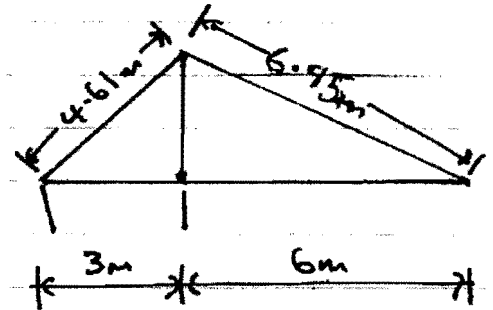
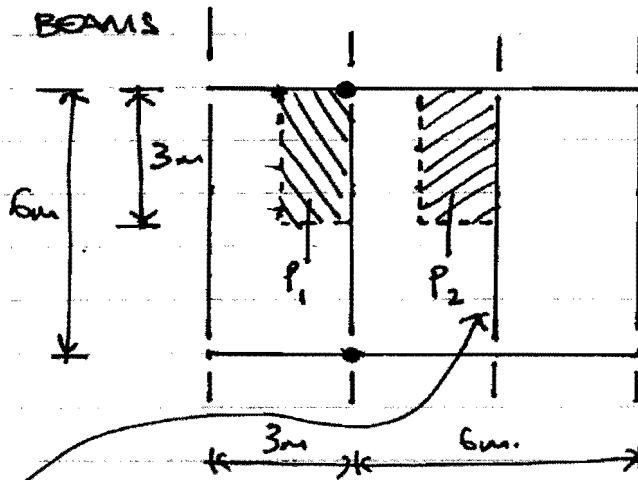


2003/2013/1/1

1a) VERTICAL LOADS ARISING FROM SELF-WEIGHT OF METAL CHABBING AND SNOW LOADS ARE RESISTED BY ONE-WAY FLEXURE OF METAL DECK.

THIS IS TRANSMITTED AS A UDL TO THE SECONDARY BEAMS



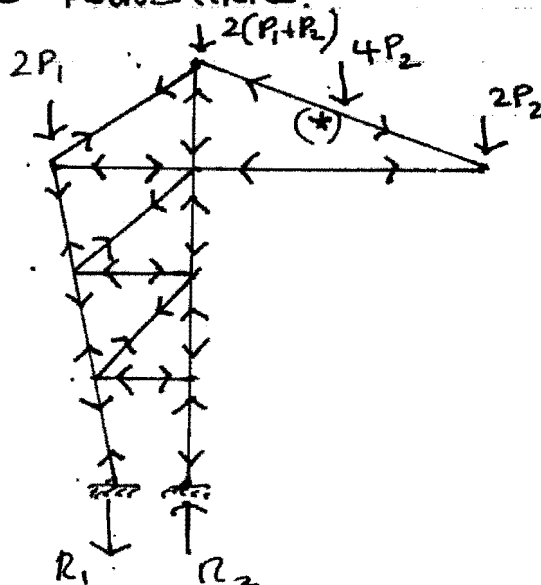
$$\therefore P_1 = q \times \frac{6}{2} \times \frac{4.61}{2}$$

$$P_2 = q \times \frac{6}{2} \times \frac{6.95}{4}$$

\therefore LOAD ON SECONDARY BEAM = $4P_2$

WHERE q = VERTICAL DESIGN LOAD

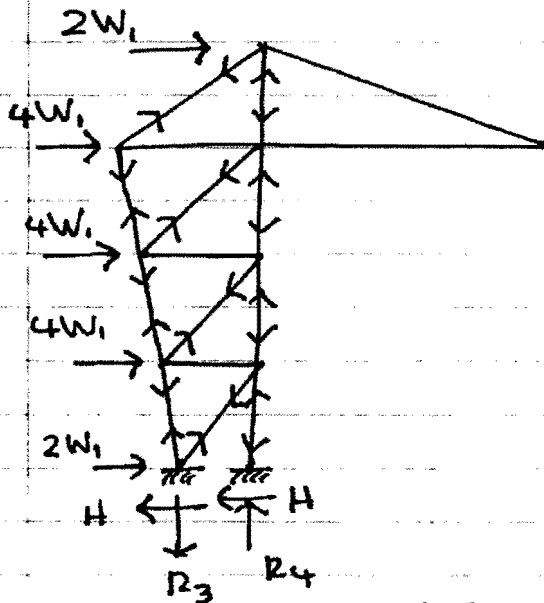
THE SECONDARY BEAMS ARE IN TURN SUPPORTED BY THE PRIMARY BEAMS (SKETCH BELOW). THESE POINT LOADS ARE TRANSFERRED AS TENSION / COMPRESSION IN THE TRIANGULATED FRAME AND SAFELY TO THE FOUNDATIONS.



(*) THIS MEMBER IN THE PRIMARY FRAME IS SUBJECTED TO FURTHER IN ADDITION TO TENSION. ALL OTHER MEMBERS IN PRIMARY FRAME ARE STAYS OR TIES.

HORIZONTAL LOADS IMPOSED BY WIND PRESSURE ARE RESISTED BY FLEXURE OF METAL CLADDING. THIS IS TRANSMITTED AS A UDL ON SECONDARY BEAMS (SIMILAR TO VERTICAL LOADS) WHERE:

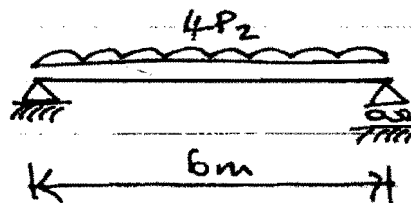
$$W_1 = w \times \frac{3.5}{2} \times \frac{6}{2} \quad (w = \text{WIND PRESSURE})$$



THESE ARE TRANSMITTED AS POINT LOADS ON THE PRIMARY FRAME (SKETCH LEFT). THESE POINT LOADS ARE SUBSEQUENTLY TRANSFERRED AS TENSION / COMPRESSION IN THE TRIANGULATED FRAME AND SAFELY TO THE FOUNDATIONS.

NOTE: STABILITY / LOAD PATH FOR TRANSVERSE WIND LOADS NOT DISCUSSED HERE.

