overline{U} - 2c - g(S - S_f)t = const$$

$$\frac{dx}{dt} = \overline{U} - c$$

Fall velocity of particles of sand in water (20°C)

$$W = 56 \times 10^4 D^2 (\rho_s - \rho) / \rho$$

For
$$D > 0.002$$
 m (and shape factor=0.7)

$$W \stackrel{.}{=} 3.3 D^{1/2} ((\rho_s - \rho)/\rho)^{1/2}$$

Initial motion of sediment on a flat bed

$$\frac{u_*k_*}{v} > 70$$

$$\frac{\tau_c}{(\rho_s - \rho)gD} = 0.05$$

Velocity in uniform flow in a channel

$$\overline{U} = CR^{\frac{1}{2}}S^{\frac{1}{2}}$$

$$\overline{U} = \frac{1}{n}R^{\frac{2}{3}}S^{\frac{1}{2}}$$



Prandtl-Karman

Hydraulically smooth
$$\left(\frac{u_{\star}k_{s}}{v} < 5\right)$$
 $\frac{u}{u_{\star}} = 2.5 \log_{\epsilon}\left(\frac{9.05yu_{\star}}{v}\right)$ $\frac{\overline{U}}{u_{\star}} = 2.5 \log_{\epsilon}\left(\frac{3.66Ru_{\star}}{v}\right)$ Hydraulically rough $\left(\frac{u_{\star}k_{s}}{v} > 70\right)$ $\frac{u}{u_{\star}} = 2.5 \log_{\epsilon}\left(\frac{30.2y}{k_{s}}\right)$ $\frac{\overline{U}}{u_{\star}} = 2.5 \log_{\epsilon}\left(\frac{12.1R}{k_{\star}}\right)$

Variation of the concentration of sediment in suspension with distance from the bed

$$\frac{C}{C_a} = \left[\left(\frac{d - y}{y} \right) \left(\frac{a}{d - a} \right) \right]^{\frac{W}{Ku_*}}$$

Sediment load in suspension

$$\int_{b}^{d} Cu dy = 11.6u \cdot C_{b} b [I_{1} \log_{e}(Ad) + I_{2}]$$

where
$$A = \frac{9.05u}{v}$$
 for a hydraulically smooth bed
$$= \frac{30.2}{k}$$
 for a hydraulically rough bed

	$W/Ku_{\star} = 0.2$ $W/Ku_{\star} = 0.6$			****		XX/77 1.6		
	W/Ku,	_* = 0.2	$W/Ku_* = 0.6$		$W/Ku_* = 1.0$		$W/Ku_* = 1.5$	
b/d	I_1	I ₂	Iı	I ₂	I ₁	I ₂	Iı	I ₂
0.02	5.003	5.960	1.527	2.687	0.646	1.448	0.310	0.873
0.01	8.892	11.20	2.174	4.254	0.788	2.107	0.341	1.146
0.005	15.67	20.47	3.033	6.448	0.934	2.837	0.366	1.431
0.004	18.77	24.73	3.364	7.318	0.981	3.094	0.372	1.525
0.003	23.71	31.53	3.838	8.579	1.042	3.444	0.379	1.647
0.002	32.88	44.23	4.608	10.65	1.129	3.967	0.389	1.819
0.001	57.46	78.30	6.247	15.17	1.277	4.944	0.401	2.117
0.0005	100.2	137.7	8.413	21.26	1.426	6.027	0.409	2.413
0.0001	363.9	504.9	16.50	44.53	1.773	8.947	0.422	3.113

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Limiting shear stress for a particle on a slope

$$\frac{\left(\tau_c\right)_{\theta}}{\tau_c} = \cos\theta \left(1 - \frac{Tan^2\theta}{Tan^2\phi}\right)^{\frac{1}{2}}$$

