

ENGINEERING TRIPOS PART IIB

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Wednesday 5 May 2004 9 to 10.30

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Module 4B14

SOLAR-ELECTRONIC POWER: GENERATION AND DISTRIBUTION

*Answer not more than **three** questions*

*The approximate percentage of marks allocated to each part of a question is shown in the right margin*

*There is a one-page datasheet attachment*

**You may not start to read the  
questions printed on the  
subsequent pages of this question  
paper until instructed that you  
may do so by the Invigilator**

(TURN OVER)

1 A p-n junction Si solar cell has the following junction parameters under dark conditions:

(i)	built in potential	<b>0.93 eV</b>
(ii)	p-doping	<b><math>10^{23} \text{ m}^{-3}</math></b>
(iii)	minority carrier hole life time	<b>1 ns</b>
(iv)	minority carrier electron lifetime	<b>1 <math>\mu\text{s}</math></b>
(v)	electron diffusion length	<b>200 <math>\mu\text{m}</math></b>
(vi)	hole diffusion length	<b>0.5 <math>\mu\text{m}</math></b>
(vii)	intrinsic carrier concentration	<b><math>2.0 \times 10^{16} \text{ m}^{-3}</math></b>

The junction temperature is **300K**. Assume that the number of available states at the edge of the valence band and conduction band are equal, i.e.  $N_v = N_c$ . The junction area is  **$10^{-3} \text{ m}^2$** . The junction is formed so that the n-type region extends **1  $\mu\text{m}$**  from the surface, followed by the p-type region extending a further **300  $\mu\text{m}$**  to form the bulk of the cell. Calculate the following;

- a) Doping of the n-type region [30%]
- b) If the transport of electrons outside the depletion region is only due to diffusion;
- (i) calculate the peak value of the minority carrier density in the p-type bulk region when a forward voltage of **0.5V** is applied across the junction, and
  - (ii) sketch the minority carrier distribution. [40%]
- c) When the surface of the p-n junction is exposed to the solar system an open circuit voltage of **0.6V** is measured. Estimate the ideal short circuit current and optical generation rate under these conditions. Hence sketch the corresponding current ( $I$ ) vs voltage ( $V$ ) characteristic for the p-n junction when operating as a solar cell. [30%]

State all assumptions made

2 a) Would the energy conversion efficiency of a Si solar cell be higher for **600 nm** light or **800 nm** light? Give reasons for your answer.

Hence comment on the theoretical limit to terrestrial photovoltaic solar energy conversion efficiency. [20%]

b) In practice what limits the open circuit voltage  $V_{oc}$  and short circuit current  $I_{sc}$  available from a Si solar cell? [20%]

c) Draw the equivalent circuit for a solar cell and explain the physical origin of each component. [30%]

d) It is common to apply a thin transparent insulating layer on the front surface of Si solar cells.

(i) What is the purpose of this layer?

(ii) If the layer has a refractive index of **2.0**, calculate an appropriate thickness for the layer. State reasons for any assumptions made.

(iii) What would the ideal refractive index be? [30%]

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3. A multi-crystalline Si solar cell has the following measured parameters:

Short circuit current under AM 1.5 solar light	2.0 A
Dark $I$ - $V$ characteristic ideality factor	1.2
Open circuit voltage $V_{oc}$	0.55 V

Cell temperature was 300 K during all measurements.

a) What is the typical dark current that can be expected from this cell under reverse bias? [20%]

b) Estimate the power conversion efficiency of the cell if it has a surface area of  $10^{-2} m^2$  and AM 1.5 light is considered to have an energy flux of  $1 kW m^{-2}$  [25%]

c) Give a better estimate for the efficiency for the cell taking into account its contact resistance, measured to be  $0.05 \Omega$ , and assuming its reverse leakage resistance under dark conditions is immeasurably large. [25%]

d) The temperature coefficient for the open circuit voltage ( $dV_{oc}/dT$ ) of the multi-crystalline solar cell in (a) is  $-2.0 mVK^{-1}$ . Identify the main solar cell parameter which gives rise to the temperature coefficient and explain why it does so.

Calculate the value of this parameter at an operating temperature of 330K. [30%]

4. a) Explain how it is possible to have power dissipation within a solar cell when it is connected with other cells to form a power module. [20%]
- b) Describe the common control strategy used for maximising power output from a large solar array. Comment on whether it would be viable to have a single control unit for a photovoltaic generator made up from power modules mounted on south, west and east facing facades of a multi-storey office block. [25%]
- c) Show in block diagram form the key elements of a grid connected photovoltaic power generator. By referring to the block diagram, discuss the importance of high frequency DC power switching for efficient grid connection of photovoltaic arrays. [30%]
- d) Draw the phasor diagram and AC circuit representation for a photovoltaic generating system connected onto the power network. What are the key assumptions which are inherent in such a representation? [25%]

**END OF PAPER**



**Paper 4B14**
**SOLAR CELL ELECTRONIC POWER: GENERATION AND  
DISTRIBUTION**
**Formulae and Constants**

Reflection co-efficient from the third layer of a 3 layer system comprising of a thin film sandwiched between two bulk materials extending away from their interfaces with the thin film:

$$R = \frac{r_1^2 + r_2^2 + 2r_1r_2 \cos \vartheta}{1 + r_1^2 r_2^2 + 2r_1r_2 \cos \vartheta}$$

$$\text{where } r_1 = \frac{n_1 - n_2}{n_1 + n_2} \quad r_2 = \frac{n_2 - n_3}{n_2 + n_3} \quad \vartheta = \frac{2\pi n_2 d}{\lambda}$$

$n_1$ ,  $n_2$  and  $n_3$  are the refractive indices of 3 materials  $m_1$ ,  $m_2$  and  $m_3$  respectively:  $d$  is the thickness of the thin film  $m_2$  sandwiched between materials  $m_1$  and  $m_2$ . Direction of light flow is taken to be from  $m_1$  to  $m_3$ .

**Fill Factor for a solar cell**

$$FF_o = \frac{\frac{qV_{oc}}{kT} - \ln\left(\frac{qV_{oc}}{kT} + 0.72\right)}{\frac{qV_{oc}}{kT} + 1}$$

where  $V_{oc}$  is the open circuit voltage for the cell.

**Constants**

Electronic charge unit      **q:  $1.602 \times 10^{-19}$  C**

Boltzmann's Constant      **k:  $1.38 \times 10^{-23}$  Jk<sup>-1</sup>**

Speed of light      **c:  $3 \times 10^8$  mS<sup>-1</sup>**

Planck's Constant      **h:  $6.626 \times 10^{-34}$  Js**

Dielectric permittivity free space  $\epsilon_0$ :  **$8.85 \times 10^{-12}$  F m<sup>-1</sup>**

Relative permittivity of Si  $\epsilon_r$ : **11.9**

Refractive index (for weakly and non-absorbing wavelengths)  **$n = \epsilon_r^{0.5}$**

Band-gap energy of Si: **1.12 qV J**