1bi) SECONDARY BEAM A:



LOADS:

$$P_2 \text{ AT ULS} = \left[(1.2 \times 0.15 \text{ kN/m}) + (1.2 \times 0.75 \text{ kN/m}) \right] \times \frac{6}{2} \times \frac{6.9}{4}$$

$$= 5.63 \text{ kN}$$

$$\therefore 4P_2 \text{ AT ULS} = 22.52 \text{ kN} \quad (\text{EXCLUDES SELF. WT. OF BEAM})$$

$$4P_2 \text{ AT SLS} = 18.77 \text{ kN}$$

BENDING CAPACITY (ULS)

$$M_{APP} = (P_2) l / 8 = 22.52 \times 6 / 8 = 16.89 \text{ kNm}$$

$$\text{T124 UB } 203 \times 102 \times 23 \quad (Z_p = 234 \text{ cm}^3; f_p = 83.1 \text{ kN/m})$$

THEORETICAL ELASTIC CRITICAL MOMENT:

$$M_c = \frac{\pi^2}{L^2} \left[EI_{yy} \left(GJ + \frac{\pi^2}{L^2} EC_w \right) \right]^{0.5}$$

$$C_w = \frac{D^2 I_{yy}}{4} = \frac{0.1939^2 \times 164 \times 10^{-8}}{4} = 1.54 \times 10^{-8}$$

$$\therefore M_c = \frac{\pi^2}{L^2} \left\{ 210 \times 10^9 \times 164 \times 10^{-8} \left[(81 \times 10^9 \times 7.02 \times 10^{-8}) + \frac{\pi^2}{36} (210 \times 10^9 \times 1.5 \times 10^{-8}) \right] \right\}^{0.5}$$

$$= 24.9 \text{ kNm}$$

$$\lambda_{LT} = \sqrt{\frac{N_{FP}}{M_c}} = \sqrt{\frac{83.1}{24.9}} = 1.82$$

$$\therefore \chi_{LT} \approx 0.25 \text{ (FROM LTB CHART IN DATA SHEET)}$$

$$\therefore M_{cr} = 0.25 \times 83.1 \text{ kNm} = 20.76 \text{ kNm} > 16.89 \text{ kNm}$$

NOTE: ADDITIONAL MOMENT

$$\text{AT ULS DUE TO SELF WT.} = (23 \times 9.81) \times 6^2 / 8 \times 1.2$$

$$= 1.2 \text{ kNm}$$

$$20.76 \text{ kNm} > (16.89 + 1.2) \text{ kNm}$$

\(\therefore\) UB 203 x 102 x 23 is SATISFACTORY

DEFLECTION (SLS)

$$\delta_{MAX} = 6000 / 200 = 30 \text{ mm}$$

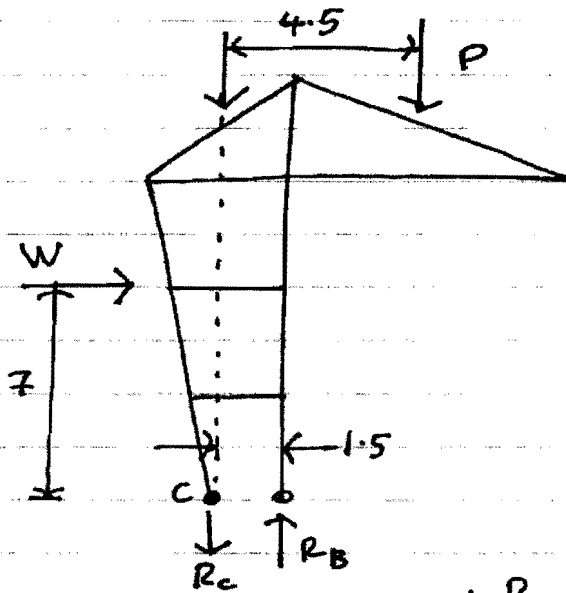
$$\delta = \frac{5 (4P_2) l^3}{384 EI} = \frac{5 \times 18.77 \times 10^3 \times 6000^3}{384 \times 210 \times 10^3 \times 2105 \times 10^4}$$

$$= -11.94 \text{ mm} < 30 \text{ mm}$$

\(\therefore\) UB 203 x 102 x 23 is SATISFACTORY

303/2013/1/4

1bii) COLUMN B LOADS:



$$\therefore R_B = \frac{1}{1.5} (7W + 4.5P)$$

WHERE: $P = q \times 6 \times 6.95$

$$W = w \times 6 \times 14$$

$q =$ VERTICAL LOAD INTENSITY

$w =$ WIND LOAD INTENSITY

$$\therefore \text{AT ULS: } q = 1.2 \times (0.15 + 0.75) = 1.08 \text{ kN/m}^2$$

$$w = 1.2 \times 2 = 2.4 \text{ kN/m}^2$$

$$\therefore R_B = \frac{1}{1.5} (7 \times 201.6 + 4.5 \times 45) = \underline{1076 \text{ kN}}$$

TRY UC 203x203x46 (PLASTIC SWAYH LOAD = $5870 \times 355 = 2084 \text{ kN}$)

$$\lambda = \frac{350}{5.13} = 68.2 ; \lambda_e = \pi \sqrt{\frac{210 \times 10^3}{355}} = 76.4$$

$$\therefore \bar{\lambda} = 68.2 / 76.4 = 0.89 ; r/y = 5.13 / (203/2) = 0.505$$

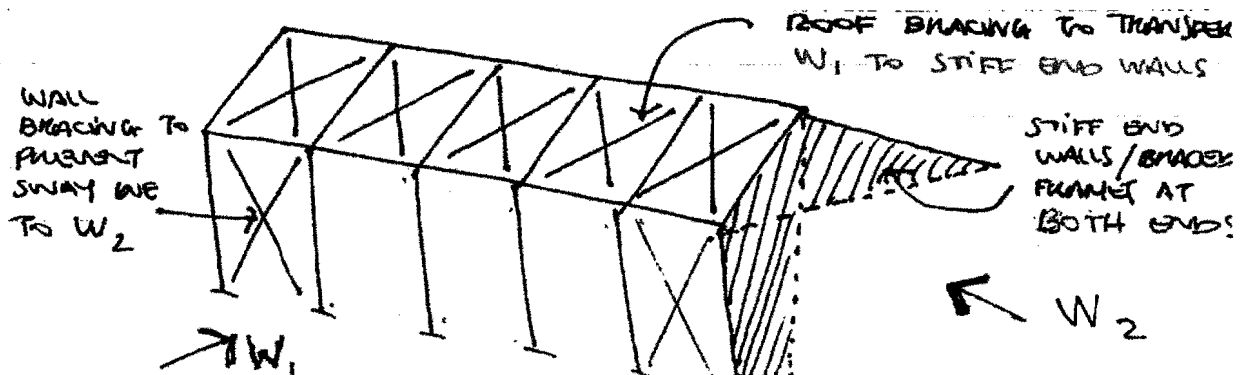
\therefore USE CURVE B

$\alpha \approx 0.66$ (FROM BUCKLING CHART IN DATA SHEET)

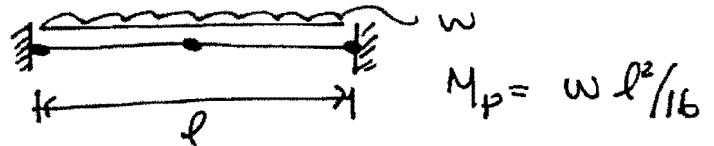
$$\therefore R_{ult} = 0.66 \times 2084 \text{ kN} = 1375 \text{ kN} > 1076 \text{ kN}$$

\therefore UC 203x203x46 IS SATISFACTORY.