"Regime" formulae

$$\overline{U} = 0.635 \quad \int^{\frac{1}{2}} R^{\frac{1}{2}}$$

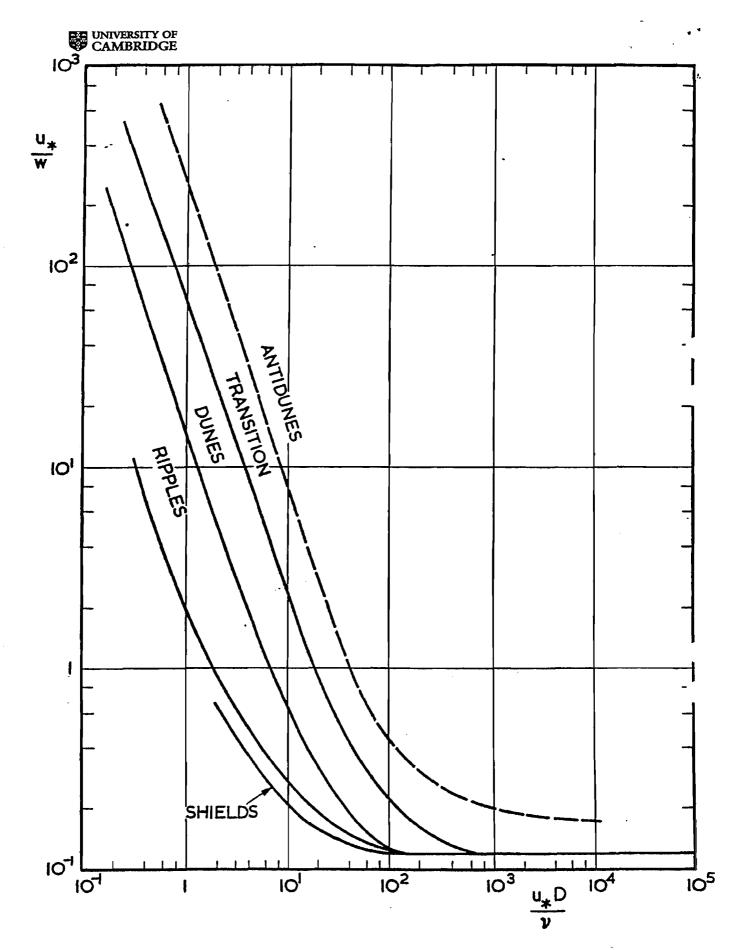
$$P = 4.83 \quad Q^{\frac{1}{2}}$$

$$R = 0.4725 \quad Q^{\frac{1}{3}} \int^{-\frac{1}{3}}$$

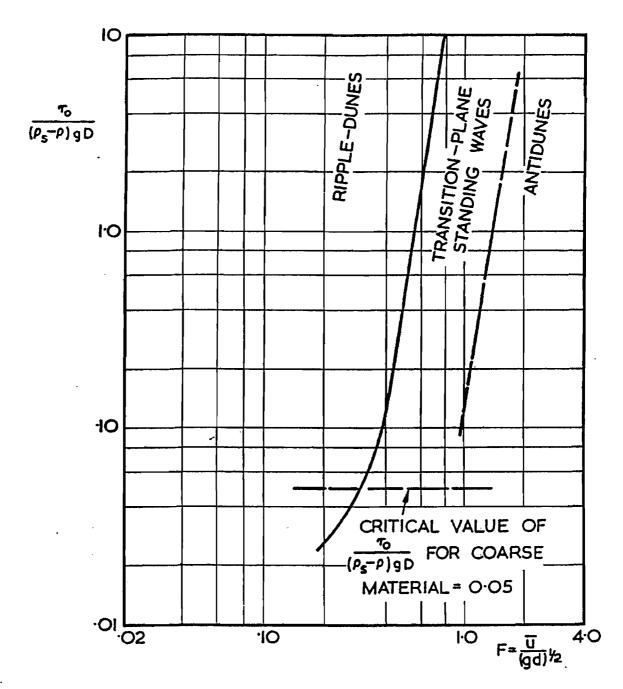
$$S = 0.000303 \quad \int^{\frac{5}{3}} Q^{-\frac{1}{6}}$$

