

ENGINEERING TRIPOS PART IIA

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Tuesday 28 April 2009 2.30 to 4.00

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Module 3B1

RADIO FREQUENCY ELECTRONICS

*Answer not more than **three** questions.*

*All questions carry the same number of marks.*

*The **approximate** percentage of marks allocated to each part of a question is indicated in the right margin.*

*Attachment:*

*Chart for question 4, to be detached and submitted with the solution.*

STATIONERY REQUIREMENTS

Single-sided script paper

SPECIAL REQUIREMENTS

Engineering Data Book

CUED approved calculator allowed

**You may not start to read the questions printed on the subsequent pages of this question paper until instructed that you may do so by the Invigilator**

1 A new electric aircraft is fitted with a radio telemetry system to transmit data back to a base station at the airfield. The transmitter operates at 433 MHz with a power of 10 mW and uses a small isotropic (unity gain) antenna. In order to achieve good reception range, the base station uses an antenna with a *Gain* of 30, which is pointed in the direction of the aircraft to maximise the signal.

(a) Define the terms *Gain*, *Effective Aperture*, *Directivity* and *Radiation Resistance* for an antenna and explain how they are inter-related. [20%]

(b) If the telemetry system receiving antenna is connected to a matched impedance of  $75 \Omega$  and the receiver input circuitry is sensitive down to  $10 \mu\text{V}$ , what is the maximum aircraft range that can be achieved for the data to be received? [40%]

(c) In an attempt to improve performance, the engineer decides to change the transmitter antenna for a quarter-wave dipole. How long should the new antenna be and by how much will this increase the working range? Are there any disadvantages to using it? [15%]

(d) It is also proposed to use the same quarter-wave antenna for the aircraft's radio-telephony, which operates at 175 MHz. If the *Radiation Efficiency* at 433 MHz is 90%, and the antenna comprises a large diameter piece of wire, what is its *Radiation Efficiency* at 175 MHz? [25%]

State all assumptions and approximations made.

2 A digital radio telemetry system uses a diode ring mixer in its receiver to mix the incoming RF signal with that from a Local Oscillator (LO), to produce the Intermediate Frequency (IF) signal. Another diode ring mixer is also used in the Local Oscillator, to double the frequency produced by a quartz crystal oscillator.

(a) Draw the circuit for a diode ring mixer and briefly explain how it operates for frequency mixing and doubling. What provisions could be made to ensure that the mixer output does not contain a DC component ? [25%]

(b) After demodulation the telemetry receiver outputs an analogue square-wave signal, which is unfortunately subject to substantial higher frequency interference and voltage spikes. If the maximum data rate is 4800 bits/second, design a suitable 4-pole VCVS filter, using 10 k $\Omega$  resistors, to clean up the signal prior to it being fed into a comparator to reconstruct the digital data stream. Justify your choices of filter type and cut-off frequency. A filter design table is given below. [40%]

(c) The front-end of the receiver uses a resonant LC tank circuit, where  $L = 10 \mu\text{H}$  and  $C = 330 \text{ pF}$ . If the inductor has a series resistance of 3  $\Omega$ , estimate the  $Q$ -factor of the tank circuit. How could a *Negative Impedance Converter* (NIC) be used to increase the  $Q$ -factor to 100 ? [35%]

VCVS 4-pole filter design table

Bessel		Butterworth		Chebyshev 0.5 dB	
$f_n$	$A$	$f_n$	$A$	$f_n$	$A$
1.432	1.084	1.000	1.152	0.597	1.582
1.606	1.759	1.000	2.235	1.031	2.660

State all assumptions and approximations made.

(TURN OVER

3 A low cost data transmission system comprises a microstrip patch antenna, with two feed points, linked to an amplifier in a feedback configuration such that it oscillates and radiates at 1.5 GHz. The amplifier supply voltage is modulated 0 – 10 V by the data signal to give an *Amplitude Modulated* (AM) carrier wave.

(a) Draw the circuit for a suitable single stage transistor amplifier and select component values to give input and output impedances of approximately  $100 \Omega$  and 10 dB of gain when loaded. Assume a bipolar transistor is available with  $h_{fe} = 200$ . [25%]

(b) Estimate the bandwidth of the amplifier, when connected to a matched source, if the transistor has the following properties:  $f_t = 22 \text{ GHz}$ ,  $c_{cb} = 0.15 \text{ pF}$ ,  $c_{oe} = \text{negligible}$ . [30%]

(c) Briefly describe the mode of operation of a microstrip patch antenna and calculate the length of a 1.5 GHz resonant patch, assuming the dielectric substrate has a *Relative Permittivity* of 3. [15%]

(d) How should the patch be connected with the amplifier to realise an oscillator circuit? [15%]

(e) If the substrate dielectric is 1.6 mm thick, what width should the microstrip feed lines be to give a *Characteristic Impedance* of  $100 \Omega$ ? [15%]

State all assumptions and approximations made.

4 A digital set-top box produces an RF signal at 500 MHz, to be plugged into an old fashioned analogue TV set with an aerial socket impedance of  $75 \Omega$ . The amplifier within the set-top box has an output impedance represented by a resistance of  $165 \Omega$  in series with an inductance of 28.6 nH.