1c)



2 a) FIRST ESTIMATE \Rightarrow ASSUME FIXED ENDED BEAM



WHERE l IS THE CLEAR SPAN BETWEEN HANGERS
 $= 2(16-3) = 26\text{m}$

$$\therefore M_p = 9 \times 26^2 / 16 = 380.3 \text{ kNm}$$

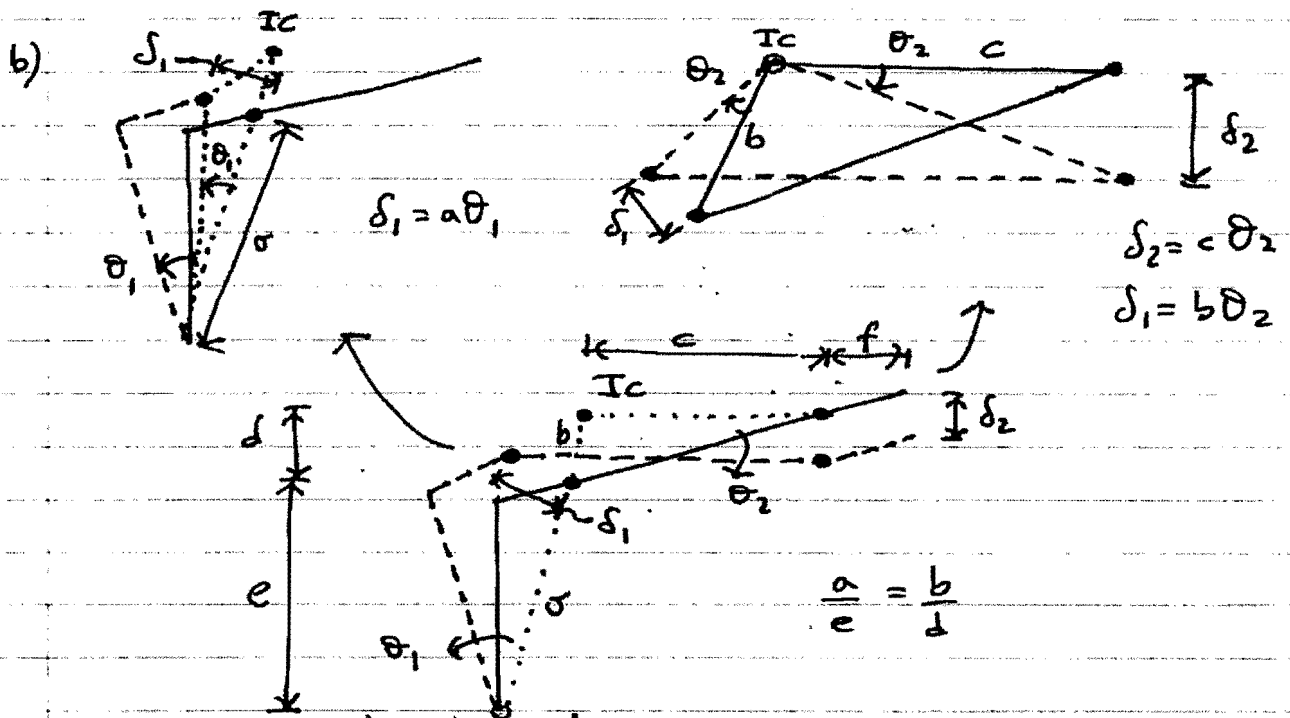
$$\text{DESIGN YIELD STRESS} = \sigma_y / \gamma_m = \frac{275}{1.05} = 262 \text{ MPa}$$

$$\therefore Z_p = 380.3 \times 10^3 \text{ Nm} / 262 \text{ MPa} = 1452 \text{ cm}^3$$

TRY UB 457 x 152 x 67 ($Z_p = 1453 \text{ cm}^3$; $M_p = 380.6 \text{ kNm}$)

$$\therefore \text{SELF-WT.} = 67 \times 9.81 \times 1.4 / (10)^3 = 0.93 \text{ kN/m}$$

$$\therefore \text{REVISED LOAD} = 9 + 0.93 = \underline{9.93 \text{ kN/m}}$$



$$\therefore \theta_1 = \frac{b\theta_2}{a} = \frac{d\delta_2}{ec} \quad ; \quad \theta_2 = \delta_2 / c$$

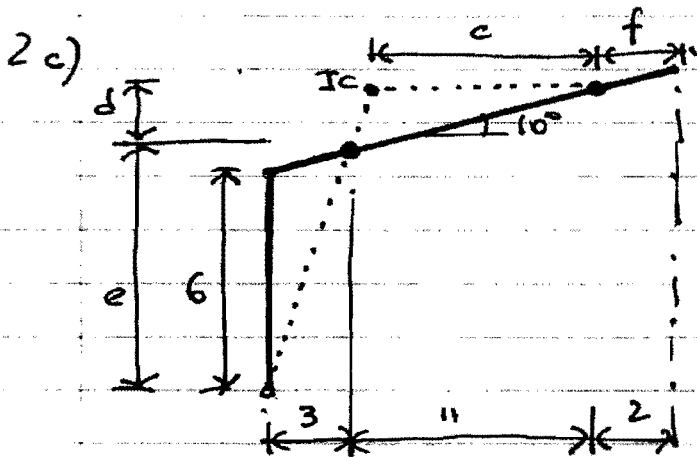
EXTERNAL WORK DONE = WORK DISSIPATED IN HINGES

$$2 \times \underbrace{\left(w f \delta_2 + w c \delta_2 / 2 \right)}_{2 \text{ HALVES}} = \underbrace{2 M_p \left[(\theta_1 + \theta_2) + \theta_2 \right]}_{2 \text{ HALVES}}$$

IGNORES -VE WORK DONE BY RISING OF RAFTER OVER HAUNCH REGION.

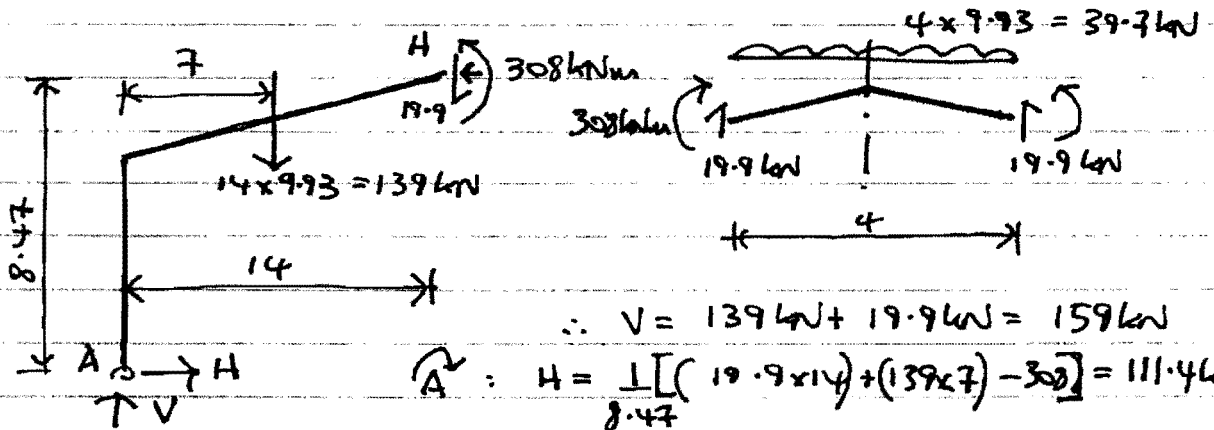
$$\therefore w \delta_2 \left(f + \frac{c}{2} \right) = M_p \left(\underbrace{\frac{\delta_2 d}{c e}}_{\theta_1} + \underbrace{2 \frac{\delta_2}{c}}_{2\theta_2} \right)$$