SYMBOLS

- Concentration of sediment. Chezy roughness coefficient $\left(=(2g/C_f)^{1/2}\right)$ C
- friction coefficient
- grain size or body diameter
- D₆₅ grain size for which 65% by weight of grains have a smaller diameter
- Lacey silt factor
- fo, fc coefficients in f-capacity equation
- h K ripple height
- Karman constant
- K_f coefficient in f-capacity equation
- roughness height
- wetted perimeter of a channel
- total flow rate of water Q
- hydraulic radius (=A/P)R
- S channel slope
- t
- horizontal component of fluid velocity u
- \overline{U} mean velocity
- $(\tau, /\rho)^{v_1}$ u*
- v vertical component of fluid velocity
- W fall velocity
- x,y co-ordinates
- angle of a slope to the horizontal
- angle of repose of sediment φ
- kinematic viscosity
- density of fluid ρ
- density of sediment ρ_{s}
- shear stress on the bed τ_{\bullet}
- critical value of τ , for sand movement τ_{ϵ}

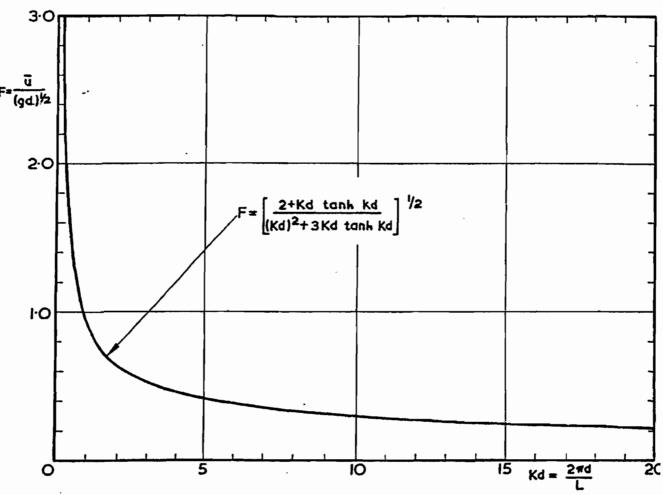


BED REGIMES IN OPEN CHANNEL FLOW (Albertson Simons & Richardson)

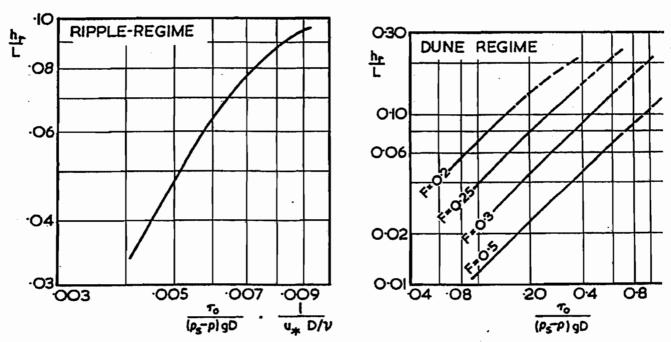


BED REGIMES IN OPEN-CHANNEL FLOW (Garde & Albertson)





WAVELENGTH OF DUNES (Kennedy)



RIPPLE/DUNE STEEPNESS (Garde & Albertson)

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Answers

- 1. a) 1,4,5,5,7,8,10,10,9,7,7,6,5,5,4,3,4,0 and 8.33 $\,\mathrm{m}^3/\mathrm{s}$
- 2 174 seconds
- 3 a) 0.82 m/s
 - b) 2.46 kg/s per metre width
 - c) Dunes (Albertson, Simons, Richardson) Ripple-dunes (Garde and Albertson)
- 4 a) 17 litres/sec and 5.33 kW
 - b) 777 rpm and 91p per day