(a) By calculation, design an impedance matching circuit, using three passive components, for this application. [20%]

(b) Using the Smith Chart, design impedance matching circuits comprising the following components:-

- (i) an inductor and a capacitor
- (ii) a capacitor and a length of  $75 \Omega$  coaxial cable
- (iii) an inductor and a length of  $75 \Omega$  coaxial cable [45%]

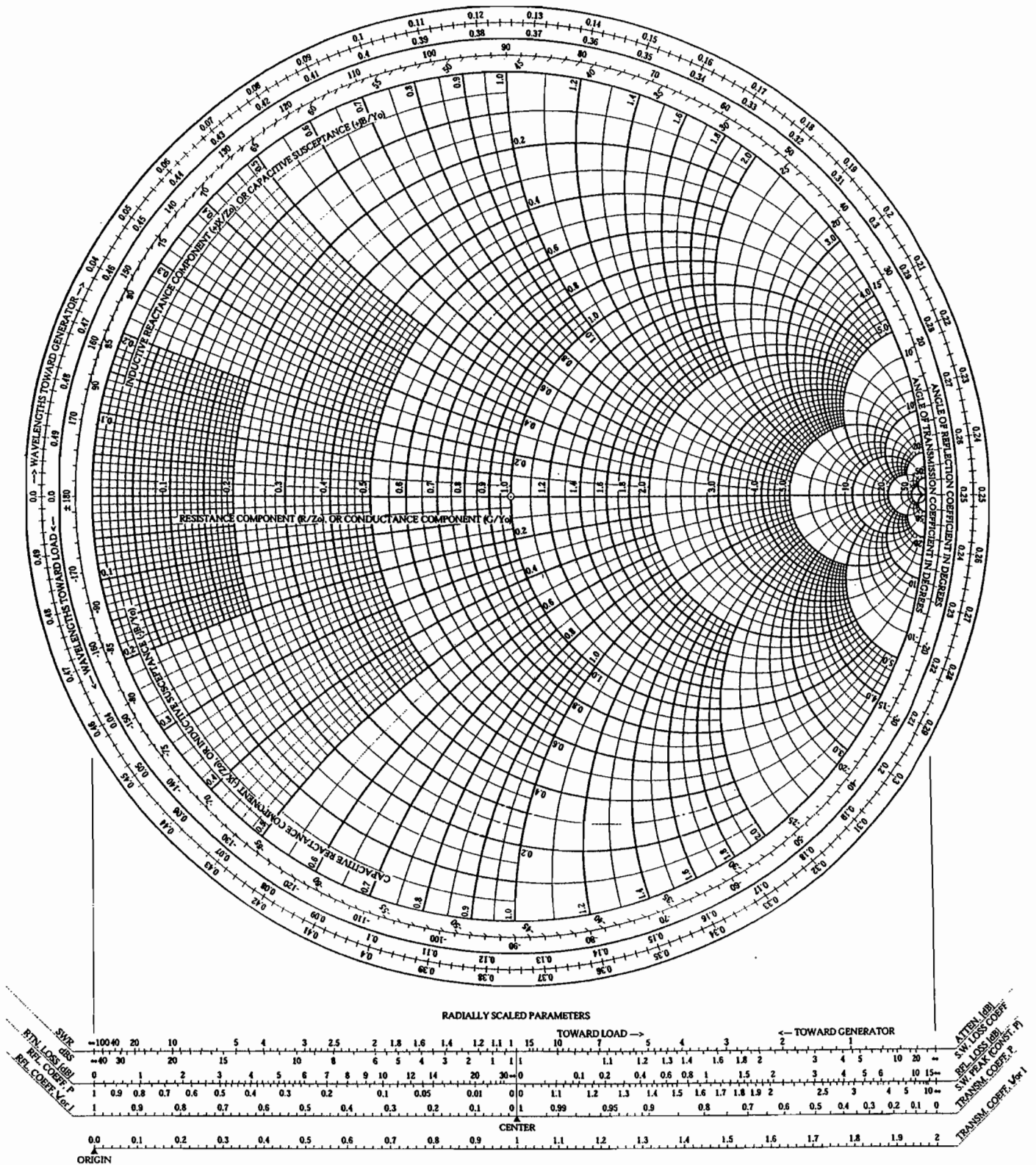
(c) If the coaxial cable dielectric has a *Relative Permittivity*,  $\epsilon_r = 2.2$  and costs 20 pence per metre, a capacitor costs 2 pence and an inductor 10 pence, which matching circuit would be the cheapest? [15%]

(d) Considering the matching circuit which comprises an inductor and a length of coaxial cable, if the set-top box output frequency is changed to 420 MHz but the matching circuit is left unchanged, estimate the magnitude of the *Voltage Reflection Coefficient* which would result from such a frequency change. [20%]

State all assumptions and approximations made.

**END OF PAPER**

Chart for question 4; to be detached and handed in with script.



3B1 – 2009 Numerical answers

1 (b) 26.2 km (1.33 pW)

1 (c) 17.3 cm each half. Range increases to 32.1 km

1(d) 70%

2 (b) Use a low pass Bessel filter (for pulse shape) @ 9600 Hz.  $C_1 = 1.16$  nF,  $C_2 = 1.03$  nF

2(c)  $Q = 58$  with equiv.  $R = 10.1$  k $\Omega$ . For  $Q=100$ ,  $R' = 17.4$  k $\Omega$ , hence shunt with  $-24$  k $\Omega$

3 (a)  $R_4 = 100$   $\Omega$ ,  $R_3 = 15$   $\Omega$ ,  $R_2 = 120$   $\Omega$ ,  $R_1 = 680$   $\Omega$

3 (b) 1.46 GHz (or 2.9 GHz incl. source impedance of 100  $\Omega$  )

3 (c) 57.7 mm

3 (e) 0.28 mm

4 (a)  $C_{\text{series}} = 3.54$  pF,  $C = 3.9$  pF,  $L = 48$  nH

4 (b) (i) series 3.03 pF, parallel 85.3 nH  
(ii) 26.3 nH and  $0.118 \lambda$   
(iii) 3.79 pF and  $0.449 \lambda$

4 (c) coax. + C = 5.6 pence

4 (d) Voltage refl. coeff. = 0.15