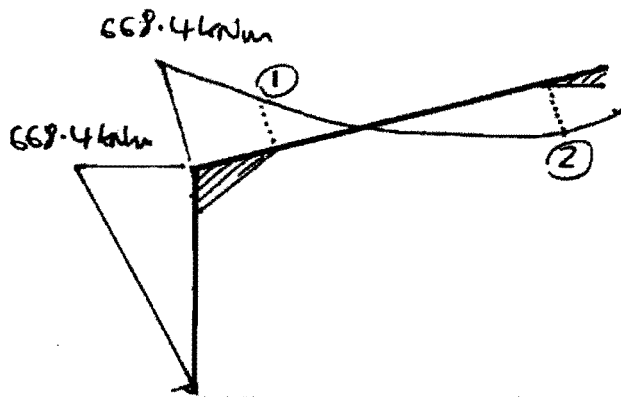
$$M_p = \frac{w \left(f + \frac{c}{2} \right)}{\left(\frac{d}{c e} + \frac{2}{c} \right)} = \frac{\frac{w c}{2} \left(\frac{2f}{c} + 1 \right)}{\frac{2}{c} \left(\frac{d}{2e} + 1 \right)} = \frac{w c^2}{4} \left[\frac{1 + 2f/c}{1 + d/2e} \right]$$



$d = 11 \tan 10^\circ = 1.94 \text{ m}$
 $e = 6 + 3 \tan 10^\circ = 6.53 \text{ m}$
 $g = \frac{3}{6.53} (6.53 + 1.94) = 3.89 \text{ m}$
 $c = 16 - (3.89 + 2) = 10.11 \text{ m}$

$$\therefore M_p = \frac{9.93 \times 10.11^2}{4} \left[\frac{1 + 4/10.11}{1 + 1.94/13.06} \right] = 308.3 \text{ kNm}$$

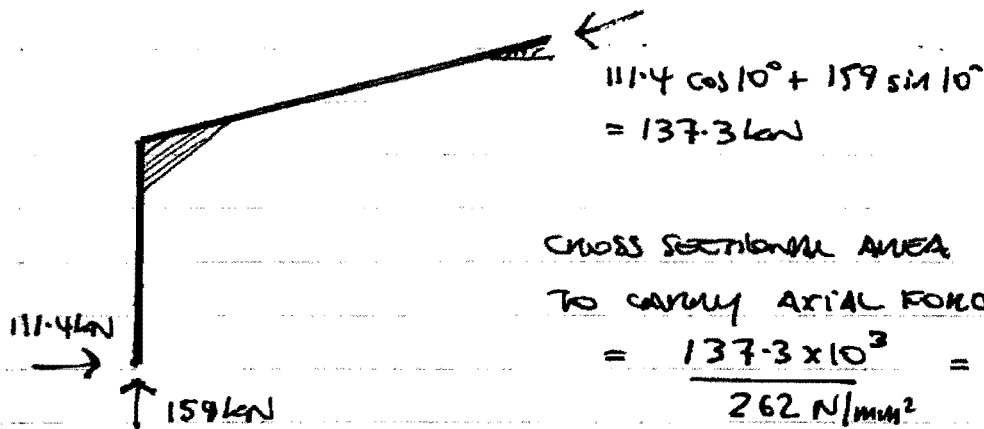




$$\textcircled{1} = 668.4 - \left[(9.93 \times 3 \times 1.5) + 308 \right]$$

$$= \underline{\underline{315.7 \text{ kN/m}}}$$

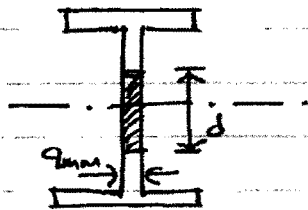
$$\textcircled{2} = \underline{\underline{308 \text{ kN/m}}}$$



CROSS SECTIONAL AREA REQUIRED
TO CARRY AXIAL FORCES

$$= \frac{137.3 \times 10^3}{262 \text{ N/mm}^2} = 524 \text{ mm}^2$$

$$\therefore d = 524 / 4 = 58 \text{ mm}$$



UB 457 x 152 x 67

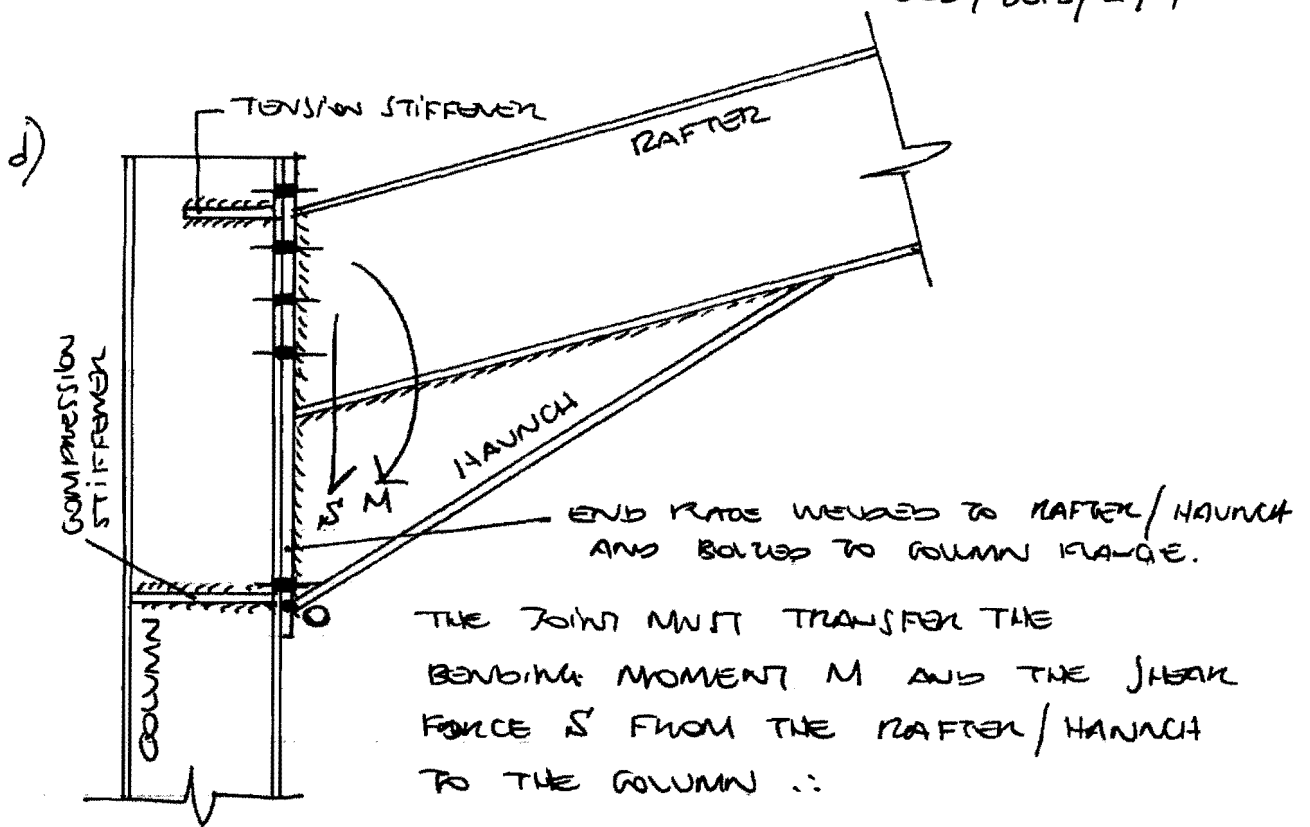
$$\text{REDUCED } M_p = M_p - \sigma_d t d^2 / 4$$

