# Version NAF/2

EGT2 ENGINEERING TRIPOS PART IIA

Monday 2 May 2016 2 to 3.30

### Module 3C9

# FRACTURE MECHANICS OF MATERIALS AND STRUCTURES

Answer not more than three questions.

All questions carry the same number of marks.

The *approximate* percentage of marks allocated to each part of a question is indicated in the right margin.

Write your candidate number <u>not</u> your name on the cover sheet.

#### STATIONERY REQUIREMENTS

Single-sided script paper

# SPECIAL REQUIREMENTS TO BE SUPPLIED FOR THIS EXAM

CUED approved calculator allowed Attachment: 3C9 datasheet (8 pages). Engineering Data Book

# 10 minutes reading time is allowed for this paper.

You may not start to read the questions printed on the subsequent pages of this question paper until instructed to do so.

1 (a) Explain why the energy release rate G and the stress intensity factor K are equivalent loading parameters in linear elastic fracture mechanics. [20%]

(b) Figure 1 shows an asymmetric double cantilever beam, of thickness B, made from an elastic-brittle solid of Young's modulus E and toughness  $G_{\rm C}$ . The beam is subjected to an end load P, to produce a crack mouth opening displacement u.

(i) Show that the energy release rate is given by

$$G = \frac{P^2}{2B} \frac{\partial C}{\partial a},$$

where C = u / P is the compliance of the specimen and *a* is the crack length. [25%]

(ii) Thereby obtain an expression for the failure load  $P_c$  in terms of  $G_c$ , a,  $h_1$ ,  $h_2$  and B. [40%]

(iii) Comment on the expected crack path in the context of mode mixity. [15%]

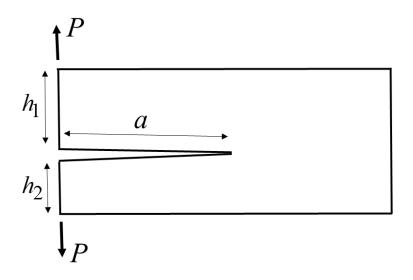


Fig. 1

2 (a) It is commonly observed that the stress intensity factor  $K_R$  for continued crack growth increases with crack extension  $\Delta a$  for a metallic alloy. Explain the physical basis for this observation. Show on a sketch of  $K_R$  versus  $\Delta a$  how this behaviour can lead to stable crack growth before fast fracture, and state the conditions for instability.

(b) A welding operation on a large steel plate imparts a longitudinal residual stress distribution, through the thickness of the plate, as sketched in Fig. 2. Poor welding practice leads to the existence of a through-thickness crack, of semi-length a = 10 mm, at the centre of the plate as shown. The plane of the crack is normal to the stress field.

(i) Calculate the magnitude of the stress intensity factor K at each crack tip due to the residual stress field. [20%]

(ii) In service, the crack extends by stress corrosion. Obtain expressions for K as a function of crack semi-length a, for a in the range 10 mm to 100 mm, and state the values of K for a = 30 mm, 90 mm and 100 mm.

(iii) An additional longitudinal stress state is now applied to the plate by external loading, and the total value of K is obtained by superposition of the residual and applied stress states. Explain the limitations of the assumption of linear superposition.

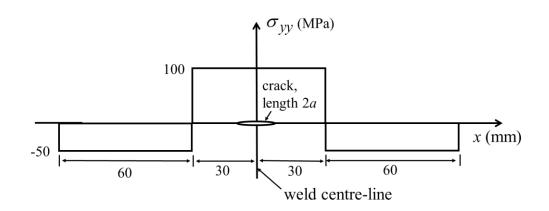


Fig. 2

[30%]

[35%]

[15%]

### 3 Account for the following observations:

| (a)<br>weld | It is necessary to qualify the safety of a nuclear reactor pressure vessel made from<br>ded steel using the J-integral approach rather than linear elastic fracture mechanics. | [25%] |
|-------------|--|-------|
| (b)         | Metallic alloys are tougher but weaker than freshly drawn silica glass.  | [25%] |
| (c)<br>root | Non-propagating fatigue cracks can exist at the root of a small notch but not at the of a large notch.   | [25%] |
| (d)         | Severe turbulence on a metallic aircraft wing can extend its fatigue life.   | [25%] |

4 (a) Specimens of 7075-T6 aluminium alloy were subjected to fully reversed cyclic loading. Failure occurred after 545 cycles when tested at a cyclic plastic strain range  $\Delta \varepsilon^{p} = 0.01$ , and after 2000 cycles at  $\Delta \varepsilon^{p} = 0.005$ . Calculate the constants in the Coffin-Manson fatigue law for this material. [25%]

(b) The amplitude of cyclic stress-stress strain response of the 7075-T6 aluminium alloy is idealised by the bi-linear relation

$$\begin{split} \frac{\Delta\varepsilon}{2} &= \frac{1}{E} \frac{\Delta\sigma}{2} \ , \qquad \qquad \text{for} \quad \frac{\Delta\sigma}{2} \leq \sigma_{\rm Y} \\ \frac{\Delta\varepsilon}{2} &= \frac{\sigma_{\rm Y}}{E} + \frac{1}{E_{\rm T}} \left( \frac{\Delta\sigma}{2} - \sigma_{\rm Y} \right) \ , \qquad \qquad \text{for} \quad \frac{\Delta\sigma}{2} > \sigma_{\rm Y} \end{split}$$

in terms of the Young's modulus E = 70 GPa, post-yield tangent modulus  $E_{\rm T} = 7$  GPa, and yield strength  $\sigma_{\rm Y} = 280$  MPa. A large sheet of the 7075-T6 aluminium alloy contains a circular hole (with elastic stress concentration factor  $k_T = 3$ ) and the plate is subjected to a fully reversed uniaxial cyclic stress of amplitude  $\Delta \sigma / 2 = 250$  MPa. Estimate the number of cycles for crack initiation by making use of Neuber's rule,  $k_{\sigma}k_{\varepsilon} = k_{\rm T}^2$ . [50%]

(c) Explain mean stress relaxation at a notch root and whether Neuber's rule takes it into account. [25%]

#### **END OF PAPER**