$$= 380.6 \text{ kNm}$$

$$- (262 \times 9 \times 58^2 / 4) \times 10^{-6}$$

$$= 378.6 \text{ kNm} > 315.7$$

\therefore UB 457 x 152 x 67 is SATISFACTORY.

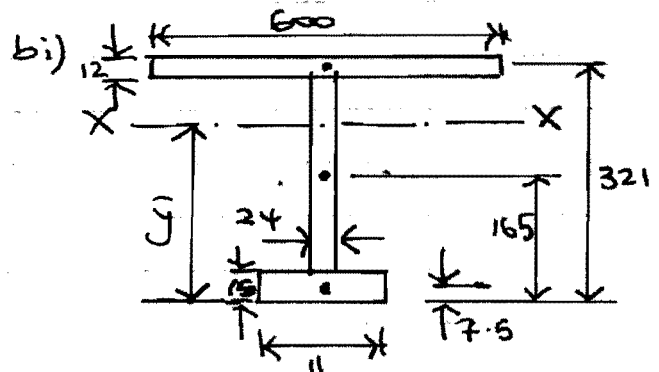
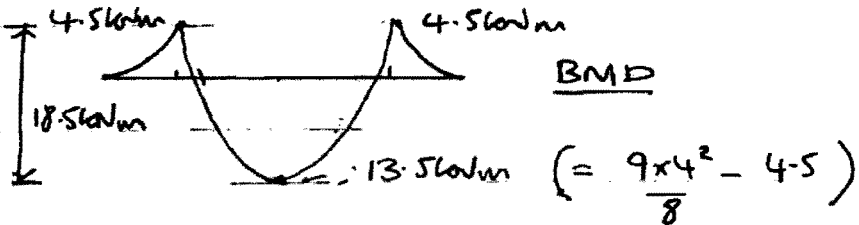
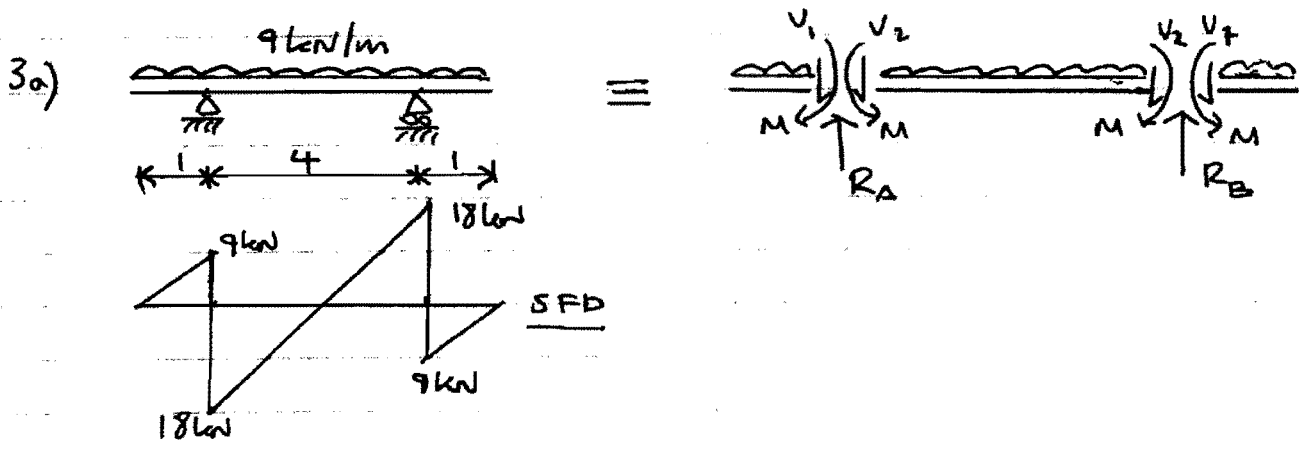


DESIGN CHECK FOR M (RAFTER/HANUCH PIVOTS ABOUT O):

1. CHECK WELD IN TENSION BETWEEN RAFTER AND END-PLATE.
2. CHECK TENSION IN BOLTS, PARTICULARLY 1ST AND 2ND ROW FROM TOP.
3. CHECK WRYING/BENDING OF END-PLATE AND COLUMN FLANGE IN VICINITY OF TOP FLANGE OF RAFTER.
4. CHECK TENSIVE CAPACITY OF COLUMN WEB IN VICINITY OF TOP FLANGE OF RAFTER (INTRODUCE TENSION STIFFENER IF REQUIRED).
5. CHECK BUCKLING OF COLUMN WEB IN VICINITY OF BOTTOM OF HANUCH (INTRODUCE COMPRESSION STIFFENER IF REQUIRED).

DESIGN CHECK FOR S :

1. CHECK SHEAR CAPACITY OF WELD.
2. CHECK SHEAR CAPACITY OF BOLTS (NOTE: BOLTS WILL BE SUBJECT TO COMBINED SHEAR AND TENSION).
3. CHECK BEARING CAPACITY OF END-PLATE AND COLUMN FLANGE AT BOLTS.



$$\bar{y} = \frac{\sum Ay}{\sum A}$$

$$= \frac{[(600 \times 12 \times 321) + (300 \times 24 \times 165) + (15 \times 75 \times 7.5)]}{[(600 \times 12) + (300 \times 24) + (75 \times 15)]}$$

$\therefore \bar{y} = 226 \text{ mm}$

$25 \cdot \frac{E_s}{E_g} = 25 \times \frac{210}{70} = 75 \text{ mm}$

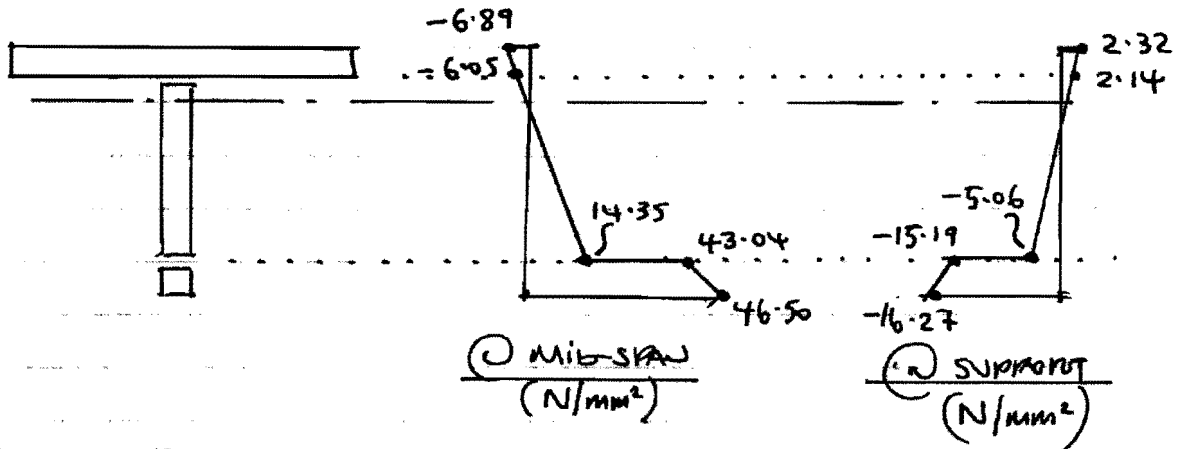
$$I_{xx} = \left[\left(\frac{600 \times 12^3}{12} \right) + (600 \times 12 \times 95^2) \right] + \left[\left(\frac{24 \times 300^3}{12} \right) + (24 \times 300 \times 61^2) \right]$$

$$+ \left[\left(\frac{75 \times 15^3}{12} \right) + (75 \times 15 \times 218.5^2) \right]$$

$\therefore I_{xx} = 199.6 \times 10^6 \text{ mm}^4$

AT MID-SPAN $\sigma(y) = My/I = 13.5 \times 10^6 y / 199.6 \times 10^6 = 0.068y$

AT SUPPORT $\sigma(y) = My/I = 4.5 \times 10^6 y / 199.6 \times 10^6 = 0.023y$

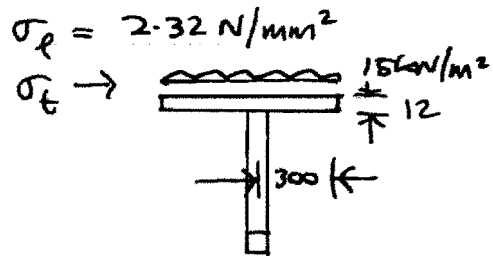
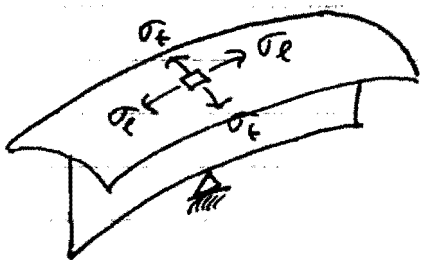


bii) GLASS WEB

MAX. LONGITUDINAL TENSILE STRESS = 14.35 N/mm²

∴ USE FULLY TONGHERED GLASS

GLASS PANNE



$$\therefore M = w l^2 / 2 = (15 \times 0.3^2) / 2 = 0.675 \text{ kNm}$$

$$\therefore \sigma_t = \frac{M}{Z} = \frac{0.675 \times 10^6 \times 6}{1000 \times 12^2} = 28.2 \text{ N/mm}^2$$

$$\therefore \sigma_{\text{resultant}} = \sqrt{2.32^2 + 28.2^2} = \underline{28.3 \text{ N/mm}^2}$$

∴ USE FULLY TONGHERED GLASS

STEEL BLOCK

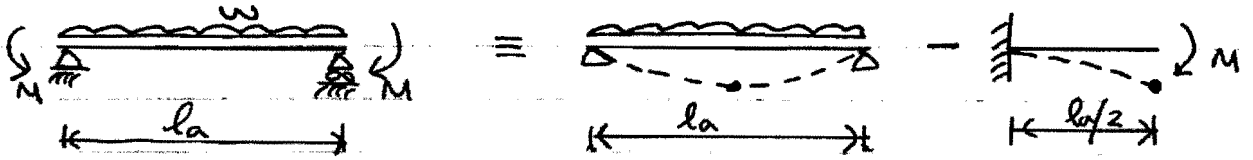
$$\sigma = 46.10 \text{ N/mm}^2 \quad \therefore \underline{\underline{USE S275 STEEL}}$$

biii) TRANSVERSE SHEAR FLOW $q = \frac{S A_c \bar{y}}{I} \Rightarrow \tau = \frac{S A_c \bar{y}}{I t}$

$$\therefore t = \frac{18 \times 10^3 \text{ N} \times 12 \times 600 \times 95}{199.6 \times 10^6 \times 5 \text{ N/mm}^2} = \underline{\underline{12.3 \text{ mm (GLASS-GLASS)}}}$$

$$t = \frac{18 \times 10^3 \text{ N} \times (15 \times 75) \times (226 - 7.5)}{1996 \times 10^6 \times 5 \text{ N/mm}^2} = \underline{\underline{4.4 \text{ mm (STEEL-GLASS)}}}$$

biv) δ AT MID-SPAN:



$$= \frac{5 w l_a^4}{384 EI} - \frac{W}{2} \cdot \frac{l_a^2}{8 EI}$$

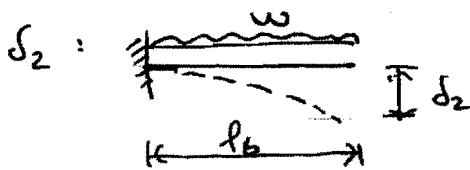
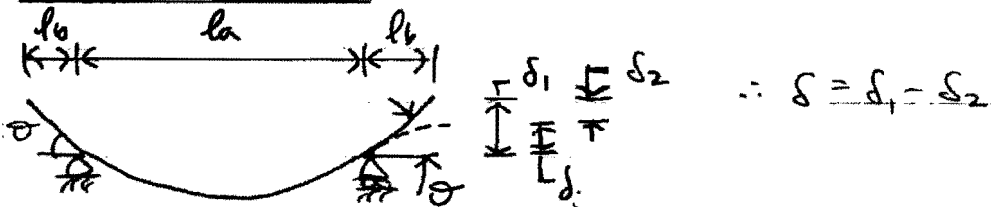
$$= \frac{w l_a^2}{EI} \left(\frac{5 l_a^2 - 24}{384} \right)$$

$$= \frac{w l_a^2}{384 EI} (5 l_a^2 - 24)$$

$$\therefore \delta_{\text{MID SPAN}} = \frac{9 \times 10^3 \times 4^2 (5 \times 4^2 - 24)}{1.6 \times 384 \times 70 \times 10^9 \times 199 \times 10^{-6}}$$

$$\delta_f \text{ (SLS)} = \underline{\underline{0.94 \text{ mm}}} = \text{SPAN} / 4255$$

δ AT FREE END:



$$\delta_2 = \frac{w l_b^4}{8 EI}$$

$$\delta = l_b \theta$$

$$\text{WHERE } \theta = \theta_1 - \theta_2$$

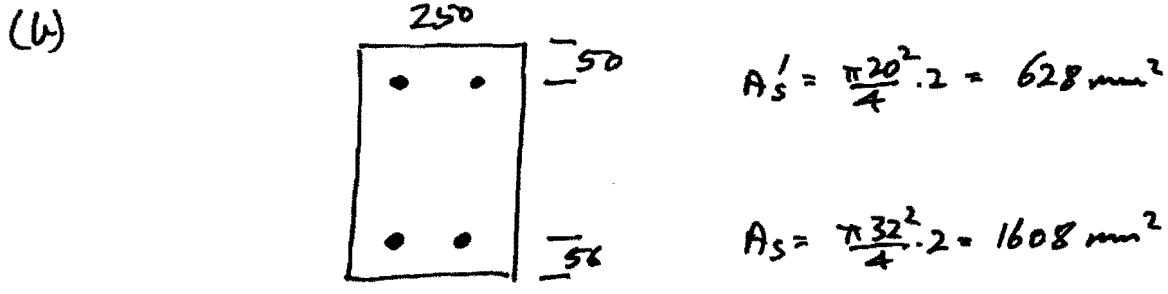
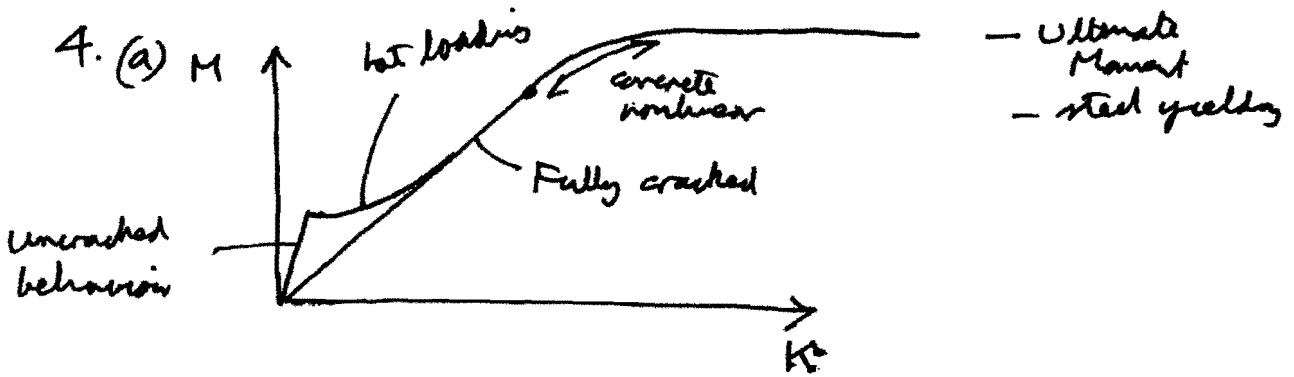
$$\therefore \theta = \left(\frac{w l_a^3}{24 EI} \right) - \left(\frac{W}{2} \cdot \frac{l_a}{2} \cdot \frac{1}{EI} \right)$$

$$\therefore \delta_1 = l_b \left(\frac{w l_a^3}{24EI} - \frac{w l_a l_b^2}{4EI} \right)$$

$$\begin{aligned} \Rightarrow \delta &= \frac{w l_b^4}{8EI} + \frac{w l_b^3 l_a}{4EI} - \frac{w l_a^3 l_b}{24EI} \\ &= \frac{w l_b}{24EI} \left[3 l_b^2 (l_b + 2 l_a) - l_a^3 \right] \end{aligned}$$

$$\begin{aligned} \therefore \delta &= \frac{9 \times 10^3 \times 1}{1.6 \times 24 \times 70 \times 10^9 \times 199.6 \times 10^6} \left[3(1+8) - 4^3 \right] \\ &= \underline{\underline{-0.62 \text{ mm (UPLIFT)}}} = \text{SPAN} / 6451 \end{aligned}$$

- c)
- THICKNESS OF STEEL AND GLASS CAN BE REDUCED FURTHER, THEREBY INCREASING WORKING STRESSES UP TO DESIGN STRENGTHS WITHOUT BREACHING SERVICEABILITY LIMITS.
 - MONOLITHIC GLASS FOR FLANGE IS NOT ADVISABLE AS IT PROVIDES NO REDUNDANCY ON FAILURE. CONSIDER REPLACING WITH LAMINATED GLASS.
 - CONSIDER LONG TERM HOOPING ON ADHESIVES
 - CONSIDER SHEAR DEFORMATION OF ADHESIVE THAT COULD RESULT IN PARTIALLY COMPOSITE T-BEAM RATHER THAN FULLY COMPOSITE T-BEAM.
 - CONSIDER DIFFERENT COEFFICIENTS OF THERMAL EXPANSION IN STEEL AND GLASS LEADING TO STRESSES IN THE ADHESIVE. THIS CAN BE CRITICAL IN LONG BEAMS.
 - THE FREE END OF THE WEB IS IN COMPRESSION OVER THE SUPPORT. CHECK RESISTANCE TO LATERAL TORSIONAL BUCKLING OR PROVIDE ADEQUATE RESTRAINT.
-

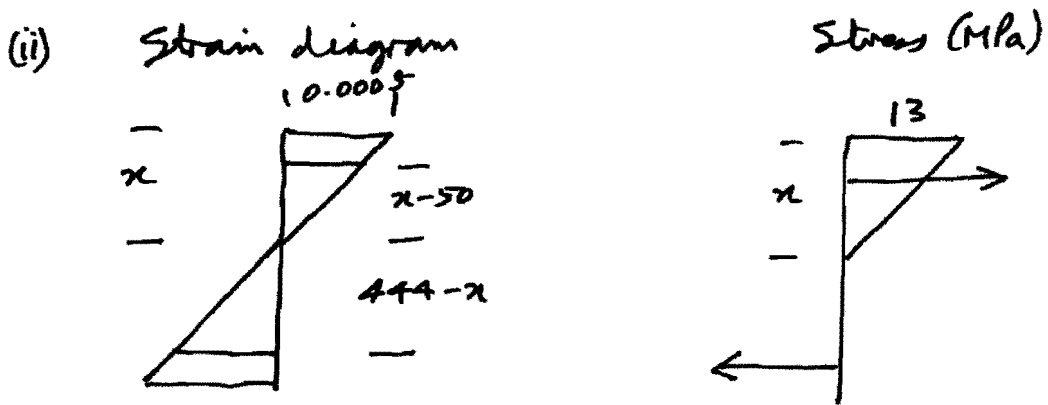


(i) 1st cracking when tensile stress at bottom = 3 MPa

$$\frac{\sigma}{y} = \frac{M}{I} \Rightarrow M = \frac{3}{250} \cdot \frac{500^3 \cdot 250}{12} \quad (\text{N, mm})$$

$$M = 31.25 \text{ kNm}$$

Curvature $\frac{\sigma}{E_c} \cdot \frac{1}{250} = \frac{3}{26 \cdot 10^3} \cdot \frac{1}{250} = 0.46 \cdot 10^{-6} \text{ mm}^{-1}$
 not asked for



Stress in top steel = $\frac{(x-50)}{x} \cdot 0.0005 \cdot E_s \cdot 200 \cdot 10^3$ (comp)

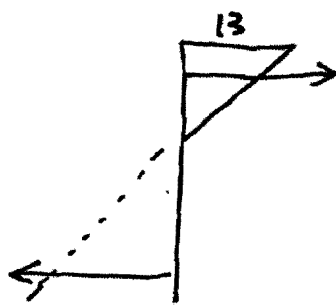
Stress in bottom steel = $\frac{(444-x)}{x} \cdot 100$ (tension)

Calculate x by satisfying longitudinal equilibrium

$$\underbrace{13 \cdot \frac{250 \cdot x}{2}}_{\text{concrete}} + \underbrace{100 \cdot 628 \cdot \frac{(x-50)}{x}}_{\text{top steel}} = \underbrace{\frac{(444-x)}{x} \cdot 1608 \cdot 100}_{\text{bottom steel}}$$

Quadratic in $x \Rightarrow x = 152.5 \text{ mm}$ (reasonable)

Can now calculate all strains \Rightarrow stresses



$$\epsilon = 0.000335 \Rightarrow \sigma = 67 \text{ MPa (comp)}$$

$$\epsilon = 0.0009586 \Rightarrow \sigma = 191 \text{ MPa (tens)}$$

Take moments about top fibre (or any other defined point)

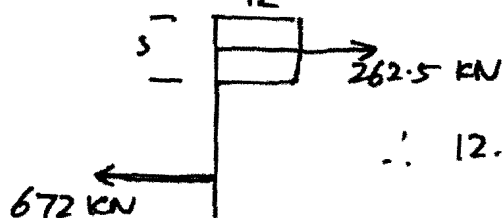
$$191 \cdot 1608 \cdot 444 - 67 \cdot 50 \cdot 628 - 13 \cdot \frac{250 \cdot 152 \cdot 2}{2} \cdot \frac{152 \cdot 2}{3} = \underline{\underline{109.2 \text{ kNm}}} \quad (\text{N, mm})$$

$$(\text{Curvature} = \frac{13}{26 \cdot 10^3} \cdot \frac{1}{102 \cdot 2} = 4.89 \cdot 10^{-6} \text{ mm}^{-1})$$

(iii) Ultimate Moment Capacity assuming all steel yields

$$\text{Stress in concrete} = \frac{30 \cdot 0.6}{1.5} = 12 \text{ MPa}$$

$$\text{Stress in steel yielding} = \frac{460}{1.1} = 418 \text{ MPa}$$



$$\therefore 12 \cdot 250 \cdot s = (672 - 262.5) \cdot 10^3$$

$$\Rightarrow s = 136.5 \text{ mm.}$$

3D3/2013/4/3

Take moments about the top

$$M = 672 \times 444 - 262.5 \cdot 50 - \frac{136.5 \cdot 12 \cdot 250^3}{2 \cdot 1000} \cdot \frac{136.5}{2}$$

(kN, mm)

$$= \underline{\underline{271.3 \text{ kNm}}}$$

$$\text{Curvature} = \frac{0.0035}{136.5} = 25.6 \cdot 10^{-6} \text{ mm}^{-1}$$

$$\text{Strain in top steel} = 25.6 \cdot (136.5 - 50) = 0.0022$$

$$\text{Stress in top steel} = 442.9 \text{ N/mm}^2$$

(not yielding)

Examiner's comments to be attached to the crib.

A disappointing paper with raw marks in all questions <50%. The candidates were clearly under time pressure but this does not explain the lack of logical thought in the bits they did do.

Qu 1. Steel design for a grandstand

The main problem here was that most of the candidates only checked for one of the three conditions (strength, stiffness and buckling), although the first two were specifically asked for and they were given a strong hint about the need to think about the buckling. Quite a large number could not determine the load in the column at the base, either leaving out the wind load, or leaving out the snow load, or simply being unable to apply equilibrium properly. The last part, where they were asked (implicitly) to find an alternative load path for the wind load was very poorly done - very few seemed able to think in three dimensions.

Qu 2. Steel Portal Frame

The most popular question. The methods adopted by the candidates were largely correct, but there were several errors and omissions in the calculations. The first part asked the candidates to estimate the size of the rafter by assuming a fixed-ended condition. Most candidates successfully derived (or recalled) that for a fixed ended beam subjected to UDL, $M_p = wl^2/16$, but several candidates used the full span between the columns rather than the clear span between the haunches. Part *b* of the question asked the candidates to derive the plastic moment at the plastic hinges of a portal frame. Most students set this up correctly by equating the external work done to the work dissipated in the hinges, but several candidates failed to notice that the total rotation in the hinge closest to the haunch was $(\theta_1 + \theta_2)$ rather than θ_1 . The free body diagrams required to solve Part *c* of the question were generally correct, but the most common error was an inconsistent sign convention leading to an incorrect direction of the bending moment at the apex haunch. Despite these errors, most candidates were able to sketch a sensible bending moment diagram. The final part of the question asked the candidates to consider the design of the column-rafter haunch. There were 'easy' marks to be gained in this final part, but few candidates attempted it. Those that did secured most of the marks allocated to this part.

Qu 3. Composite Glass/Steel beam

Very disappointing question. It could easily have been set to the 1A students as a revision exercise, since it is essentially the application of 1A principles to a new material, but it is almost as though they had put that knowledge away, never to be used again. They were unable to distinguish between loads per unit length and loads per unit area, and a significant number tried to use the density of the steel and the glass to transform the section when determining the second moment of area, rather than Young's modulus. Some simply ignored the distinction between two materials. Even if they got it right, they seemed incapable of sketching the expected stress distribution over the section. The crib expected them to take account of transverse bending of the flange when determining the stresses over the support

but no one attempted that and it wasn't penalised given the overall difficulty. Two candidates included it in their answers to part (c) - "what else would you check?" Very few of them made any serious attempt at calculating the deflections.

Qu 4. Moment curvature relationship of a reinforced concrete beam

Quite a few candidates did not appear to know what a moment-curvature relationship was, and several did not distinguish between the uncracked and cracked behaviour. The biggest problem was that almost nobody used axial equilibrium in the beam for determining where the neutral axis was located, which was essential for determining the cracked-elastic and ultimate load stress states, and wrote various degrees of nonsense depending on where they thought the neutral axis might be. Several used the design equations to determine the ultimate moment capacity, for which they were given some credit. The overall impression from this question was that they were trying to remember "the formula for ..." rather than applying fundamental principles.

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